

## ABMS OF CULTURAL EVOLUTION

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## ABMS IN PHILOSOPHY

### Review:

- Two Platonic puzzles: Justice and Meaning
- Difference between ABMs and population models.
- Why ABMs might help with Plato's puzzles

## MODELS AND SIMULATIONS

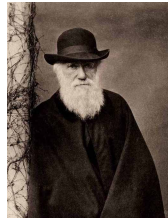
### Today:

- Population vs. ABMs models of cultural evolution
- Social networks
- Bounded Rationality

## OUTLINE

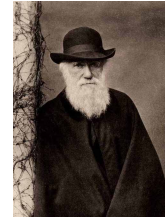
- 1 REVIEW AND MOTIVATION
- 2 POPULATION MODELS OF CULTURAL EVOLUTION
- 3 AGENT-BASED MODELS OF CULTURAL EVOLUTION
  - Explanatory Pattern
  - Components of ABMs of cultural evolution
    - Social Networks
    - Learning Rules and Bounded Rationality
- 4 NETLOGO
- 5 REFERENCES

## FROM PLATO TO DARWIN



- Plato's two puzzles: What are the origins of just behavior and linguistic meaning?
- A suggestive way of asking these questions: How did justice (respectively meaning) **evolve**?

## GAME THEORY IN BIOLOGY



Because we discussed how game theory might be useful in addressing Plato's puzzles, it might be helpful to discuss a common and fruitful analogy between

- Models of natural selection
- Rational Choice Theory (i.e. decision and game theory)

## DECISION THEORY IN BIOLOGY

**Question:** How are decision (and game theory) relevant for models of natural selection?

## DECISION THEORY IN BIOLOGY

### An Informal Argument:

- 1 Actions = Phenotypes (e.g., traits and behaviors)
- 2 Payoffs = Offspring
- 3 By definition, organisms that have the highest **actual** payoffs (offspring) will become more prevalent in the population.
- 4 So intuitively, actions (i.e. phenotypes) that have the highest **expected** payoffs (offspring) will become more prevalent.
  - The expected number of offspring of an organism with a given phenotype, given the current distribution of phenotypes in the population, is often called the **fitness** of the phenotype.

## DECISION THEORY IN BIOLOGY

**Conclusion:** Nature can be modeled as choosing organisms with particular phenotypes so as to maximize expected utility, where utility is the number of offspring.

*There exist deep and interesting connections, both thematic and formal, between evolutionary theory and the theory of rational choice . . . In rational choice theory, agents are assumed to make choices that maximize their utility, while in evolutionary theory, natural selection 'chooses' between alternative phenotypes, or genes, according to the criterion of fitness maximization. As a result, evolved organisms often exhibit behavioral choices that appear designed to maximize their fitness, which suggests the principles of rational choice might be applicable to them.*

Okasha and Binmore [2012].

## DECISION THEORY IN BIOLOGY

**Moral:** Rational choice theory can be useful in helping us understand evolution.

What about the reverse?

## CULTURAL EVOLUTION

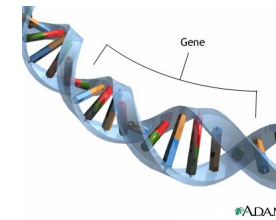


- **Observation:** The “informal” argument discusses phenotypes, i.e. realized behaviors or traits.
  - Genotypes matter only insofar as they produce traits or behavior that affect survival and reproduction.
- Human culture is a collection of behaviors and artifacts: it is not primarily a genetic phenomenon.
- So models of natural selection might be applicable to modeling **cultural evolution** as well.

## CULTURAL EVOLUTION

- This is how **population** level models of selection (whether natural or cultural) work:
  - Selection acts on the population as a whole.
- How should we use ABMS to understand “cultural evolution”?
  - Answering these questions requires speculating about the mechanism by which culture is transmitted ...

