TCSS 422: OPERATING SYSTEMS

Translation Lookaside Buffer, Smaller Tables, Multi-level Page Tables

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OBJECTIVES – 12/2

- **Questions from 11/30**
- Assignment 2 - Dec 3
- Quiz 3 – Synchronized Array - Dec 2
- Tutorial 2 – Pthread, locks, conditions tutorial - Nov 30
- Assignment 3 (as a Tutorial) - Dec 17
- Quiz 4 - Page Tables - Dec 13
- Chapter 18: Introduction to Paging
- Chapter 19: Translation Lookaside Buffer (TLB)
  - TLB Algorithm, Hit-to-Miss Ratios
- Chapter 20: Paging: Smaller Tables
  - Smaller Tables, Multi-level Page Tables, N-level Page Tables

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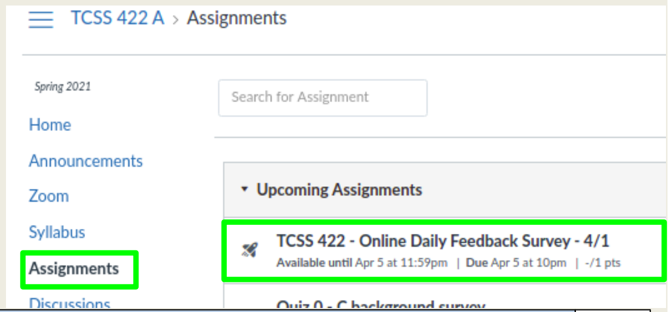
ONLINE DAILY FEEDBACK SURVEY

- Daily Feedback Quiz in Canvas – Available After Each Class
- Extra credit available for completing surveys ***ON TIME***
- Tuesday surveys: due by ~ Wed @ 11:59p
- Thursday surveys: due ~ Mon @ 11:59p



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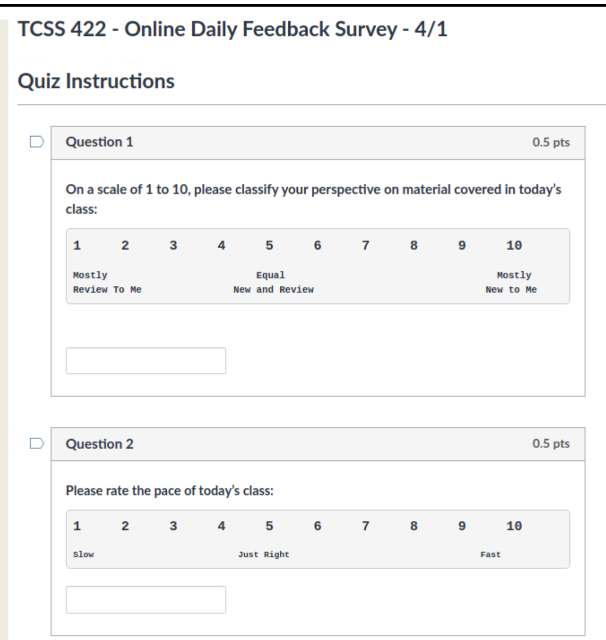

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MATERIAL / PACE

- Please classify your perspective on material covered in today's class (25 respondents):
- 1-mostly review, 5-equal new/review, 10-mostly new
- **Average – 6.02 (↓ - previous 6.29)**

- Please rate the pace of today's class:
- 1-slow, 5-just right, 10-fast
- **Average – 5.46 (↓ - previous 5.67)**

FEEDBACK

- ***Requesting more time on assignment 2, if possible.***
- ***This is unrelated, but I was hoping if an extension can be granted for assignment 2***
- ***This is unrelated, but I was hoping if an extension can be granted for assignment 2 due to conflicts with assignments from other classes***
- ***Can we get extensions on the quiz and assignment 2 due to this week? A lot of us have been busy with other classes and could use the time to turn in a sufficient enough product. Thank you!***

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CHAPTER 18: INTRODUCTION TO PAGING

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Consider a 4GB Computer with 4KB (4096 byte) pages. How many pages would fit into physical memory?

- 2^32 / 2^20 = 2^12 pages
- 2^32 / 2^12 = 2^20 pages
- 2^32 / 2^16 = 2^16 pages
- 2^32 / 2^8 = 2^24 pages
- None of the above

Start the presentation to see live content. For screen share software, share the entire screen. Get help at **pollev.com/app**

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For the 4GB computer example, how many bits are required for the VPN?

