Demonstration of augmenting paths. Let us start with a graph of order 22.


We now select a matching M. It has 6 edges.


The red edges are the matching. The edges in the matching are: $\{1,15\},\{3,10\},\{4,5\},\{2,16\},\{13,20\}$, $\{14,22\}$.

We now find a bigger matching, it has 7 edges: $\{4,9\},\{3,10\},\{2,11\},\{1,15\},\{16,20\},\{17,22\},\{5,19\}$


Note that some of the edges, like $\{1,15\}$ and $\{3,10\}$ overlap. The augmenting path will be produced by the red and green edges, so we will isolate them:

21

18

| 6 |  | 1 |
| :--- | :--- | :--- |
|  | 7 | 8 |$|$




The augmenting path is: 19-5-4-9 And the matching $M$ will be augmented to the matching: $\{3,10\}\{1,15\}\{2,16\},\{13,20\},\{5,19\}\{4,9\},\{14,22\}$