## CULTURAL EVOLUTION



**Question:** In biology, there is a mechanism by which traits are passed from parent to offspring: genes. What is the corresponding mechanism for culture?

*Because of their common informational and evolutionary character, there are strong parallels between genetic and cultural modeling [Mesoudi et al., 2006]. Like biological transmission, culture is transmitted from parents to offspring, and like cultural transmission, so in microbes and many plant species, genes are regularly transferred across lineage boundaries [Abbott et al., 2003, Jablonka and Lamb, 1995, Rivera and Lake, 2004]. Moreover, anthropologists reconstruct the history of social groups by analyzing homologous and analogous traits, much as biologists reconstruct the evolution of species by the analysis of shared characters and homologous DNA [Mace et al., 1994]. Indeed, the same programs biological systematists are used by cultural anthropologists [Holden, 2002, Holden and Mace, 2003].*

Gintis [2012]. pp 216-217.

## OUTLINE

- 1 REVIEW AND MOTIVATION
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  - Components of ABMS of cultural evolution
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## COMPONENTS OF ABMS

Agent based models (ABMS) have the following components:

- Agents with properties (e.g., location, preferences, beliefs)
- Environment (e.g. a terrain)
- Initial Conditions for agents and environment
- Rules specifying how agents interact with one another and the environment

## EXPLAINING WITH ABMS

So to build an ABM that explains some phenomenon (e.g. just behavior and/or meaning), it suffices to do the following:

- 1 Describe each component of an ABM
- 2 Identify the phenomenon (here, just behavior or meaning) to be explained with a possible configuration of the ABM
  - **Example:** If we wished to explain why some species went extinct, we could build an ABM and identify its real-world extinction with the state in the ABM in which the “virtual species” dies out.
- 3 Show that the ABM, with high probability, converges towards the configuration identified.

## ABMS OF CULTURAL EVOLUTION

In a nutshell, here's how we'll attack each of these steps for Plato's puzzles.

## ABMS OF CULTURAL EVOLUTION

**Step 1:** Build an ABM in which agents repeatedly play a game.

- Two-player games (e.g., Prisoner's dilemma, stag hunt, Lewis signaling games) are most common.
- Models with multi-player games do exist.

## ABMS CULTURAL EVOLUTION

**Step 2:** Identify just behavior (and or the existence of meaning) with a **strategic profile** in a game.

## THE PRISONER'S DILEMMA

Glaucon's definition:

*This, they say, is the origins and essence of justice. It is intermediate between the best and the worst. The best is to do injustice without paying the penalty; the worst is to suffer it without being able to take revenge. Justice is a mean between the two extremes.*

	Justice	Injustice	
Justice	$\langle 2, 2 \rangle$	$\langle 0, 3 \rangle$	
Injustice	$\langle 3, 0 \rangle$	$\langle 1, 1 \rangle$	

## ABMS CULTURAL EVOLUTION

**Step 3:** We'll argue that **If**

- Players repeatedly play certain games in certain environments
- Learn to interact with one another over time in certain ways,

**Then** the strategic profile corresponding to just behavior (respectively, meaningful communication) will become prevalent.

## ABMS OF CULTURAL EVOLUTION

**Step 1:** Build an ABM in which agents repeatedly play a game.

## PROPERTIES OF AGENTS

**Question:** Who/what are the agents in these ABMs and what properties do they have?

**Answer:** We make no deep “metaphysical” assumptions about who/what the agents are.

We simply stipulate they have the following properties:

- Preferences over strategic profiles of the game
- Learning rules for choosing which actions/strategies to employ in light of past behavior.
- Location in a social network

## COMPONENTS OF ABMS

Which components of an ABM of cultural evolution remain to be described?