24 VPN bits (indexes 2^24 locations)

16 VPN bits (indexes 2^16 locations)

20 VPN bits (indexes 2^20 locations)

12 VPN bits (indexes 2^12 locations)

None of the above

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For the 4GB computer example, how many bits are available for page status bits?

32 - 12 VPN bits = 20 status bits

32 - 24 VPN bits = 8 status bits

32 - 16 VPN bits = 16 status bits

32 - 20 VPN bits = 12 status bits

None of the above

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For the 4GB computer, how much space does this page table require? (number of page table entries x size of page table entry)

2^20 entries x 4b = 4 MB

2^12 entries x 4b = 16 KB

2^16 entries x 4b = 256 KB

2^24 entries x 4b = 64 MB

None of the above

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For the 4GB computer, how many page tables (for user processes) would fill the entire 4GB of memory?

4 GB / 16 KB = 65,536

4 GB / 64 MB = 256

4GB / 256 KB = 16,384

4GB / 4MB = 1,024

None of the above

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PAGING SYSTEM EXAMPLE

- Consider a 4GB Computer:
- With a 4096-byte page size (4KB)
- How many pages would fit in physical memory?

- Now consider a page table:
- For the page table entry, how many bits are required for the VPN?
- If we assume the use of 4-byte (32 bit) page table entries, how many bits are available for status bits?
- How much space does this page table require?
  # of page table entries x size of page table entry
- How many page tables (for user processes) would fill the entire 4GB of memory?

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CHAPTER 19: TRANSLATION LOOKASIDE BUFFER (TLB)

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TRANSLATION LOOKASIDE BUFFER

- Legacy name…
- Better name, "Address Translation Cache"
- TLB is an on CPU cache of address translations
  - virtual → physical memory

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COUNTING MEMORY ACCESSES

- Example: Use this Array initialization Code

```
int array[1000];
...
for (i = 0; i < 1000; i++)
        array[i] = 0;
```

- Assembly equivalent:

```
0x1024 movl $0x0,(%edi,%eax,4)
0x1028 incl %eax
0x102c cmpl $0x03e8,%eax
0x1030 jne 0x1024
```


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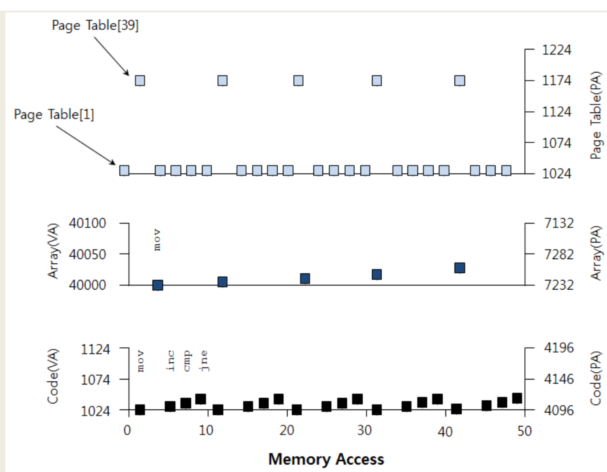
VISUALIZING MEMORY ACCESSES:
FOR THE FIRST 5 LOOP ITERATIONS

- Locations:
  - Page table
  - Array
  - Code
- 50 accesses for 5 loop iterations



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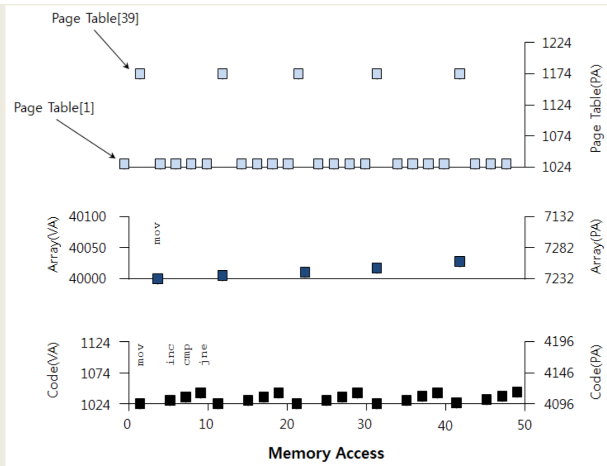
TRANSLATION LOOKASIDE BUFFER - 2

