POLS 205 Political Science as a Social Science

Describing and Exploring Data

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Random Variables & Basic Probability Theory

Central Tendency of a Random Variable

Dispersion of a Random Variable

Exploring Data with Graphics (part 1)

Running example: Household wealth in 2007

We take the following data from the 2007 Survey of Consumer Finances:

Net Household Wealth The sum of financial and non-financial assets (e.g., vehicle and home equity), minus debt, in thousands of dollars

Education The education of the head of household, coded as less than high school, high school, some college, and college

Age The age of the head of household, in years

Race The self-identified race of the head of household: non-Hispanic white, black, Hispanic, Asian, or other

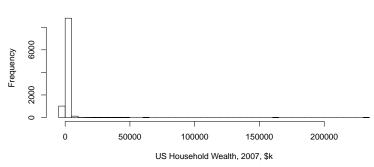
Running example: Household wealth in 2007

The first few samples from this data are:

wealth	educ	age	race
-0.40	Less than HS	48	White
689.00	Less than HS	67	White
197.40	College	44	White
-9.25	High School	51	White
19.02	High School	49	White
-3.66	College	36	White

Our primary interest is in wealth

We have 10000 samples: how can we get an overview of the data without poring over a hundred slides of numbers?



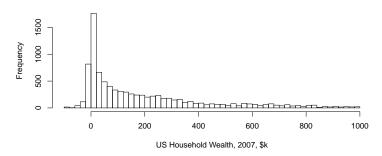
Histogram (all values)

Make a histogram!

One problem: the distribution of wealth has many small values and a small number of very large ones

Bill Gates is skewing the scale and pushing the rest of us into the left bin



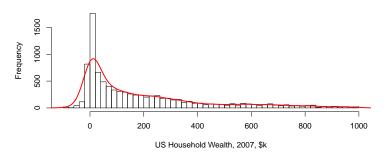


Let's restrict the picture to households with less than one million in wealth

Note that the choice of "bins" for the histogram is up to us

Our program may default to bins that are too wide or too narrow





Finally, we can replace the whole histogram with a density plot

The red line was produced by a kernal density estimator (technical)

Don't need to know how to make, just that it can help clean up the graph

Random variables review

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-3.66	College	36	White

Quick review: what are the levels of measurement here?

Review from last time

Recall the three different ways to divide random variables into categories:

- Discrete vs. Continuous
- Nominal vs. Ordered
- Additive vs Ratio Intervals

But what exactly is a random variable?

A random variable is a variable with some probability of taking on each of several values

What is Probability?

Suppose that we can make a mutually exclusive and exhaustive list of the possible outcomes of an event

Denote the set of possible outcomes $\Omega \in \{\omega_1, \omega_2, \ldots\}$

This need not be daunting; the event could be which button on a vending machine we choose:

Soda Choice \in {Coke, Sprite, Water}

(Read the \in symbol as "in". It lists the elements of a set)

Probability Theory rests on three axioms (untestable assumptions):

Each possible outcome has a probability All the possible choices have probability $0 \le \Pr(\omega) \le 1$

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We usually write probabilities as numbers between 0 and 1

But people understand probabilities better as frequencies

Say "1 in 1000 chance", not "Probability of 0.001", to minimize misperception

Probability and Random Variables

A random variable is one which varies from case to case probabilistically

Next time, we'll talk about how that variation might arise from mathematical functions called probability distributions

Today, we will summarize that empirical, or sample, variation of the variable

There are two broad ways to summarize sample variation:

- Identify the central tendency of a variable
- Measure the dispersion around that center

Defining measures of central tendency

Consider a random variable *x* with $n_x = 15$ observations:

3 8 9 4 3 8 1 8 7 8 1 5 3 10 8

It will help to sort this variable from smallest to largest.

Define $x_{\text{sorted}} = \text{sort}(x)$:

1 1 3 3 3 4 5 7 8 8 8 8 8 9 10

How can we summarize the central tendency of this variable?