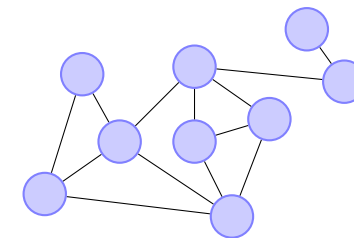
- Agents with properties (e.g., location, preferences, beliefs)
- Environment
- Initial Conditions for agents and environment
- Rules specifying how agents interact with one another and the environment

## PROPERTIES OF AGENTS

**Question:** In what type of environment do agents interact?

**Answer:** A social network.

## NETWORKS



Nodes = Agents

Edges = Indicate which agents “interact” , by playing a game

## COMMON SOCIAL NETWORKS



What are some common social networks that might be represented in this way?

- Facebook (Edges indicate the “friend” relation)
- The world-wide web (Edges indicate reciprocal links)
- Co-authorship networks (Edges indicate co-authors)
- Actor Network (Edges indicate the actors have appeared in a movie together)

## COMMON FEATURES OF SOCIAL NETWORKS

Many social networks share **network structure**.

## STRUCTURE OF REAL SCIENTIFIC NETWORKS

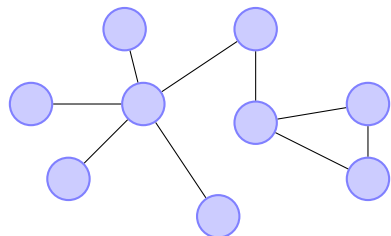
What types of structural properties do academic co-authorship networks and other social networks share?

Here are four.

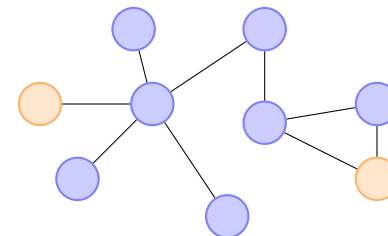
**Small Diameters**



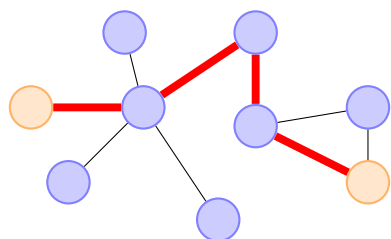
## FINDING THE DIAMETER



## FINDING THE DIAMETER



## DIAMETER



Diameter: The longest-shortest path between any two nodes in the network.

## EMPIRICAL SIZE OF CONNECTED COMPONENTS

number of authors	biology 1,520,251	physics 52,909	mathematics 253,339
diameter	24	20	27

Newman [2001]

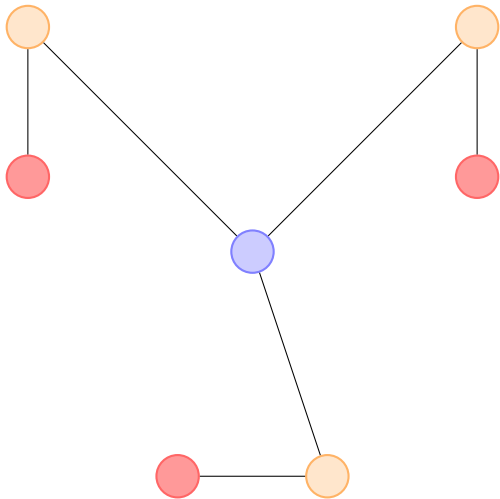
## SMALL DIAMETER

Many other social networks have small diameters (and **average-path-length**)

- E.g., [Milgram, 1967]'s small world experiment
- E.g., The Kevin Bacon Game
- E.g., Erdős Numbers