- **Goal:** Reduce access to the page tables
- **Example:** 50 RAM accesses for first 5 for-loop iterations
- Move lookups from RAM to TLB by caching page table entries



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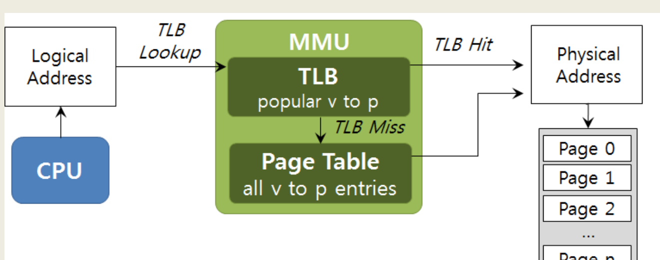
TRANSLATION LOOKASIDE BUFFER (TLB)

- Part of the CPU's Memory Management Unit (MMU)
- Address translation cache



Address Translation with MMU

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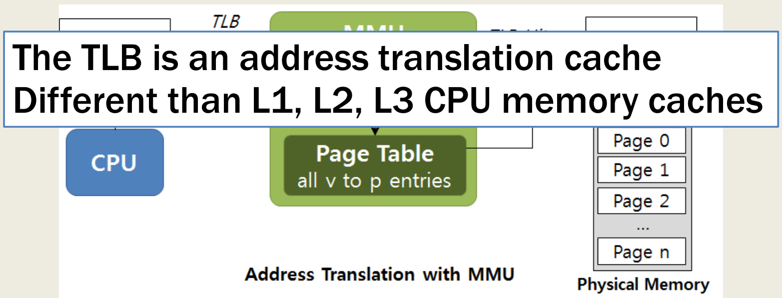
TRANSLATION LOOKASIDE BUFFER (TLB)

- Part of the CPU's Memory Management Unit (MMU)
- Address translation cache



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TLB BASIC ALGORITHM

- For: array based page table
- Hardware managed TLB

```
VPN = (VirtualAddress & VPN_MASK ) >> SHIFT
(Success , TlbEntry) = TLB_Lookup(VPN)
   if(Success == True){ // TLB Hit
   if(CanAccess(TlbEntry.ProtectBits) == True ){
       Offset = VirtualAddress & OFFSET_MASK
       PhysAddr = (TlbEntry.PFN << SHIFT) | Offset
       AccessMemory( PhysAddr )
   }else RaiseException(PROTECTION_ERROR)
```

Generate the physical address to access memory

TLB BASIC ALGORITHM - 2

```
    else{ //TLB Miss
        PTEAddr = PTBR + (VPN * sizeof(PTE))
        PTE = AccessMemory(PTEAddr)
        (…)  // Check for, and raise exceptions…

        TLB_Insert( VPN , PTE.PFN , PTE.ProtectBits)
        RetryInstruction()
    }
}
```

Retry the instruction… (requery the TLB)

TLB – ADDRESS TRANSLATION CACHE

- Key detail:
- For a TLB miss, we first access the page table in RAM to populate the TLB… **we then requery the TLB**
- **All address translations go through the TLB**

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OBJECTIVES – 5/25

- Questions from 5/25
- Assignment 2
- Activity – Memory Segmentation (available in Canvas)
- Tutorial 2 – Pthread, locks, conditions tutorial
- Quiz 4 - Page Tables - Dec 13
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TLB EXAMPLE

```
0:      int sum = 0 ;
1:      for( i=0; i<10; i++){
2:              sum+=a[i];
3:      }
```

- Example:
- Program address space: 256-byte
  - Addressable using 8 total bits (2^8)
  - 4 bits for the VPN (16 total pages)
- Page size: 16 bytes
  - Offset is addressable using 4-bits
- Store an array: of (10) 4-byte integers

OFFSET 00 04 08 12 16

	00	04	08	12
VPN = 00				
VPN = 01				
VPN = 03				
VPN = 04				
VPN = 05				
VPN = 06		a[0]	a[1]	a[2]
VPN = 07	a[3]	a[4]	a[5]	a[6]
VPN = 08	a[7]	a[8]	a[9]	
VPN = 09				
VPN = 10				
VPN = 11				
VPN = 12				
VPN = 13				
VPN = 14				
VPN = 15				

