Detecting Network Effects Randomizing Over Randomized Experiments

Martin Saveski (@msaveski)_

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Martin Saveski MIT



Jean Pouget-Abadie Harvard



Guillaume Saint-Jacques MIT



Weitao Duan LinkedIn



Souvik Ghosh LinkedIn



Ya Xu LinkedIn



Edo Airoldi Harvard

Treatment

$$Z_i = 1$$

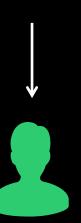
New Feed Ranking Algorithm

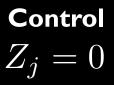


Treatment

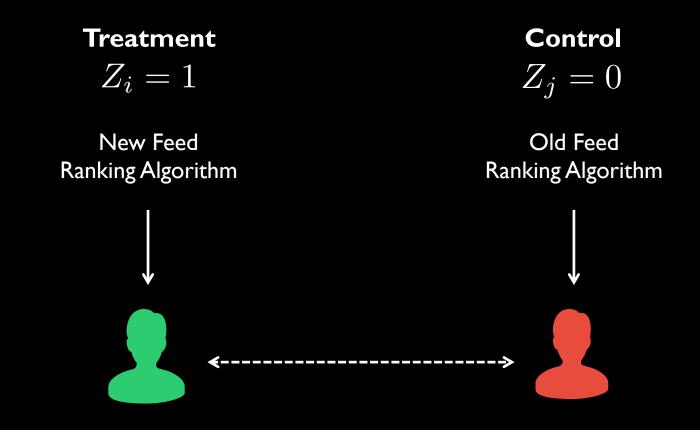
 $Z_i = 1$

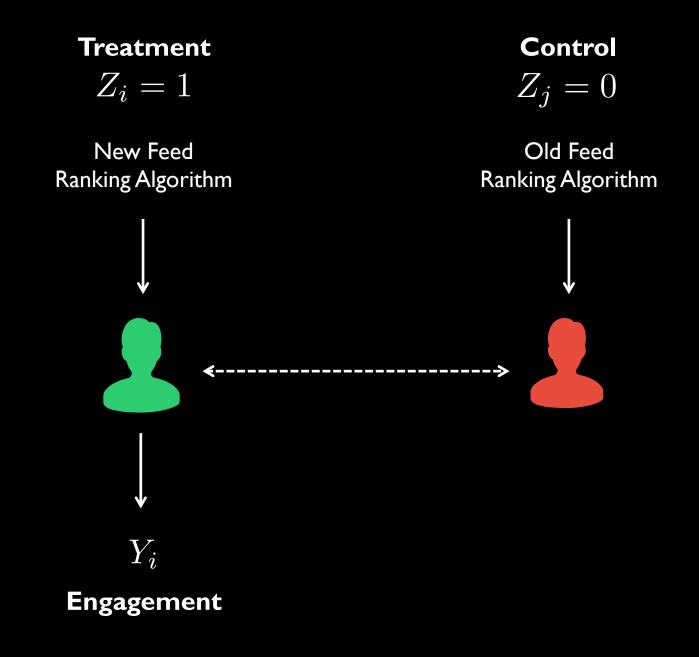
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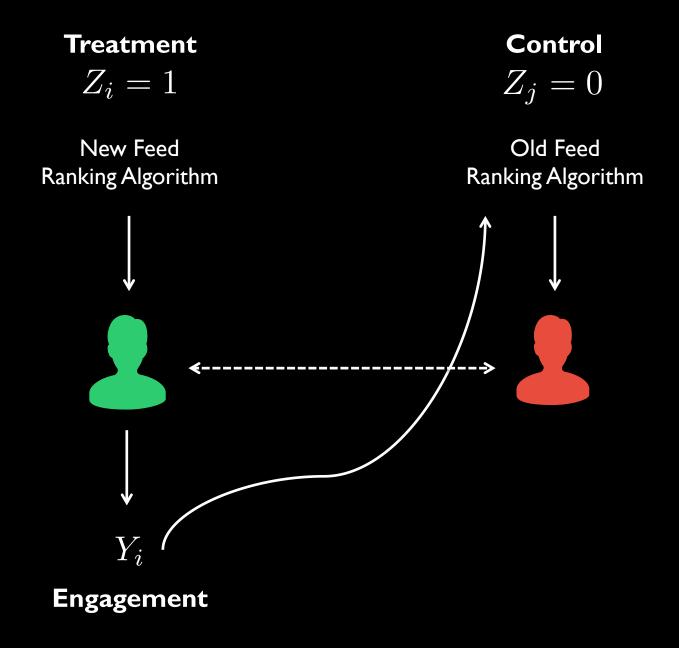