Three options: the mode, median, and mean

The mode of a variable is its most common value:

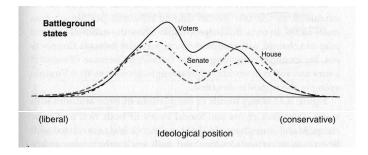
1 1 3 3 3 4 5 7 8 8 8 8 8 9 10

In this case, 8 is the most frequently occurring value.

The mode is clearly defined for **any discrete** variable. Doesn't matter if the variable is ordered/nominal, additive/ratio

The mode is not clearly defined for continuous variables

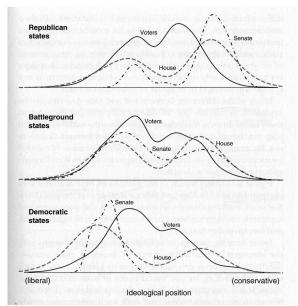
- Recall that the probability that a continuous variable takes on any specific value is 0
- There are just too many possible values for any one to repeat
- So there won't be a clear mode in the literal sense
- However, social scientists often speak of the mode of a continuous variable with reference to its density



Each maximum on this density graph can be though of as a "mode" (Graph from Gelman, *Red State, Blue State*)

If more than one maximum appears, we call the variable "multi-modal" (e.g., bimodal)

If only one maximum appears, we call the variable "unimodal"



Aside on maxima

Recall from calculus:

A maximum of a twice-differentiable function f(x) occurs whenever: $\frac{df(x)}{dx} = 0$ and $\frac{d^2f(x)}{dx^2} < 0$

A global maximum occurs at x^* when: $f(x^*) = \max(f(x)), \frac{df(x)}{dx^*} = 0$, and $\frac{d^2f(x)}{dx^{*2}} < 0$

A local maximum occurs at x^{ℓ} when: $f(x^*) \neq \max(f(x)), \frac{df(x)}{dx^{\ell}} = 0$, and $\frac{d^2f(x)}{dx^{\ell 2}} < 0$

There can be more than one maximum, but only one global maximum

In social science, we will treat any maximum on the density plot that "stands-out" visually as a mode, whether it is the global max or not

The Median of a Random Variable

The median of a variable is its middle value:

1 1 3 3 3 4 5 7 8 8 8 8 8 9 10

If n_x is even, we can just average the middle-most pair of values.

Formally, the median is:

$$\operatorname{median}(x) = \begin{cases} \operatorname{sort}(x)_{(n_x+1)/2} & \text{if } n_x \text{ is odd} \\ \frac{1}{2} \left(\operatorname{sort}(x)_{n_x/2} + \operatorname{sort}(x)_{n_x/2+1} \right) & \text{if } n_x \text{ is even} \end{cases}$$

Here, of course, it is 7.

The Median of a Random Variable

The median has two nice properties:

- It is defined for any ordered random variable (either continuous or discrete)
- It is *robust*, in the sense that adding a big outlier to the data does not move the median "too much"

For example, suppose we in recording our random variable, we accidentally mistyped 10 as 100.

The mean would double, but the median would still be 7

The mean of a random variable is...

The mean of a random variable is... what exactly?

1 1 3 3 3 4 5 7 8 8 8 8 8 9 10

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The mean is the best known measure of central tendency

We know how to calculate it:

$$\mathrm{mean}(x) = \bar{x} = \frac{1}{n} \sum_{i=1}^{n_x} x_i$$

Here, the mean is $5.7\overline{3}$

But what is it in words? (ie, the mode is the "most common value", the median is "the middle value", and the mean is...)

At the Gauss Street fair, you are offered the chance to win a prize for guessing a man's weight

But the rules of the contest are strict and unusual.

- The man is behind a screen, so you can't judge based on appearance
- He has been drawn at random from the US population
- You must guess his *exact* weight, to the pound, or you win nothing!

What should you guess?

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What should you guess?

The *mode* of US males' weight (rounded to the pound)

This will be more often right than any other guess. (But only right how often?)

Further down Gauss Street, you find another unusual weight-guessing contest.

This time:

- There is one man behind a screen (you still can't judge based on appearance)
- He has been drawn at random from the US population
- You must guess the man's weight to the nearest fraction of a pound.

The closest guess wins.