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TLB EXAMPLE - 2

```
int sum = 0 ;
for( i=0; i<10; i++){
        sum+=a[i];
}
```

- Consider the code above:
- Initially the TLB does not know where a[] is
- Consider the accesses:
- a[0], a[1], a[2], a[3], a[4], a[5], a[6], a[7], a[8], a[9]
- **How many pages are accessed?**
- **What happens when accessing a page not in the TLB?**

	OFFSET 00	04	08	12 (–16)
VPN = 00				
VPN = 01				
VPN = 03				
VPN = 04				
VPN = 05				
VPN = 06		a[0]	a[1]	a[2]
VPN = 07	a[3]	a[4]	a[5]	a[6]
VPN = 08	a[7]	a[8]	a[9]	
VPN = 09				
VPN = 10				
VPN = 11				
VPN = 12				
VPN = 13				
VPN = 14				
VPN = 15				

TLB EXAMPLE - 3

```
int sum = 0 ;
for( i=0; i<10; i++){
        sum+=a[i];
}
```

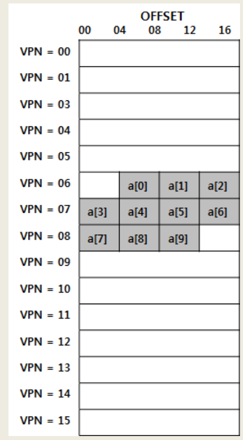
- For the accesses: a[0], a[1], a[2], a[3], a[4],
- a[5], a[6], a[7], a[8], a[9]

- How many are hits?
- How many are misses?
- What is the hit rate? (%)
  - 70% (3 misses one for each VP, 7 hits)

	OFFSET 00	04	08	12 (–16)
VPN = 00				
VPN = 01				
VPN = 03				
VPN = 04				
VPN = 05				
VPN = 06		a[0]	a[1]	a[2]
VPN = 07	a[3]	a[4]	a[5]	a[6]
VPN = 08	a[7]	a[8]	a[9]	
VPN = 09				
VPN = 10				
VPN = 11				
VPN = 12				
VPN = 13				
VPN = 14				
VPN = 15				

TLB EXAMPLE - 4

```
int sum = 0 ;
for( i=0; i<10; i++){
        sum+=a[i];
}
```



- What factors affect the hit/miss rate?
  - Page size
  - Data/Access locality (how is data accessed?)
    - Sequential array access vs. random array access
  - Temporal locality
  - Size of the TLB cache (how much history can you store?)

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CHAPTER 20: PAGING: SMALLER TABLES

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LINEAR PAGE TABLES

- Consider array-based page tables:
  - Each process has its own page table
  - 32-bit process address space (up to 4GB)
  - With 4 KB pages
  - 20 bits for VPN
  - 12 bits for the page offset

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LINEAR PAGE TABLES - 2

- Page tables stored in RAM
- Support potential storage of 2^{20} translations
  = 1,048,576 pages per process @ 4 bytes/page
- Page table size 4MB / process

$$\text{Page table size} = \frac{2^{32}}{2^{12}} * 4Byte = 4MByte$$

- Consider 100+ OS processes
  - Requires 400+ MB of RAM to store process information

LINEAR PAGE TABLES - 2

- Page tables stored in RAM
- Support potential storage of 2^{20} translations
  = 1,048,576 pages per process @ 4 bytes/page
- Page table size 4MB / process

Page tables are <u>too big</u> and consume too much memory.

Need Solutions …

- Consider 100+ OS processes
  - Requires 400+ MB of RAM to store process information

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PAGING: USE LARGER PAGES

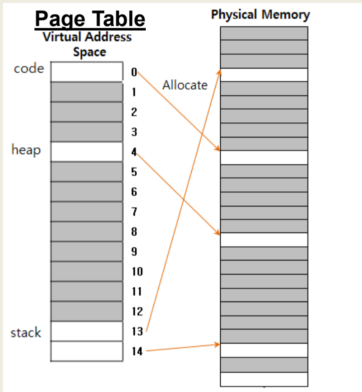
- **Larger pages** = 16KB = 2^{14}
- 32-bit address space: 2^{32}
- 2^{18} = 262,144 pages

$$\frac{2^{32}}{2^{14}} * 4 = 1MB \text{ per page table}$$

- Memory requirement cut to ¼
- However pages are huge
- Internal fragmentation results
- 16KB page(s) allocated for small programs with only a few variables

