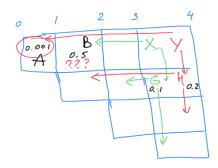
Section

Dynamic programming

Introduction to Computational Linguistics Section

Olga Zamaraeva
University of Washington
May 22, 2020

- "Greedy" algorithms pick the highest score at every step
 - e.g. highest probability edge
- Not all greedy algorithms always return the correct result
- ► Why?
- Does CKY always return a correct result? Why?



Grammar:

$$P(X) \rightarrow BG = P(Y) \rightarrow AH$$

$$P(B) \gg P(A) \quad \text{if possible ??}$$

$$P(G) < P(H)$$

Grammar	Lexicon
$S \rightarrow NP VP$	Det ightarrow that this the a
$S \rightarrow Aux NP VP$	$Noun ightarrow book \mid \mathit{flight} \mid \mathit{meal} \mid \mathit{money}$
$S \rightarrow VP$	$Verb ightarrow book \mid include \mid prefer$
$NP \rightarrow Pronoun$	$Pronoun ightarrow I \mid she \mid me$
$NP \rightarrow Proper-Noun$	$Proper-Noun ightarrow Houston \mid NWA$
NP o Det Nominal	$Aux \rightarrow does$
$Nominal \rightarrow Noun$	$Preposition \rightarrow from \mid to \mid on \mid near \mid through$
$Nominal \rightarrow Nominal Noun$	
$Nominal \rightarrow Nominal PP$	
VP o Verb	
$VP \rightarrow Verb NP$	
$VP \rightarrow Verb NP PP$	
$VP \rightarrow Verb PP$	
$VP \rightarrow VP PP$	
$PP \rightarrow Preposition NP$	

Figure 12.1 The \mathcal{L}_1 miniature English grammar and lexicon.

LING472

Dunamia

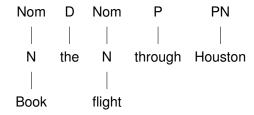
Book the flight through Houston

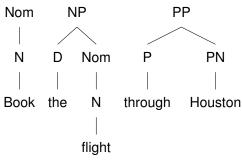
LING472

Section

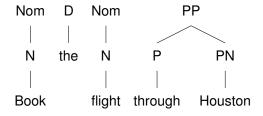
Dynamic programming

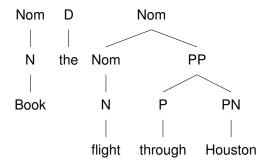
LING472





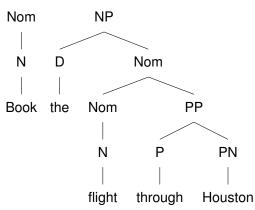
No more possibilities! Backtrack...





LING472

Dynamic programming



No more possibilities! Backtrack... Up to where?..

LING472

Dynamic programming

Backtrack to the very beginning, actually!

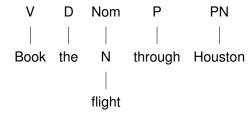
Book the flight through Houston

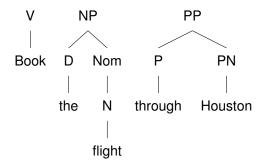
LING472

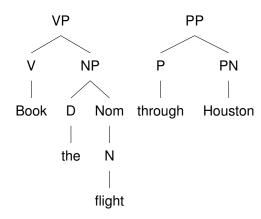
Section

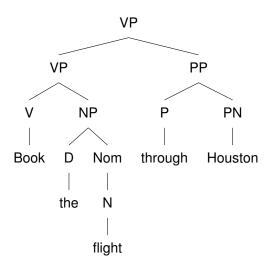
Dynamic programming

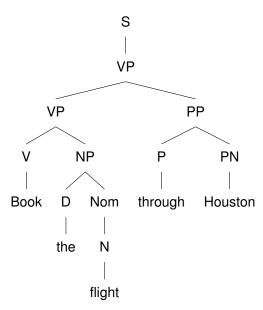
Dvnamic



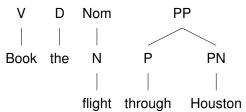


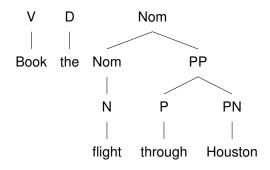


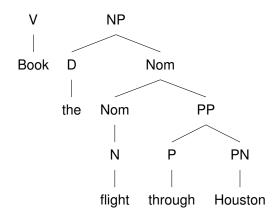


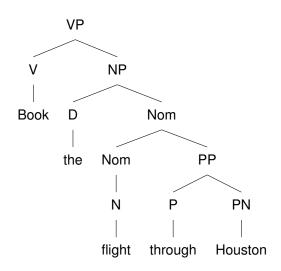


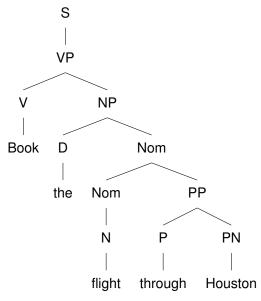
Or, we could have instead done:











How do we make sure we get both trees?