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What should you guess? The median of US males' weight

In unimodal continuous distributions, the median tends to be close to as much of the data as possible

For most cases, the mean will be higher than the median because of the existence of a small handful of very obese individuals in the US population (outliers)

That is, if the average weight is 175, and there are some individuals weighing 375, there simply can't be any -25 pounders to balance them out in the mean.

At the last booth on Gauss Street, still another vendor seeks your hard-earned money in a weight-guessing contest

This time:

- There are many men behind a screen (you still can't judge based on appearance)
- Each has been drawn at random from the US population
- The booth has invested in a fancy scale that can measure this large group at once. You must guess their combined weight, and know only how many men are in the group

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What should you guess? The *mean* of US males' weight ($\times n$, of course).

Some properties of the mean:

• The mean minimizes the sum of the (squared) distances between the population and itself

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- The mean minimizes the (squared) error of prediction of a random draw from the population
- The mean is the expected value of x. That is

$$E(x) = mean(x) = \bar{x} = \frac{1}{n} \sum_{i=1}^{n_x} x_i$$

When can we use the mean?

Can the mean be computed for all kinds of random variables?

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Can the mean be computed for all kinds of random variables?

No, just additive or ratio level variables

But remember we can convert nominal variables to a series of binary ones, and binary variables are ratio level

So we can convert our education variable to four binary variables, and calculate their means:

Less than High School	0.14
High School	0.33
Some College	0.19
College	0.34

For binary variables, the mean is the only appealing measure of central tendency (why?)

Robustness

A robust statistic is one that is relatively insensitive to extreme values

Extreme values are often misleading:

- They may be simple measurement error; e.g., the coder added a digit
- They may result from unusual processes not similar to the middle of the data; e.g., ithe origins of nternet billionaires' wealth

Non-robust statistics like the mean may reflect the middle of our data poorly compared to robust measures like the median

However, if there are no weird outliers, non-robust measures will be more efficient in using all the available information

Grading example

- Most teachers compute course grades by taking the mean of a set of assignment grades.
- Why use the mean, and not the median or mode?
- When would the mean be the "best" way to compute a course grade?
- When would the median be better?
- Would we ever want the mode?

Weighted Measures of Central Tendency

A simple generalization of mode, median, and mean is to add weights for each observation

Let w_i be a set of weights for each observation

The weighted mean is then $\frac{\sum_{i=1}^{n} w_i x_i}{\sum_{i=1}^{n} w_i}$

What are the weights? Many possibilities

- the number of times that number appears
- a measure of "importance": E.g., School districts weighted by number of students, or countries weighted by GDP

Conditional Measures of Central Tendency

We can also create conditional version of the mean, median, and mode

That is, we can compute the mean wealth conditional on a respondent's age

Or the median wealth for a respondent with a college degree

These are the conditional mean and conditional median

Conditional Measures of Central Tendency

The conditional mean is also an estimator of the conditional expectation, E(X|A)

Potentially useful: Most of our hypotheses are about conditional expectations of dependent variables!

Goal of most inference: find the conditional expectation of our dependent variable given specific values of our independent variables

Can do this even when independent variables are continuous, but not as straightforward.

But a major problem with using conditional means to estimate conditional expectations is the role of confounding variables

That is, conditional means don't control for any other variables

Measures of central tendency leave out a lot compared to histograms

If summarizing a histogram in one number, use a central tendency

But two numbers? What would you want next?

Some sense of dispersion, or how far away the data tend to be from the center

Measuring dispersion

Compared to central tendency, dispersion is easy to overlook, but crucial:

- Tells us how well the center predicts specific values
- 2 Tells us how noisy the variable is
- Tells us how much the world differs from observation to observation

Because social science is about understanding variation, dispersion should be our bread and butter

Three measures of dispersion: range, quantiles, and variance

The Range of a Random Variable

The range of a variable is the set of its minimum and maximum values:

1 1 3	3	- 3	4	5		8	8	8	8	8	9	10
-------	---	-----	---	---	--	---	---	---	---	---	---	----

The range of this variable is [1,10]

The range is the simplest measure of dispersion, but the least useful

Very non-robust: Shifted by the most extreme outliers

The range is defined for any ordered random variable, discrete or continuous

The Quantiles of a Random Variable

The quantiles of a random variable are taken at specific intervals of the sorted variable

1 1 3 3 3 4 5 7 8 8 8 8 8 9 10

For example, we might want the quantiles enclosing the middle half of the data

Those are the 25th and 75th percentiles, highlighted above

Note that the median is the 50th percentile, so the median is a quantile as well

Quantiles are defined for any ordered random variable

The Quantiles of a Random Variable

We could calculate any number of quantiles.