PAGE TABLES: WASTED SPACE

- Process: 16KB Address Space w/ 1KB pages



A 16KB Address Space with 1KB Pages

PFN	valid	prot	present	dirty
10	1	r-x	1	0
-	0	-	-	-
-	0	-	-	-
-	0	-	-	-
15	1	rw-	1	1
…	…	…	…	…
-	0	-	-	-
3	1	rw-	1	1
23	1	rw-	1	1

A Page Table For 16KB Address Space

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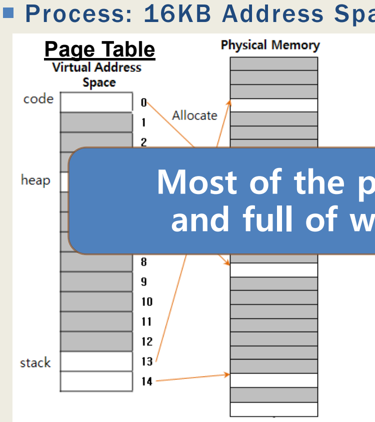
PAGE TABLES: WASTED SPACE

- Process: 16KB Address Space w/ 1KB pages



PFN	valid	prot	present	dirty
				0
				-
				-
				-
15	1	rw-	1	1
…	…	…	…	…
-	0	-	-	-
3	1	rw-	1	1
23	1	rw-	1	1

Most of the page table is unused and full of wasted space. (73%)

A 16KB Address Space with 1KB Pages

A Page Table For 16KB Address Space

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WE WILL RETURN AT 2:40PM

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MULTI-LEVEL PAGE TABLES

- Consider a page table:
- 32-bit addressing, 4KB pages
- 2^{20} page table entries
- Even if memory is sparsely populated the *per process* page table requires:

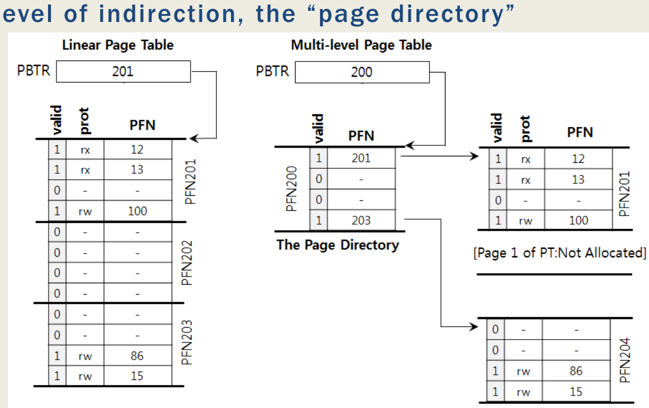
$$\text{Page table size} = \frac{2^{32}}{2^{12}} * 4Byte = 4MByte$$

- Often most of the 4MB *per process* page table is empty
- Page table must be placed in 4MB contiguous block of RAM

- MUST SAVE MEMORY!

MULTI-LEVEL PAGE TABLES - 2

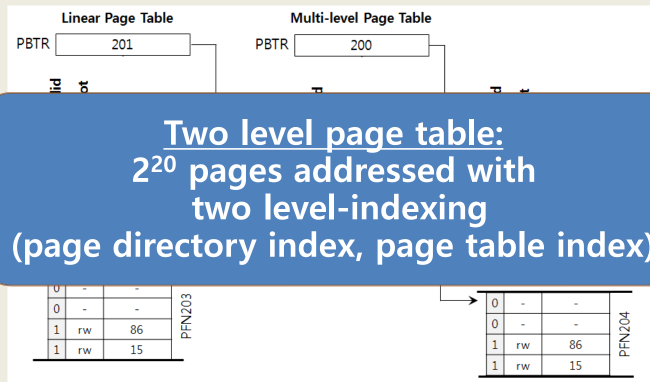
- Add level of indirection, the "page directory"



Linear (Left) And Multi-Level (Right) Page Tables

MULTI-LEVEL PAGE TABLES - 2

- Add level of indirection, the "page directory"



Two level page table:
2^{20} pages addressed with
two level-indexing
(page directory index, page table index)

