

# Assignment 6

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**Course Number:** MKTG 584 B

**Course Name:** Dynamic Structural Models

## 1 Overview

This assignment follows Assignment 5 in also allowing for bus-specific persistent unobservables. Here, you will implement the Arcidiacono & Miller algorithm, which involves an EM loop over the two-step CCP method (that you used in Assignment 3).

## 2 Assumptions

- Assume the deterministic mileage transition process and utility specification from Assignment 4.
- In your code, you don't need to infer the state transition. Just assume it to be known.
- Assume there are two unobserved types of buses.

## 3 Inputs

Your code should take the following inputs:

- Data in following format (in columns) – BusNo., Timeperiod, DecisionNo. (0 if the line refers to continuation, 1 if it refers to replacement), Mileage, Chosen (0 if this line was chosen, 1 otherwise).
- Discount factor  $\beta$

## 4 Outputs

For a given dataset and discount factor, the code should generate the following outputs:

- Parameters  $\{\theta_1, \theta_2, \theta_3, \pi\}$  and the standard errors for each of them.
- Because this is a two-step method, you need to use bootstrap to obtain the standard errors for all the parameters.

## 5 Some suggestions

- Follow the same suggestions regarding optimizers and speeding the algorithm from Assignment 5.
- Use the same dataset provided with Assignment 5 for estimating the parameters for your report as well.

## 6 Evaluation

In your submission, include the following:

1. Your code with detailed comments. I will evaluate the correctness of your code using the same dataset as that provided for Assignment 5. Your code should produce the correct parameters for the data.
2. A pdf document with the following results:
  - (a) Run your model on the dataset (provided with Assignment 5) and present the following
    - a) the parameter estimates and standard errors without bootstrap (run on the full data),
    - and b) the bootstrapped parameter estimates and standard errors with at least 250 replications.
  - (b) The probability distribution of parameters from the bootstrap process.
  - (c) Without bootstrap, specify the time it takes to run and the number of iterations for the EM algorithm to converge, along with the convergence criterion.
  - (d) Compare the estimates, standard errors, and run-times from Assignment 5 and this one. What are the main differences? For simplicity, use the non-bootstrapped estimates
  - (e) Run a simple two-step estimator (as you did in Assignment 3) and report the bias in parameters from ignoring persistent unobservables. It is sufficient to compare the non-bootstrapped parameter estimates from Assignment 3 and Assignment 6 (since the estimates are consistent, though inefficient).
  - (f) Report the differences in runtime (for non-bootstrapped estimation) for the two-step method and two-step method with EM.