For the wealth data, we have the following quantiles (\$k):

0.1%	-106
1%	-31
2.5%	-15
5%	-5
25%	13
50%	115
75%	365
95%	1908
97.5%	3597
99%	8409
99.9%	25637

Quantiles are great: easy to understand, can summarize dispersion to arbitrary specificity, and are robust

The Variance of a Random Variable

The variance of a variable is the square of the standard deviation:

1 1 3 3 3 4 5 7 8 8 8 8 8 9 10

Here, the variance is 9.0, and the standard deviation is ≈ 3.01

But what is the standard deviation?

- how much a random draw from this random variable would differ from the mean on average
- the expected error when we predict this variable using its expected value

The Variance of a Random Variable

The standard deviation has a simple meaning: "how much we miss by"

Mathematically, this take a bit of work:

$$var(x) = \sigma^2 = E((X - E(x))^2)$$

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Mathematically, this take a bit of work:

$$\operatorname{var}(\mathbf{x}) = \sigma^2 = \operatorname{E}\left((\mathbf{X} - \operatorname{E}(\mathbf{x}))^2\right)$$
$$\operatorname{sd}(\mathbf{x}) = \sigma = \sqrt{\left(\operatorname{E}\left((\mathbf{X} - \operatorname{E}(\mathbf{x}))^2\right)\right)}$$

In words, the variance is how much you expect a specific observation to differ from the mean of the variable, squared

We take the square root to get how much you expect a specific observation to differ from the mean

The Variance of a Random Variable

How do we apply this formula? Let's do some algebra:

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= $E(x^2) - E(x)^2$

This leads to an estimator of the variance $(\hat{\sigma}^2)$ for a given sample of data:

$$\hat{\sigma}^2 = \frac{1}{n} \sum_{i=1}^n (x_i^2) - \frac{1}{n} \sum_{i=1}^n \bar{x}^2$$

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$$= \frac{1}{n} \sum_{i=1}^n (x_i^2) - \bar{x}^2$$

(Stat packages usually use a slightly different estimator that works better in small samples)

Chris Adolph (UW)

$$\bar{x} = \frac{1}{4}(-5-5+5+5)$$

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= 0

$$\frac{1}{n}\sum_{i=1}^{n}(x_i-\bar{x}) = \frac{1}{4}(-5-5+5+5-4\times 0)$$

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= 0

$$\frac{1}{n}\sum_{i=1}^{n}(x_{i}-\bar{x}) = \frac{1}{4}(-5-5+5+5-4\times 0)$$
$$= 0$$
$$\sqrt{\hat{\sigma}^{2}} = \sqrt{\frac{1}{4}(25+25+25+25)-0^{2}}$$

$$\bar{x} = \frac{1}{4}(-5-5+5+5)$$

= 0

$$\frac{1}{n}\sum_{i=1}^{n}(x_i-\bar{x}) = \frac{1}{4}(-5-5+5+5-4\times 0) = 0$$

$$egin{array}{rcl} \sqrt{\hat{\sigma}^2} &=& \sqrt{rac{1}{4}}(25+25+25+25)-0^2 \ \hat{\sigma} &=& 5 \end{array}$$

Okay. But why not take absolute values instead?

We could calculate the absolute error and get the same result:

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$$\frac{1}{n}\sum_{i=1}^{n}|x_i-\bar{x}| = \frac{1}{4}(|-5-0|+|-5-0|+|5-0|+|5-0|)$$

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\end{aligned}$$

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\end{aligned}$$

$$\sum_{i=1}^n |x_i - \bar{x}| &= \frac{1}{4}(|-5 - 0| + |-5 - 0| + |5 - 0| + |5 - 0|) \\
&= 5
\end{aligned}$$

Which suggests that the average absolute deviation is a pretty good measure of dispersion too

 $\frac{1}{n}$

It's a bit more complicated...