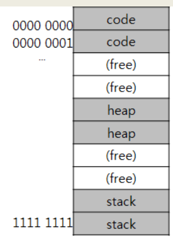
Linear (Left) And Multi-Level (Right) Page Tables

MULTI-LEVEL PAGE TABLES - 3

- Advantages
  - Only allocates page table space in proportion to the address space actually used
  - Can easily grab next free page to expand page table
- Disadvantages
  - Multi-level page tables are an example of a time-space tradeoff
  - Sacrifice address translation time (now 2-level) for space
  - Complexity: multi-level schemes are more complex

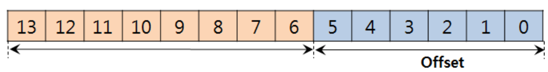
EXAMPLE

- 16KB address space, 64byte pages
- How large would a one-level page table need to be?
- 2^{14} (address space) / 2^{6} (page size) = 2^{8} = 256 (pages)



Flag	Detail
Address space	16 KB
Page size	64 byte
Virtual address	14 bit
VPN	8 bit
Offset	6 bit
Page table entry	2^8(256)

A 16-KB Address Space With 64-byte Pages



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EXAMPLE - 2

- 256 total page table entries (64 bytes each)
- 1,024 bytes page table size, stored using 64-byte pages = (1024/64) = 16 page directory entries (PDEs)
- Each page directory entry (PDE) can hold 16 page table entries (PTEs) *e.g. lookups*
- 16 page directory entries (PDE) x 16 page table entries (PTE) = 256 total PTEs
- **Key idea: the page table is stored using pages too!**

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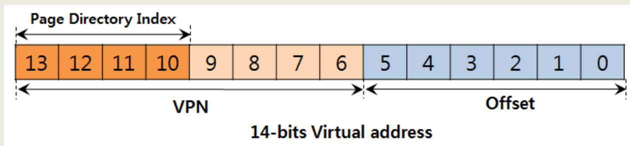
PAGE DIRECTORY INDEX

- Now, let's split the page table into two:
  - 8 bit VPN to map 256 pages
  - 4 bits for page directory index (PDI – 1st level page table)
  - 6 bits offset into 64-byte page



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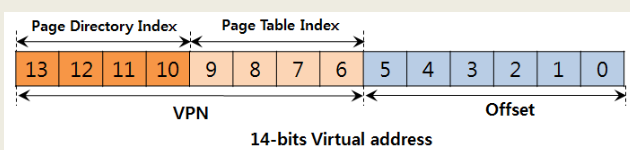
PAGE TABLE INDEX

- 4 bits page directory index (PDI – 1st level)
- 4 bits page table index (PTI – 2nd level)



- To dereference one 64-byte memory page,
  - We need one page directory entry (PDE)
  - One page table Index (PTI) – can address 16 pages

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EXAMPLE - 3

- **For this example, how much space is required to store as a *single-level* page table with any number of PTEs?**
- 16KB address space, 64 byte pages
- 256 page frames, 4 byte page size
- 1,024 bytes required (*single level*)
- **How much space is required for a *two-level* page table with only 4 page table entries (PTEs) ?**
- Page directory = 16 entries x 4 bytes (1 x 64 byte page)
- Page table = 4 entries x 4 bytes (1 x 64 byte page)
- 128 bytes required (2 x 64 byte pages)
  - Savings = using just 12.5% the space !!!

32-BIT EXAMPLE

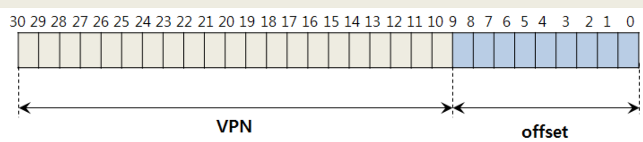
- Consider: 32-bit address space, 4KB pages, 2^{20} pages
- Only 4 mapped pages
- **Single level**: 4 MB (we've done this before)
- **Two level**: (old VPN was 20 bits, split in half)
- Page directory = 2^{10} entries x 4 bytes = 1 x 4 KB page
- Page table = 4 entries x 4 bytes (mapped to 1 4KB page)
- 8KB (8,192 bytes) required
- Savings = using just .78 % the space !!!
- 100 sparse processes now require < 1MB for page tables