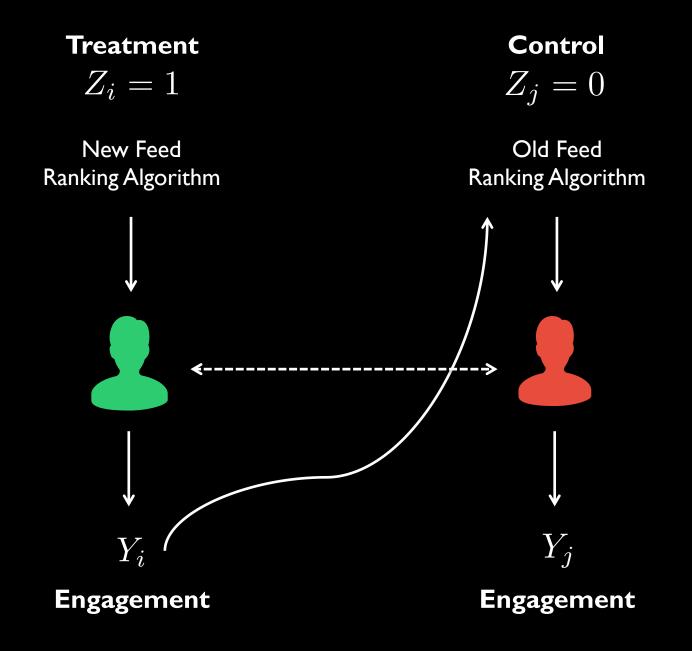


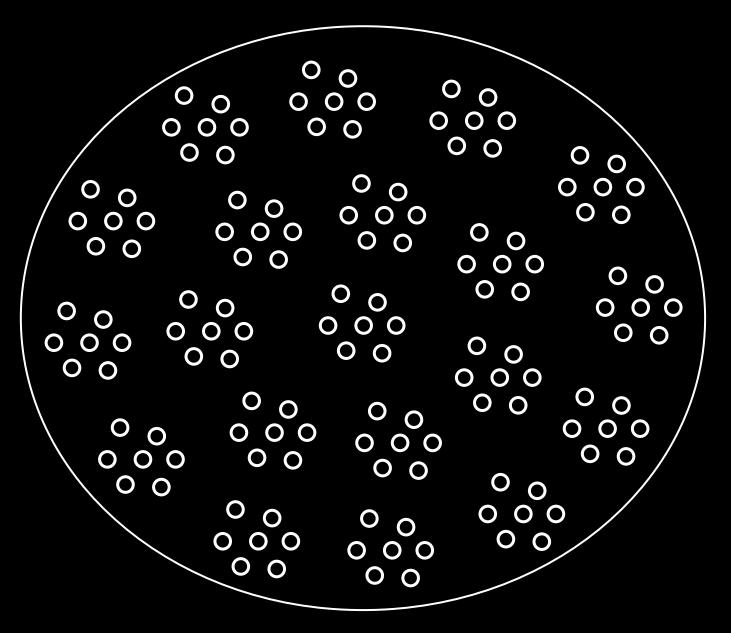
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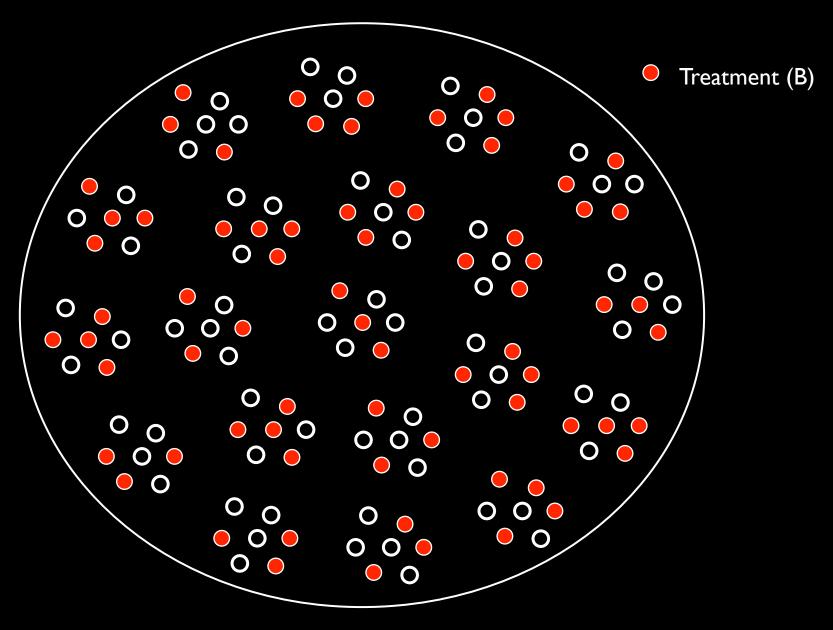