But recall I mentioned in small samples we need to correct the estimate of the standard deviation

Using this estimator instead will lower bias in small samples like this one:

$$\hat{\sigma}_{\text{corrected}}^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i^2) - \frac{n}{n-1} \bar{x}^2$$

In this case, a less biased estimate of the sd is thus 5.7 (!)

(Why? Beyond scope of 205; has to do with assuming we know the true population mean when calculating this sd.)

Dispersion for a nominal variable

How do we summarize the dispersion of a nominal variable?

Range, quantiles, and variance are undefined in this case

I recommend fractionalization, which is the probability that any two observations drawn at random have the same value

Fractionalization ranges from $\epsilon > 0$ for a very dispersed variable to 1 for a nominal variable with the same value at each observation

In our wealth data, education has a fractionalization of 0.29, and race 0.59.

Exploratory Data Analysis, Part 1

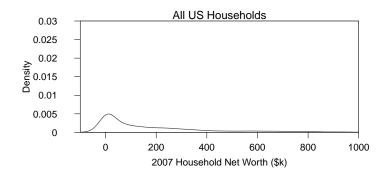
We will spend much time on the "math" of data analysis

But the visual side is equally important

Can quickly come to grips with statistical concepts with the right pictures

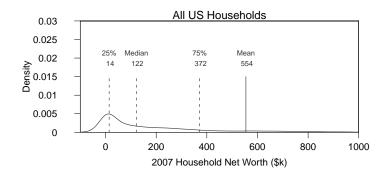
Pictures are the most powerful data analytic tool

But you need to make the right picture—and that takes statistical knowledge



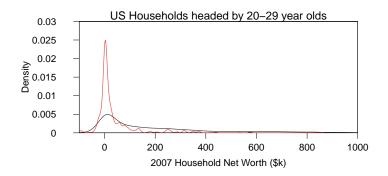
Let's explore the distribution of wealth using pictures.

We'll start by restricting the range of our density plot to the [\$0, \$1,000,000] interval (Why?)



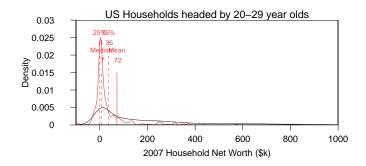
Marking the mean and interquartile range (25th and 75th percentiles) helps: note the mean is much higher than the median

This distribution is *right-skewed*: asymmetric with a long right tail



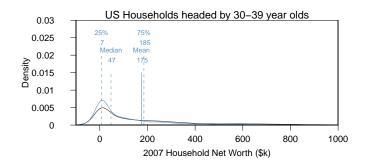
Let's select on age, to focus on people in their twenties

How do these distributions differ?

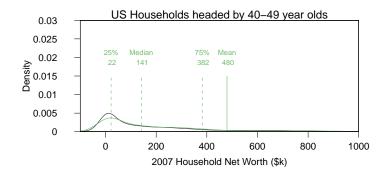


We can also compute *conditional* means and quantiles

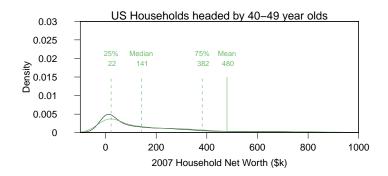
How do these conditional measures differ from the global ones?



From here, we can move up the age variable by ten year increments What do we see?

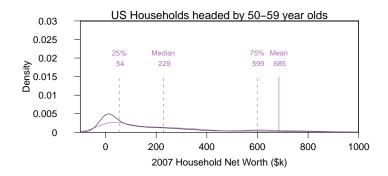


Is the apparent relationship between wealth and age necessarily causal?



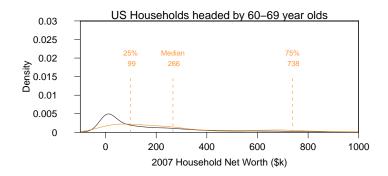
Is the apparent relationship between wealth and age necessarily causal?