OBJECTIVES – 12/2

- Questions from 11/30
- Assignment 2 - Dec 3
- Quiz 3 – Synchronized Array - Dec 2
- Tutorial 2 – Pthread, locks, conditions tutorial - Nov 30
- Assignment 3 (as a Tutorial) - Dec 17
- Quiz 4 - Page Tables - Dec 13
- Chapter 18: Introduction to Paging
- Chapter 19: Translation Lookaside Buffer (TLB)
  - TLB Algorithm, Hit-to-Miss Ratios
- Chapter 20: Paging: Smaller Tables
  - Smaller Tables, Multi-level Page Tables, **N-level Page Tables**

MORE THAN TWO LEVELS

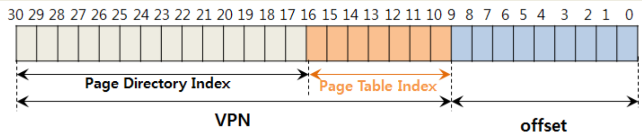
- Consider: page size is 2^9 = 512 bytes
- Page size 512 bytes / Page entry size 4 bytes
- VPN is 21 bits



Flag	Detail
Virtual address	30 bit
Page size	512 byte
VPN	21 bit
Offset	9 bit

MORE THAN TWO LEVELS - 2

- Page table entries per page = 512 / 4 = 128
- 7 bytes – for page table index (PTI)



Flag	Detail
Virtual address	30 bit
Page size	512 byte
VPN	21 bit
Offset	9 bit
Page entry per page	128 PTEs

→ $\log_2 128 = 7$

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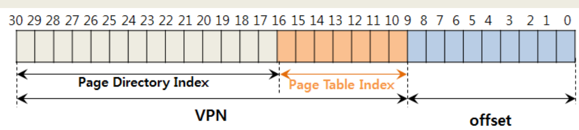
MORE THAN TWO LEVELS - 3

- To map 1 GB address space (2^{30}=1GB RAM, 512-byte pages)
- 2^{14} = 16,384 page directory entries (PDEs) are required
- When using 2^7 (128 entry) page tables…
- Page size = 512 bytes / 4 bytes per addr



Flag	Detail
Virtual address	30 bit
Page size	512 byte
VPN	21 bit
Offset	9 bit
Page entry per page	128 PTEs

→ $\log_2 128 = 7$

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MORE THAN TWO LEVELS - 3

- To map 1 GB address space (2^{30}=1GB RAM, 512-byte pages)
- 2^{14} = 16,384 page directory entries (PDEs) are required
- When using 2^7 (128 entry) page tables…
- Page size = 512 bytes / 4 bytes per addr

Can't Store Page Directory with 16K pages, using 512 bytes pages. Pages only dereference 128 addresses (512 bytes / 32 bytes)

Virtual address	30 bit
Page size	512 byte
VPN	21 bit
Offset	9 bit
Page entry per page	128 PTEs

→ $\log_2 128 = 7$

MORE THAN TWO LEVELS - 3

- To map 1 GB address space (2^{30}=1GB RAM, 512-byte pages)
- 2^{14} = 16,384 page directory entries (PDEs) are required
- When using 2^7 (128 entry) page tables…
- Page size = 512 bytes / 4 bytes per addr

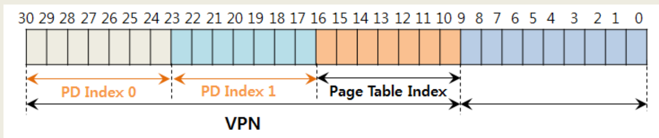
**Need three level page table:
Page directory 0 (PD Index 0)
Page directory 1 (PD Index 1)
Page Table Index**

Virtual address	30 bit
Page size	512 byte
VPN	21 bit
Offset	9 bit
Page entry per page	128 PTEs

→ $\log_2 128 = 7$

MORE THAN TWO LEVELS - 4

- We can now address 1GB with"fine grained" 512 byte pages
- Using multiple levels of indirection



- Consider the implications for address translation!
- How much space is required for a virtual address space with 4 entries on a 512-byte page? (let's say 4 32-bit integers)
- PD0 1 page, PD1 1 page, PT 1 page = 1,536 bytes
- Memory Usage= 1,536 (*3-level*) / 8,388,608 (*1-level*) = .0183% !!!