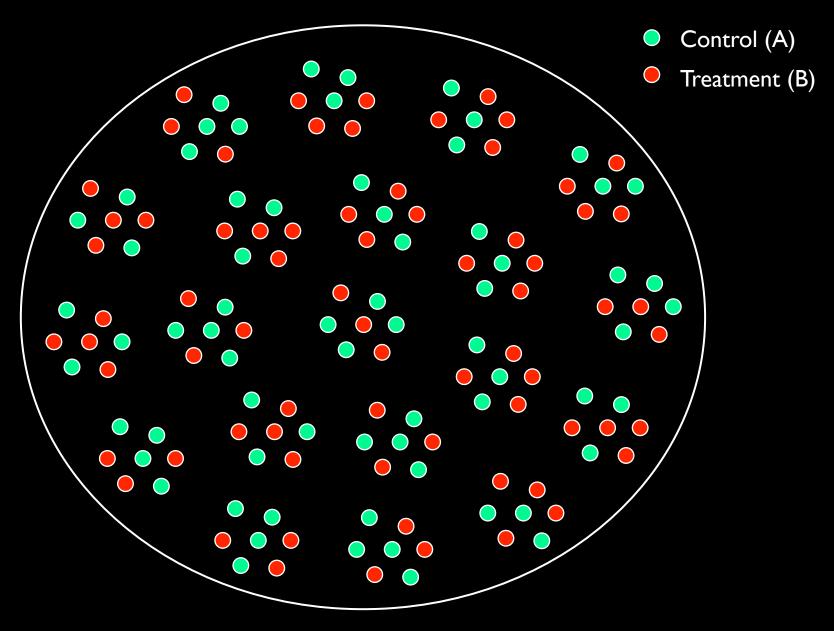


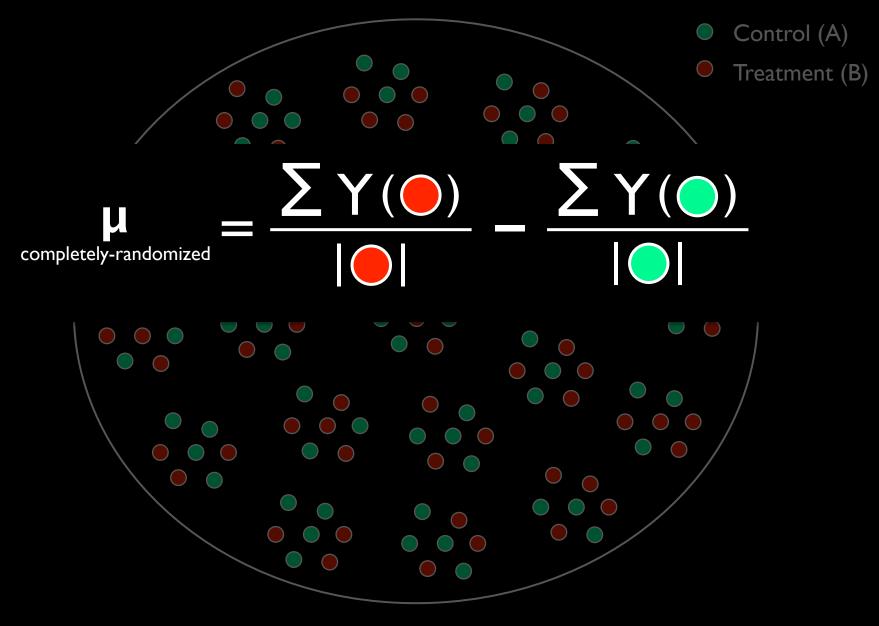


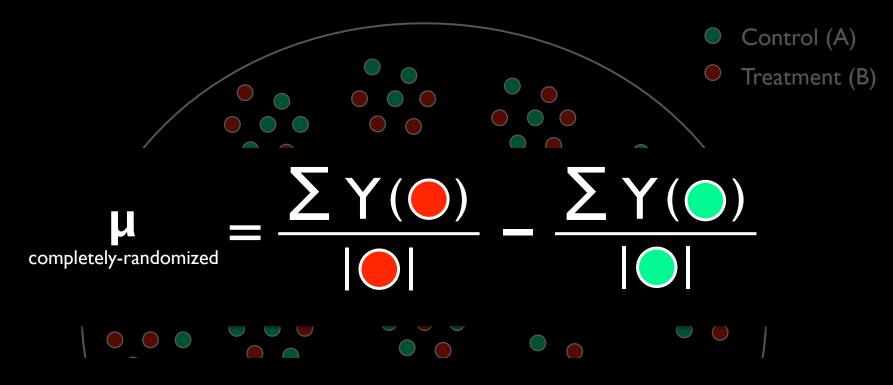








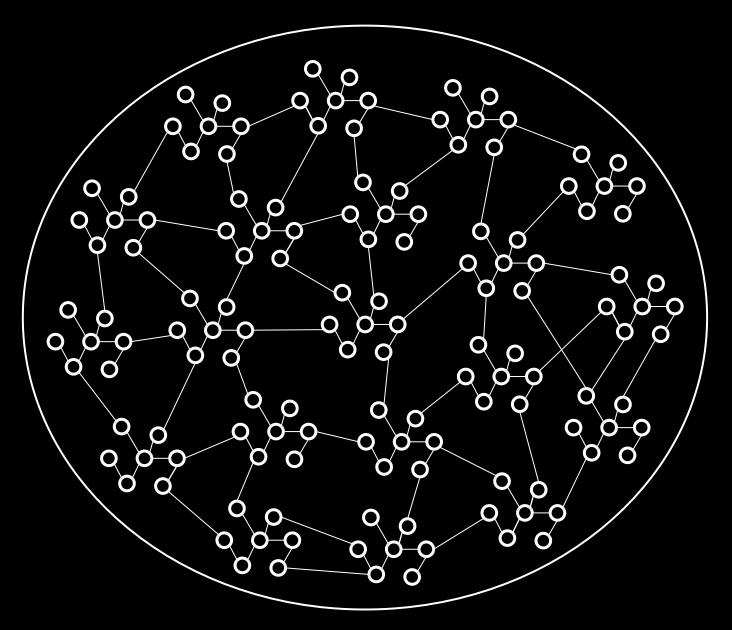




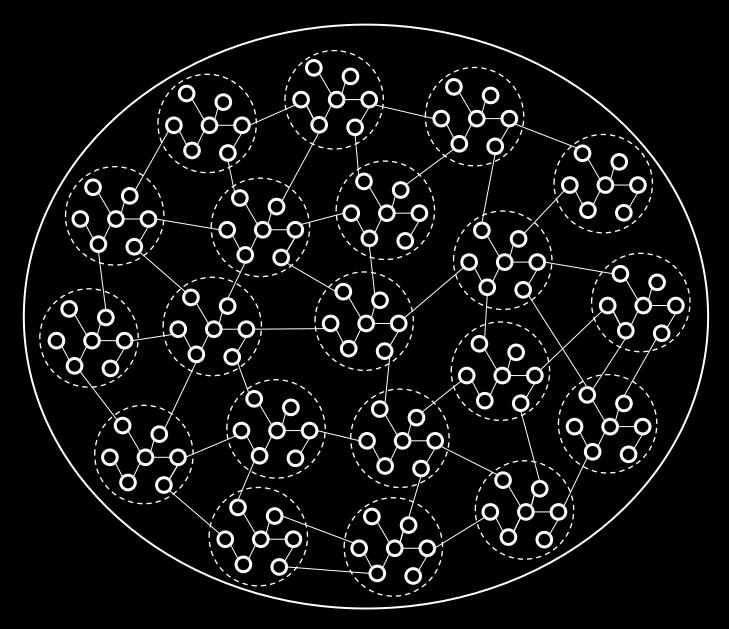
SUTVA: Stable Unit Treatment Value Assumption

Every user's behavior is affected only by their treatment and NOT by the treatment of any other user