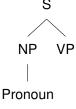
LING472

Dynamic programming

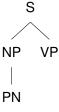
Go through all possibilities for productions

5

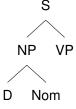






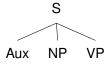




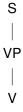




|

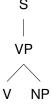


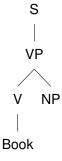
S | VP

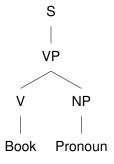


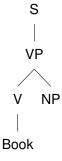


Yes, but we have more input still...

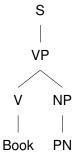




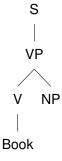


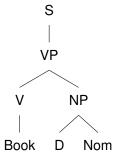


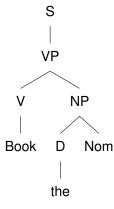
Section

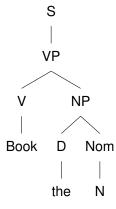


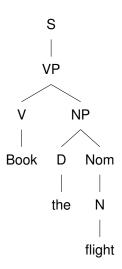
Sectio





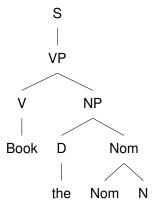


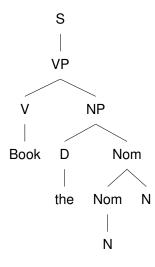




Yes, but we have more input still...



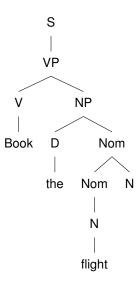




Top-Down Parsing

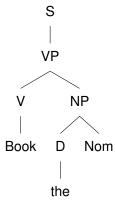
Section

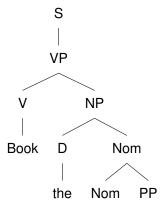
Dynamic programming

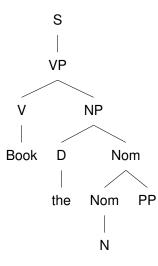


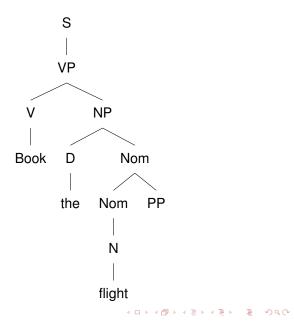
Nope... Backtrack again...