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ADDRESS TRANSLATION CODE

```
// 5-level Linux page table address lookup
//
// Inputs:
// mm_struct – process's memory map struct
// vpage – virtual page address

// Define page struct pointers
pgd_t *pgd;
p4d_t *p4d;
pud_t *pud;
pmd_t *pmt;
pte_t *pte;
struct page *page;
```


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ADDRESS TRANSLATION - 2

```
pgd = pgd_offset(mm, vpage);
if (pgd_none(*pgd) || pgd_bad(*pgd))
    return 0;
p4d = p4d_offset(pgd, vpage);
if (p4d_none(*p4d) || p4d_bad(*p4d))
    return 0;
pud = pud_offset(p4d, vpage);
if (pud_none(*pud) || pud_bad(*pud))
    return 0;
pmd = pmd_offset(pud, vpage);
if (pmd_none(*pmd) || pmd_bad(*pmd))
    return 0;
if (!(pte = pte_offset_map(pmd, vpage)))
    return 0;
if (!(page = pte_page(*pte)))
    return 0;
physical_page_addr = page_to_phys(page);
pte_unmap(pte);
return physical_page_addr;  // param to send back
```

pgd_offset():
Takes a vpage address and the mm_struct for the process, returns the PGD entry that covers the requested address...

p4d/pud/pmd_offset():
Takes a vpage address and the pgd/p4d/pud entry and returns the relevant p4d/pud/pmd.

pte_unmap()
release temporary kernel mapping for the page table entry

INVERTED PAGE TABLES

- Keep a single page table for each physical page of memory
- Consider 4GB physical memory
- Using 4KB pages, page table requires 4MB to map all of RAM
- Page table stores
  - Which process uses each page
  - Which process virtual page (from process virtual address space) maps to the physical page
- All processes share the same page table for memory mapping, kernel must isolate all use of the shared structure
- Finding process memory pages requires search of 2^{20} pages
- Hash table: can index memory and speed lookups

MULTI-LEVEL PAGE TABLE EXAMPLE

- Consider a 16 MB computer which indexes memory using 4KB pages
- (#1) For a single level page table, how many pages are required to index memory?
- (#2) How many bits are required for the VPN?
- (#3) Assuming each page table entry (PTE) can index any byte on a 4KB page, how many offset bits are required?
- (#4) Assuming there are 8 status bits, how many bytes are required for each page table entry?

MULTI LEVEL PAGE TABLE EXAMPLE - 2

- (#5) How many bytes (or KB) are required for a single level page table?
- Let's assume a simple HelloWorld.c program.
- HelloWorld.c requires virtual address translation for 4 pages:
  - 1 – code page | 1 – stack page
  - 1 – heap page | 1 – data segment page
- (#6) Assuming a two-level page table scheme, how many bits are required for the Page Directory Index (PDI)?
- (#7) How many bits are required for the Page Table Index (PTI)?

MULTI LEVEL PAGE TABLE EXAMPLE - 3

- Assume each page directory entry (PDE) and page table entry (PTE) requires 4 bytes:
  - 6 bits for the Page Directory Index (PDI)
  - 6 bits for the Page Table Index (PTI)
  - 12 offset bits
  - 8 status bits
- (#8) How much **total** memory is required to index the HelloWorld.c program using a two-level page table when we only need to translate 4 total pages?
- HINT: we need to allocate one Page Directory and one Page Table…
- HINT: how many entries are in the PD and PT

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MULTI LEVEL PAGE TABLE EXAMPLE - 4

- (#9) Using a single page directory entry (PDE) pointing to a single page table (PT), if all of the slots of the page table (PT) are in use, what is the total amount of memory a two-level page table scheme can address?
- (#10) And finally, for this example, as a percentage (%), how much memory does the 2-level page table scheme consume compared to the 1-level scheme?
- HINT: two-level memory use / one-level memory use

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ANSWERS

- #1 – 4096 pages
- #2 – 12 bits
- #3 – 12 bits
- #4 – 4 bytes
- #5 – 4096 x 4 = 16,384 bytes (16KB)
- #6 – 6 bits
- #7 – 6 bits
- #8 – 256 bytes for Page Directory (PD) (64 entries x 4 bytes)
  256 bytes for Page Table (PT) **TOTAL = 512 bytes**
- #9 – 64 entries, where each entry maps a 4,096 byte page
  With 12 offset bits, can address 262,144 bytes (256 KB)
- #10- 512/16384 = .03125 → 3.125%

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QUESTIONS

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