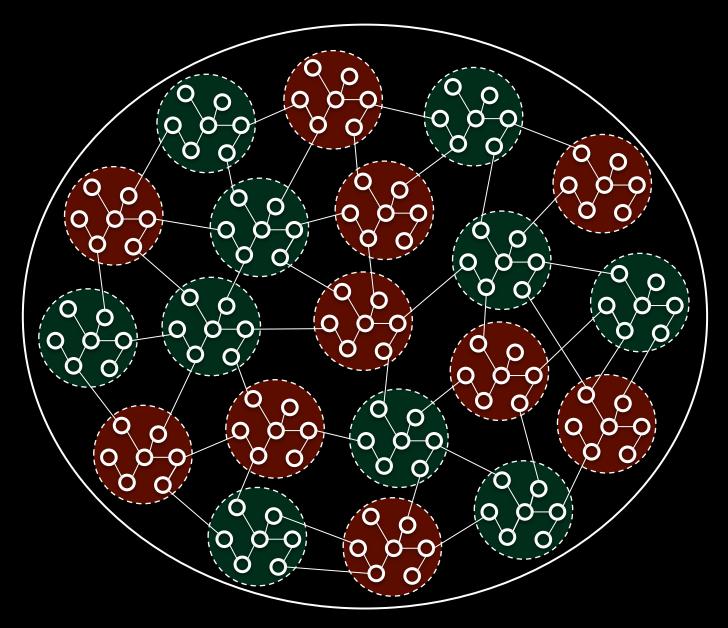


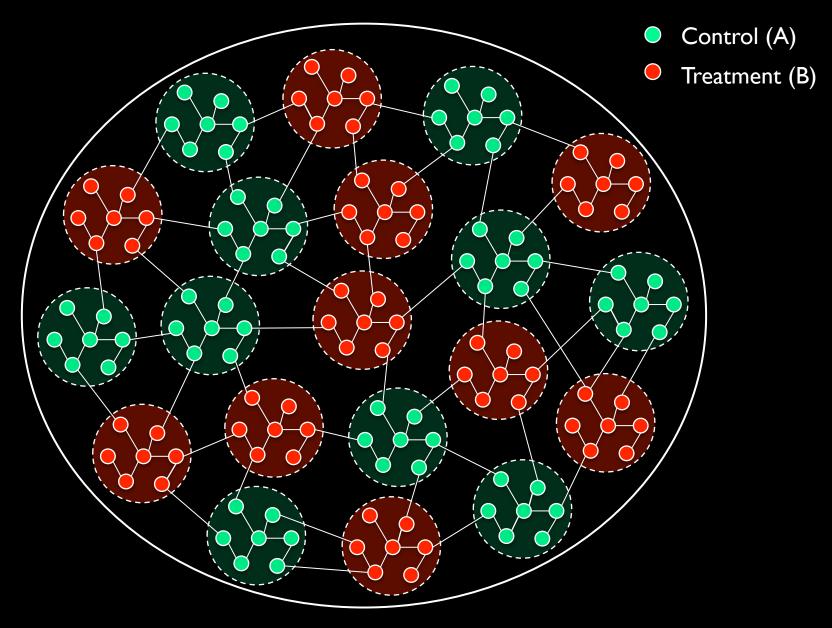


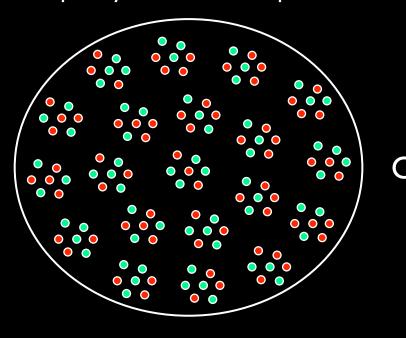
Cluster-based Randomized Experiment

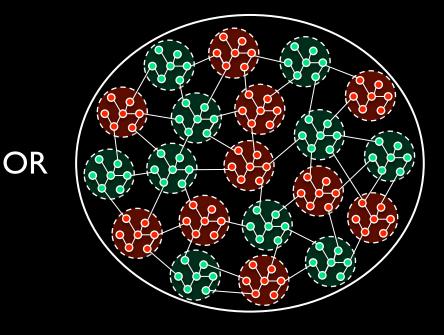


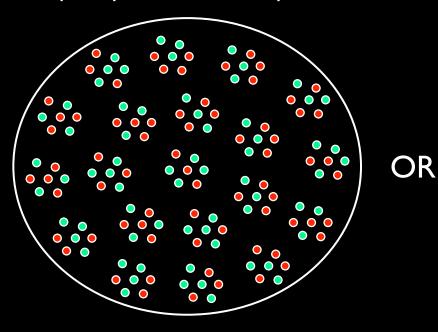
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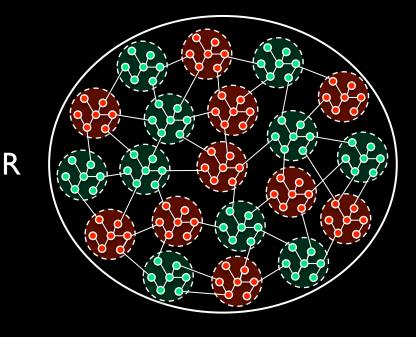