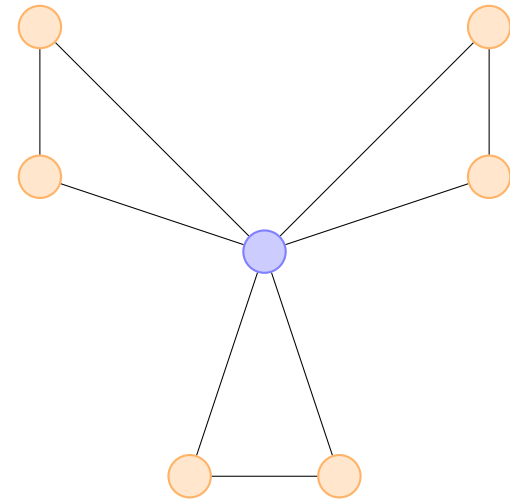
Highly Clustered

## CLUSTERING COEFFICIENT



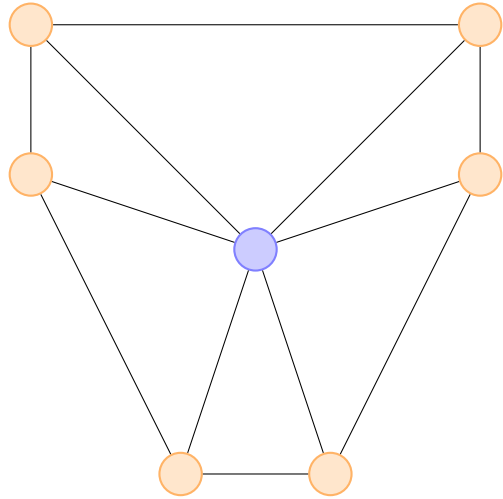
**Not** clustered

## CLUSTERING COEFFICIENT



More Clustered

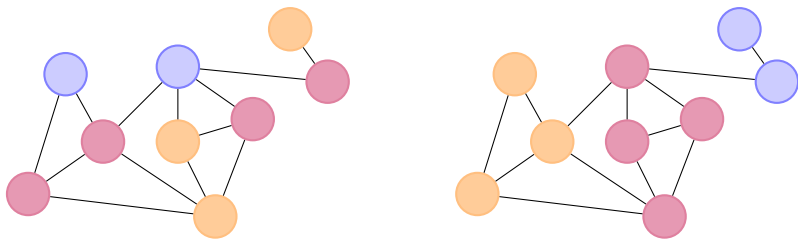
## CLUSTERING COEFFICIENT



Highly Clustered

High Homophily

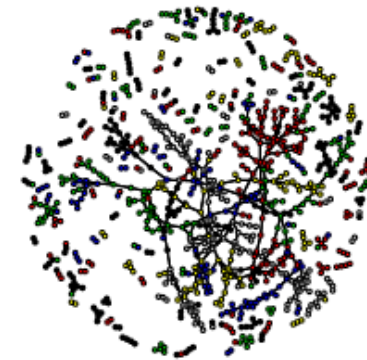
## HOMOPHILY



Left: A Non-Homophilous Network

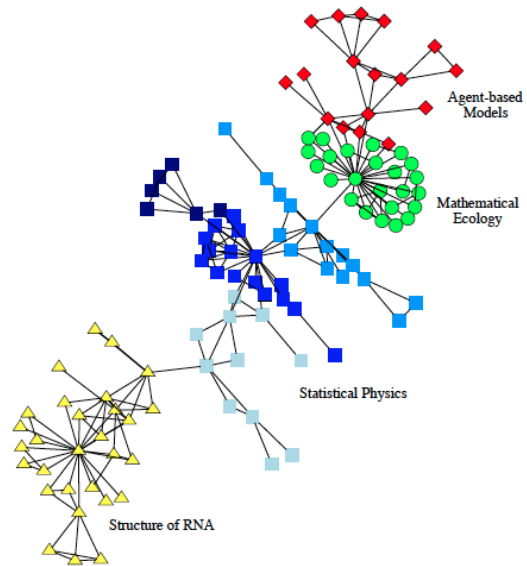
Right: A Homophilous Network

## HIGH SCHOOL SOCIAL NETWORKS



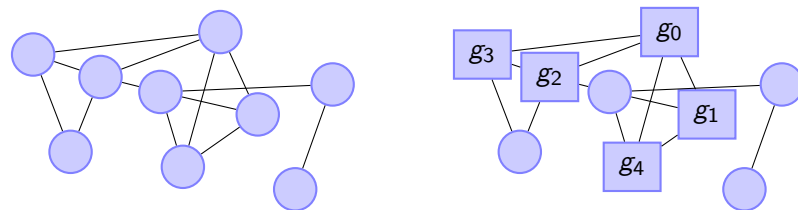
Goodreau et al. [2008]