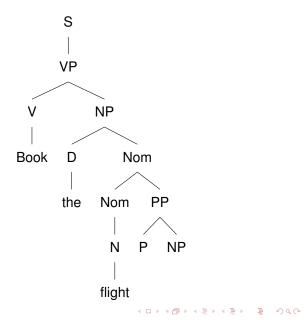


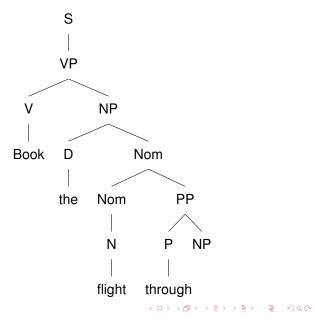


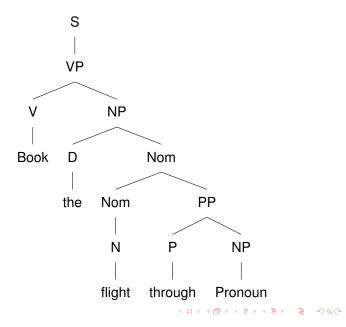


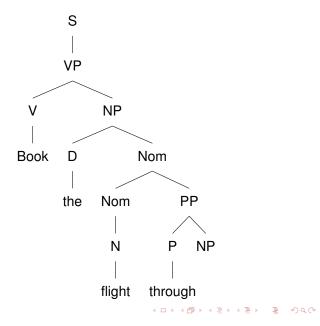


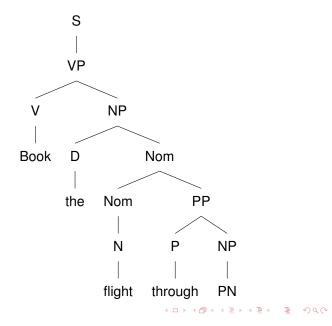


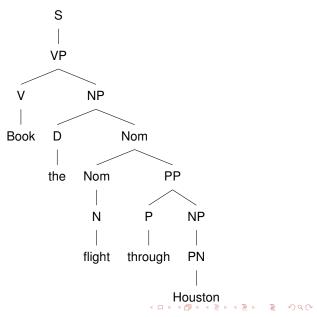












Top-Down Parsing

Dynamic

Could we have gotten the second tree by top-down parsing?

- Could we have gotten the second tree by top-down parsing?
 - Yes; it is a matter of which rule happened to be on the top of the stack
 - We grabbed VP → V NP
 - ▶ But the option VP → VP PP is also on the stack somewhere
 - Thus the returned parse is subject to an arbitrary listing of rules in the grammar

Dynamic

- Top-down parsers do not waste time exploring hypotheses not leading to S
 - ...but do waste time exploring hypotheses not matching the input
- Bottom-up parsers do not waste time exploring hypotheses not matching input
 - ...but do waste time exploring hypotheses not leading to S
- Both can take exponential time
 - (in the worst case, easier shown on abstract CFG)
 - Some recursive parsers are O(n⁴)
- An answer to poor time complexity: dynamic programming
 - $ightharpoonup O(n^3)$

Recursive definition:
$$f(0) = 0$$
; $f(1) = 1$ $f(n) = f(n-1) + f(n-2)$

0 1 1 2 3 5 8 13 21 34 55 89 144 233 377 610 987 1597 2584 4181 6765 10946 17711 28657...

$$f(100) = 218922995834555169026$$

Since we have a recursive definition, let's implement the Fibonacci numbers printer recursively!

```
def fibonacci(n):
    if n in [0,1]:
        return n
    return fibonacci(n-1) + fibonacci(n-2)
```

What's the problem with this?

```
def fibonacci(n):
    return fibonacci_helper(n,{})
def fibonacci_helper(n,memo):
    if n in [0,1]:
        return n
    if not n in memo:
        memo[n] = fibonacci_helper(n-1,memo)
            + fibonacci_helper(n-2,memo)
    return memo[n]
```

- Fill in a table with solutions to subproblems
- Then can just look up momentarily the precomputed solution
- ▶ No need to perform the same computation many times

- f(0) = 0
- f(1) = 1
- f(2) = f(1) + f(0)
 - ▶ what's f(1)?
 - ▶ what's f(0)?

- f(3) = f(2) + f(1)
 - f(2) = f(1) + f(0)
 - f(1) = 1
 - f(0) = 0

- f(4) = f(3) + f(2)
 - f(3) = f(2) + f(1)
 - f(2) = f(1) + f(0)
 - f(1) = 1
 - f(0) = 0

- f(5) = f(4) + f(3)
 - f(4) = f(3) + f(2)
 - f(3) = f(2) + f(1)
 - f(2) = f(1) + f(0)
 - f(1) = 1
 - f(0) = 0
- etc... (deep recursion; slow; do the same computation again and again)

$$f(0) = ?$$

0 1 2 3 4 5

$$f(0) = ?$$

Not in the table, so compute: f(0)=0 (or rather, return the base case)

$$f(1) = ?$$

Not in the table, so compute: f(1)=1 (or rather, return the base case)

$$f(2) = ?$$

Not in the table, so compute: f(2)=f(2-1) + f(2-2) = f(1) + f(0)

But both f(1) and f(0) are already in the table! No need to compute! Just look up!

$$f(3) = ?$$

Not in the table, so compute: f(3)=f(3-1) + f(3-2) = f(2) + f(1)

But both f(2) and f(1) are already in the table! No need to compute! Just look up!

$$f(4) = ?$$

Not in the table, so compute:
$$f(4)=f(4-1) + f(4-2) = f(3) + f(2)$$

But both f(3) and f(2) are already in the table! No need to compute! Just look up!

Dynamic programming for parsing

.ING472

Dynamic programming

Once the constituent has been discovered, store the information

Example: The CKY algorithm (Cocke-Kazami-Younger)