Cluster-based Randomized Experiment

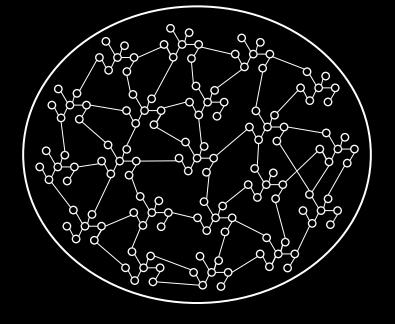


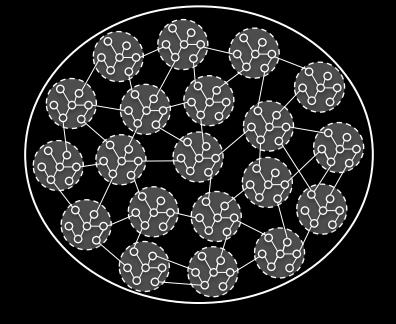
More Spillovers

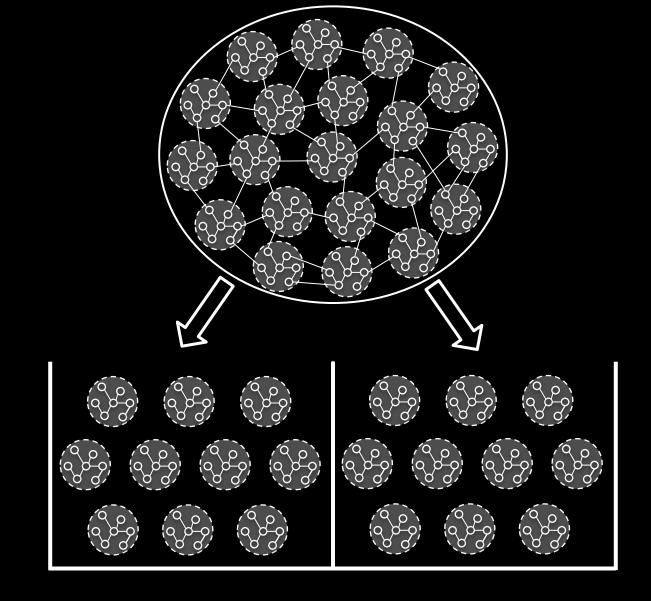
Lower Variance

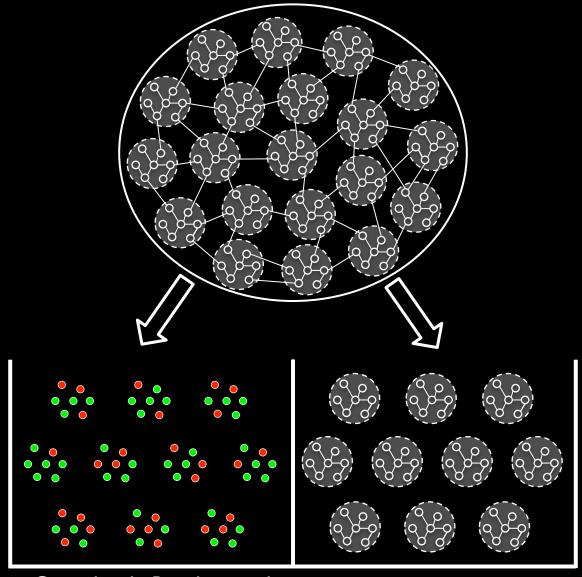
Less Spillovers Higher Variance

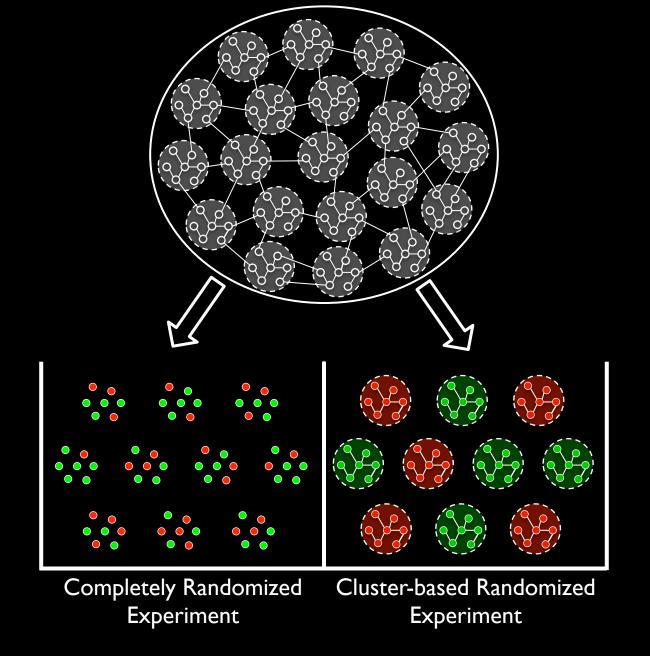
Design for Detecting Network Effects

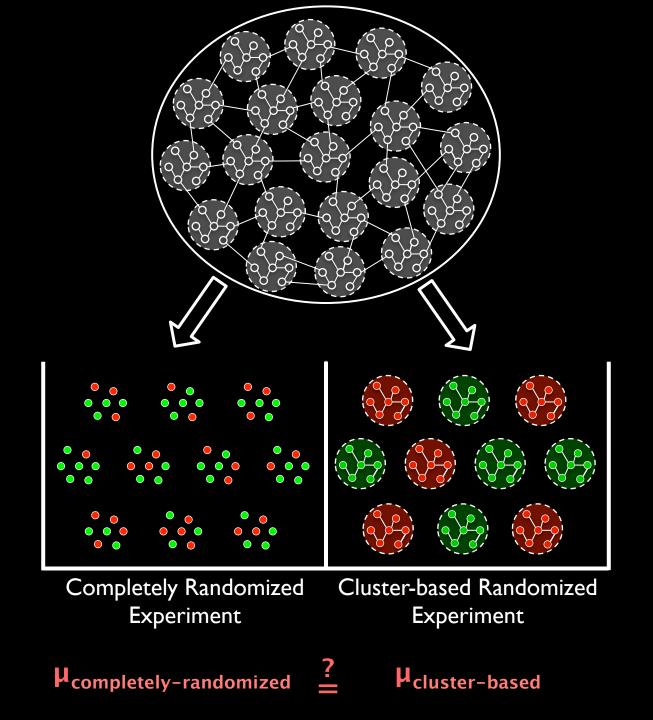












H₀: SUTVA Holds

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 $\overline{E_{\mathbf{W},\mathbf{Z}}\left[\hat{\mu}_{cbr}-\hat{\mu}_{cr}\right]}=0$

H₀: SUTVA Holds

 $E_{\mathbf{W},\mathbf{Z}}\left[\hat{\mu}_{cbr} - \hat{\mu}_{cr}\right] = 0$ $\operatorname{var}_{\mathbf{W},\mathbf{Z}}\left[\hat{\mu}_{cr} - \hat{\mu}_{cbr}\right] \leq E_{\mathbf{W},\mathbf{Z}}\left[\hat{\sigma}^{2}\right]$

H₀: SUTVA Holds

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Reject the null when:

H₀: SUTVA Holds

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$$\operatorname{var}_{\mathbf{W},\mathbf{Z}} \left[\hat{\mu}_{cr} - \hat{\mu}_{cbr} \right] \leq E_{\mathbf{W},\mathbf{Z}} \left[\hat{\sigma}^2 \right]$$

Reject the null when:

$$\left|\frac{|\hat{\mu}_{cr} - \hat{\mu}_{cbr}|}{\sqrt{\hat{\sigma}^2}} \geq \frac{1}{\sqrt{\alpha}}\right|$$