# ACADEMIC SOCIAL NETWORKS



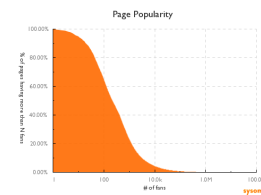
Power Law Degree Distribution

# NEIGHBORHOODS



$g_0$ 's neighborhood

# POWER LAW DEGREE DISTRIBUTION



- Power law degree distribution
  - The **degree** of a node is the number of its neighbors.
  - A power law degree distribution indicates most agents have a few neighbors; few have a modest number; even fewer have many; etc.

## COMMON FEATURES OF SOCIAL NETWORKS

Average-path-length, diameter, degree distributions, etc. are called **network structure**.

## COMPONENTS OF ABMS

Which components of an ABM of cultural evolution remain to be described?

- ~~Agents with properties (e.g., location, preferences, beliefs)~~
- ~~Environment~~
- ~~Initial Conditions for agents and environment~~
- ~~Rules specifying how agents interact with one another and the environment~~

## INITIAL CONDITIONS

**Question:** What properties do agents and their social network initially have?

**Answer:**

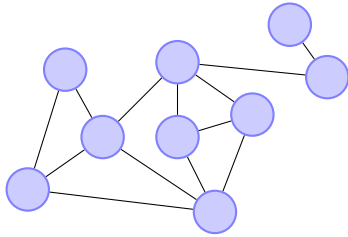
- Of course, when scientists know a lot about social conditions thousands of years ago, we can use those to build models . . .
- However, we often don't know much. So modelers consider a wide variety of initial conditions to ensure their conclusions are **robust**.
  - Example: Vary agents' initial strategies in the game.
  - Example: Vary the strength of agents' preferences.
  - Example: Vary the social network.

## COMPONENTS OF ABMS

Which components of an ABM of cultural evolution remain to be described?

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## INTERACTION



**Question:** How do agents interact with one another?

**Answer:**

- Time is divided into discrete steps: stage 1, stage 2, etc.
- On each stage, each agent plays the game with **all** of her neighbors.
- She gets to observe her performance and that of her neighbors.

## LEARNING RULES

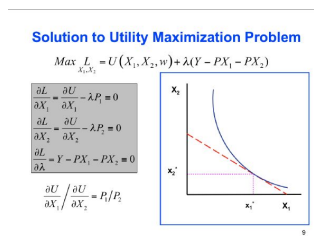


**Question:** Which actions do agents employ, and how do they choose?

**Answer:**

- For simplicity, assume she chooses the same action in each of the games.
- Agents choose actions using **learning rules**.
  - There are dozens of learning rules; I'll describe three types.

## LEARNING RULES: EXPECTED UTILITY MAXIMIZATION



**Type 1:** Agents are classically rational; they maximize subjective expected utility.

- E.g., An agent uses her neighbors past behavior to estimate the probability of their future actions. She then chooses the action maximizing her expected payoff.
- This is not common in agent-based modeling.

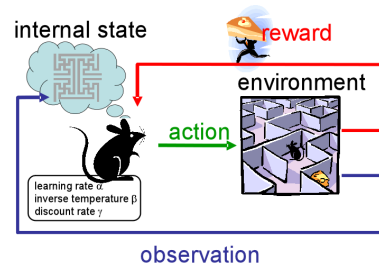
## LEARNING RULES: IMITATION



**Type 2:** Imitation Rules

- E.g., The agent adopts the best action of one of her neighbors, i.e., the action that had the highest payoff in her neighborhood.