H_0 : SUTVA Holds

$$E_{\mathbf{W},\mathbf{Z}} \left[\hat{\mu}_{cbr} - \hat{\mu}_{cr} \right] = 0$$
$$\operatorname{var}_{\mathbf{W},\mathbf{Z}} \left[\hat{\mu}_{cr} - \hat{\mu}_{cbr} \right] \leq E_{\mathbf{W},\mathbf{Z}} \left[\hat{\sigma}^2 \right]$$

Reject the null when:

$$\frac{|\hat{\mu}_{cr} - \hat{\mu}_{cbr}|}{\sqrt{\hat{\sigma}^2}} \geq \frac{1}{\sqrt{\alpha}}$$

Type I error is no greater than $\, \alpha \,$

Nuts and Bolts of Running Cluster-based Randomized Experiments

Why Balanced Clustering?

- Theoretical Motivation
 - Constants VS random variables

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- Practical Motivations

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 - Variance reduction

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 - Balance on pre-treatment covariates (homophily => large homogenous clusters)

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=> Algorithms that enforce equal cluster sizes

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Restreaming Linear Deterministic Greedy (Nishimura & Ugander, 2013)

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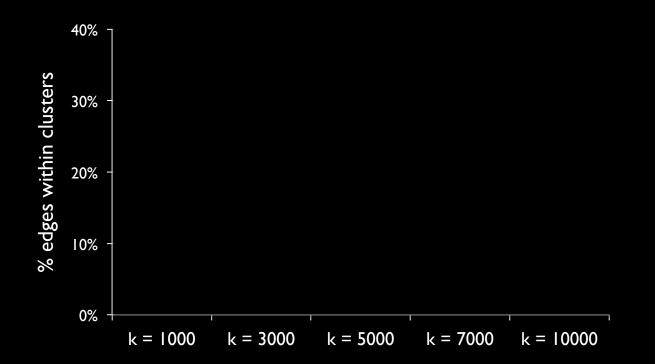
Restreaming Linear Deterministic Greedy

(Nishimura & Ugander, 2013)

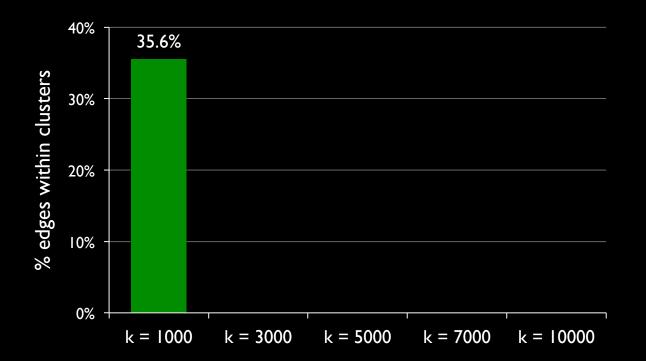
- Streaming
- Parallelizable
- Stable

- Graph: >100M nodes, >10B edges
- 350 Hadoop nodes
- I% leniency

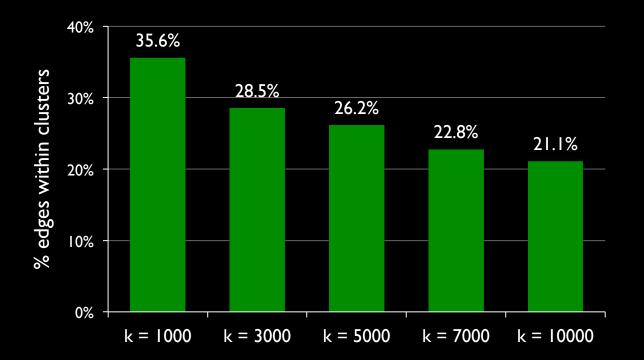
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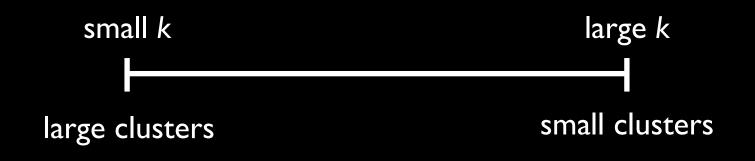
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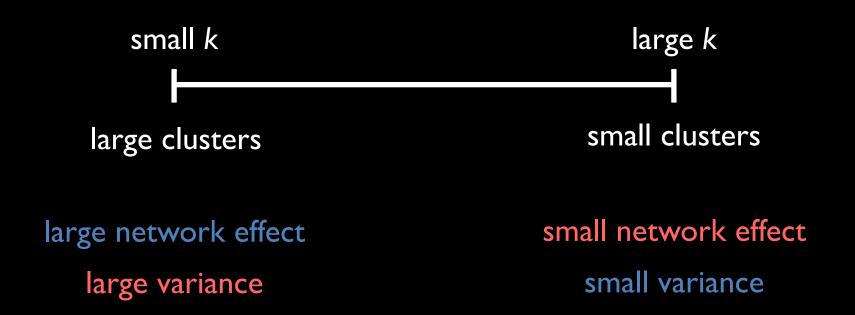


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 $Y_i = \beta_0 + \beta_1 Z_i + \beta_2 \rho_i + \epsilon_i$

 ho_i : fraction of treated friends

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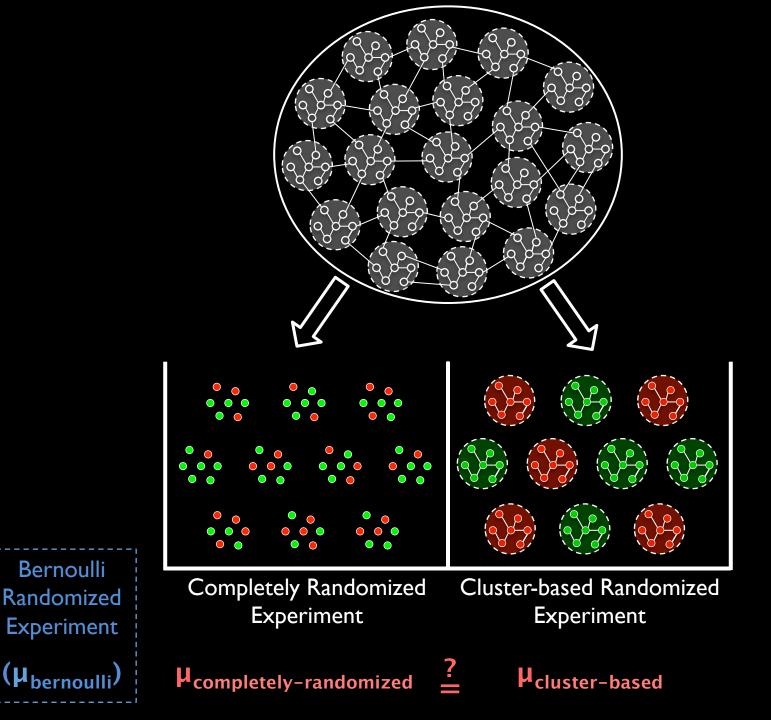
$$E\left[\hat{\mu}_{cbr} - \hat{\mu}_{cr}\right] \approx \rho \cdot \beta_2$$

ho : average fraction of a unit's neighbors contained in the cluster

Choose number of clusters M and clustering C such that

$$\max_{M,C} \frac{\rho}{\sqrt{\hat{\sigma}_C^2}}$$

Experiments on LinkedIn



- Population: 20% of all LinkedIn users [Bernoulli: 10%, Cluster-based: 10%]

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Treatment effect Standard Deviation

Bernoulli Randomization (BR)

Cluster-based Randomization (CBR)

Delta (CBR – BR)