## LEARNING RULES: REINFORCEMENT LEARNING

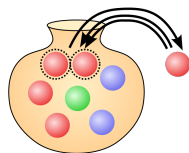


### Type 3: Reinforcement learning

- Each time an action leads to some success, the agent becomes more likely to employ it in the future.
- So agents roughly employ mixed strategies in which the probability of an action is proportional to its past payoffs.

**Example:** Here's a specific type of reinforcement learning, sometimes called Roth- Erev reinforcement learning.

## LEARNING RULES: REINFORCEMENT LEARNING



- Imagine the agent has a big urn with different colored balls.
- Different actions  $\Rightarrow$  Different color balls.
  - Example: Stag = blue; Hare = red.
- On each stage, the agent pulls a ball from the urn (at random) and plays the corresponding action.
- At the end of the stage, she then replaces that ball with  $n$  many balls of the same color, where  $n$  is her total payoff.
  - For simplicity, assume payoffs are non-negative.

## COMPONENTS OF ABMS

Which components of an ABM of cultural evolution remain to be described?

- Agents with properties (e.g., location, preferences, beliefs)
- Environment
- Initial Conditions for agents and environment
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## WHAT HAPPENS?

**Question:** What happens in ABMs like this when agents repeatedly play prisoner's dilemmas? Stag hunts? Etc.

**Answer:** Let me show you some simulations . . .

## NETLOGO

Today's Programming Concepts:

- If-else statements
- Loops
- Procedures

## COURSE OUTLINE

	Lecture	Tutorial
1	Intro to ABMs; Some Game theory	Data types
2	ABMs of cultural evolution	Loops and procedures
3	Plato's Puzzles Revisited	Agent Commands
4	Group model building	

## REFERENCES I

Abbott, R. J., James, J. K., Milne, R. I., and Gillies, A. C. (2003). Plant introductions, hybridization and gene flow. *Philosophical Transactions of the Royal Society of London. Series B: Biological Sciences*, 358(1434):1123–1132.

Gintis, H. (2012). An evolutionary perspective on the unification of the behavioral sciences. In *Evolution and Rationality: Decisions, Cooperation, and Strategic Behavior*. Cambridge University Press.

Goodreau, S. M., Handcock, M. S., Hunter, D. R., Butts, C. T., and Morris, M. (2008). A statnet tutorial. *Journal of statistical software*, 24(9):1.

Holden, C. J. (2002). Bantu language trees reflect the spread of farming across sub-saharan africa: a maximum-parsimony analysis. *Proceedings of the Royal Society of London. Series B: Biological Sciences*, 269(1493):793–799.

Holden, C. J. and Mace, R. (2003). Spread of cattle led to the loss of matrilineal descent in africa: a coevolutionary analysis. *Proceedings of the Royal Society of London. Series B: Biological Sciences*, 270(1532):2425–2433.



## REFERENCES II

- Jablonka, E. and Lamb, M. J. (1995). *Epigenetic inheritance and evolution: the Lamarckian dimension*. Oxford University Press.
- Mace, R., Pagel, M., Bowen, J. R., Otterbein, K. F., Ridley, M., Schweizer, T., and Voland, E. (1994). The comparative method in anthropology [and comments and reply]. *Current Anthropology*, 35(5):549–564.
- Mesoudi, A., Whiten, A., and Laland, K. N. (2006). Towards a unified science of cultural evolution. *Behavioral and Brain Sciences*, 29(4):329346.
- Milgram, S. (1967). The small world problem. *Psychology today*, 2(1):60–67.
- Newman, M. E. (2001). The structure of scientific collaboration networks. *Proceedings of the National Academy of Sciences*, 98(2):404—409.
- Okasha, S. and Binmore, K. (2012). *Evolution and Rationality: Decisions, Co-operation, and Strategic Behaviour*. Cambridge University Press.
- Rivera, M. C. and Lake, J. A. (2004). The ring of life provides evidence for a genome fusion origin of eukaryotes. *Nature*, 431(7005):152–155.