- Population: 20% of all LinkedIn users [Bernoulli: 10%, Cluster-based: 10%]
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	Treatment effect	Standard Deviation
Bernoulli Randomization (BR)	0.0559	0.0050
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Cluster-based Randomization (CBR)	0.0771	0.0260
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p-value: 0.4246

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Cluster-based Randomization (CBR)		
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	Treatment effect	Standard Deviation
Bernoulli Randomization (BR)	0.2108	0.2911
Cluster-based Randomization (CBR)	0.5390	0.5613
Delta (CBR – BR)		

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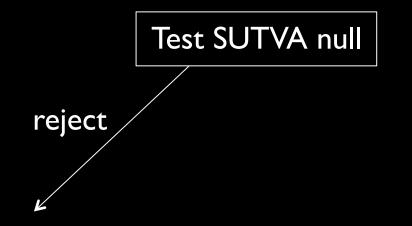
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Bernoulli Randomization (BR)	0.2108	0.2911
Cluster-based Randomization (CBR)	0.5390	0.5613
Delta (CBR – BR)	-0.3281	0.5712

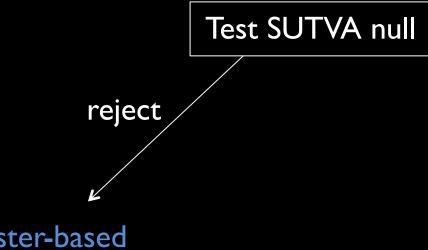
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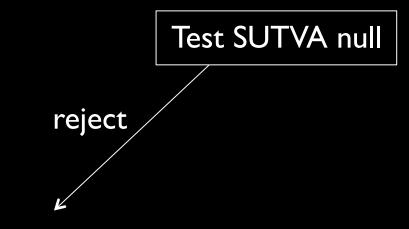
p-value: 0.0483

Test SUTVA null



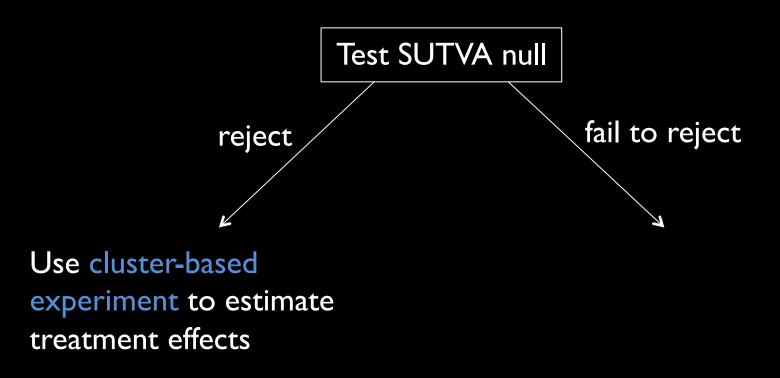


Use cluster-based experiment to estimate treatment effects

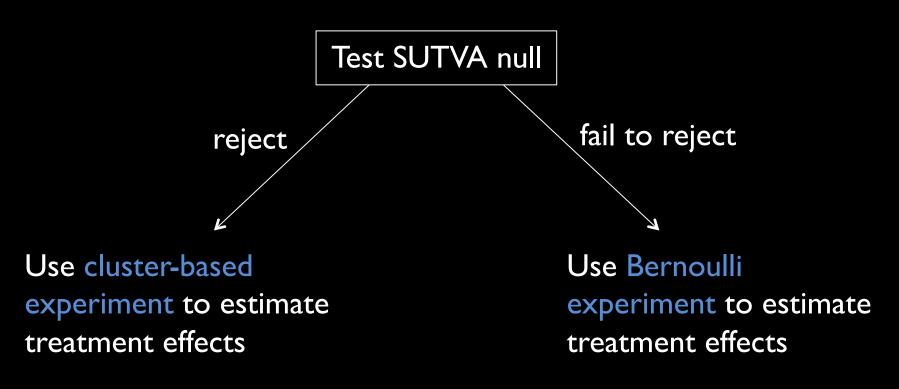


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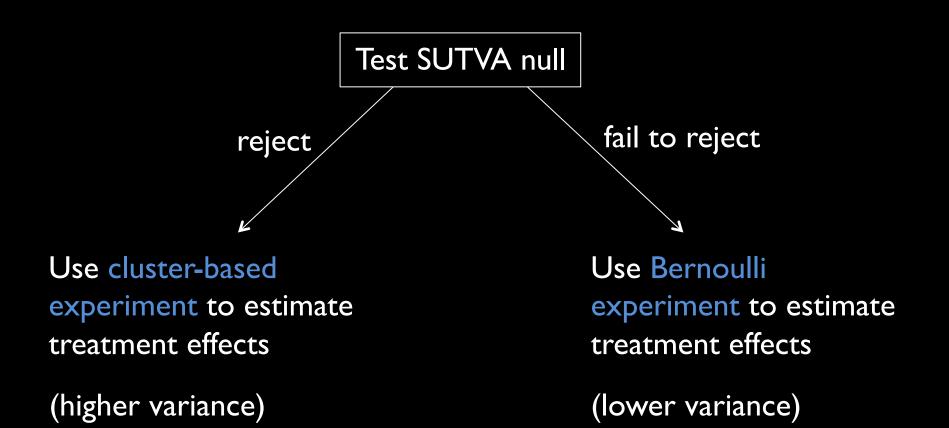
(higher variance)



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Papers available online

KDD'17 Arxiv

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