What could be confounding this relationship?



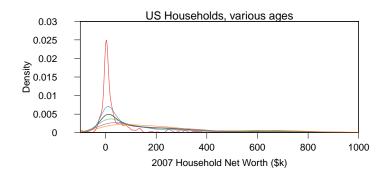
Note that more and more of our data is passing outside the right boundary with each decade

This suggests our "wealth window" approach is too limited



Indeed, the conditional mean doesn't even show up for households in their 60s!

Ideas of what to do to get the rich and not so rich on the same plot?



Looking at all the conditional plots at once

This isn't really possible with histograms—a reason to investigate density plots

Orders of Magnitude

Notice that our wealth data range across many orders of magnitude

(Orders of magnitude means "factors of ten")

This makes it hard to compare changes on different scales

If we scale our graph from \$0 to \$100 million, the range from 0 to \$1 million almost disappears in the left corner

But that's where most people are!

Logarithms

Logarithms help us look at the small and large scale in the same graph

A logarithm is just a mathematical function, log(x), which replaces variables with their order of magnitude

Specifically, the $\log_a(x)$, or "log base *a* of *x*", is defined:

 $a^{\log_a(x)} = x$

That is, when *a* is raised to this number, it equals *x*

The natural logarithm

When taking logs, does it matter which base we use? Not really The base *a* can be any positive number, but is most commonly 10 or a special number *e*

e is a famous constant, 2.718281828...

Logs in base *e* are known as natural logarithms

In this course, $\log(x)$ will be understood to mean $\log_e(x)$

Logarithms

$\log(x)$	$\log_{10}(x)$
-9.21	-4
-6.91	-3
-4.61	-2
-2.30	-1
0.00	0
2.30	1
4.61	2
6.91	3
9.21	4
11.51	5
	-9.21 -6.91 -4.61 -2.30 0.00 2.30 4.61 6.91 9.21

Note that in each row, the \log_{10} and the natural log differed only by a constant factor, 2.30.

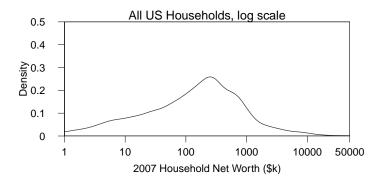
All bases of log differ from the natural log only by a constant multiplicative factor

Finally, note that we can only take the log of positive numbers.

Exponentiation

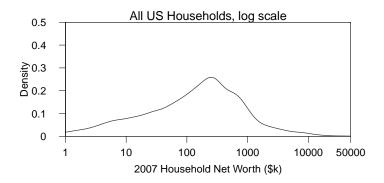
The inverse of the logarithm is just a^x , or exponentiation.

We will write e^x as exp(x) to avoid confusion



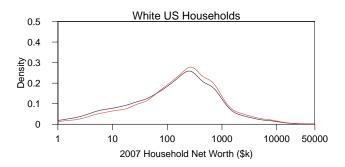
Logging wealth before plotting yields allows us to plot the whole positive range of wealth

We have to leave out negative wealth because negative values can't be logged



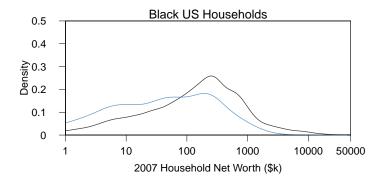
This way of plotting is also referred to as "logging the axis"

That's because all we've done is squeezed the horizontal axis more and more as we move to the right



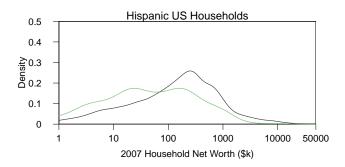
Let's use this new tool to compare wealth for different self-identified racial groups

Here are households with self-identified white heads



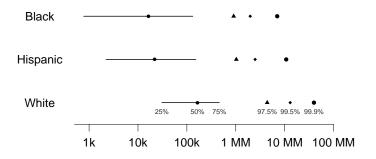
Logging helps reveal the dramatic racial differences at both ends of wealth spectrum

Can we attribute these differences to a direct causal relationship with race (ie, racial discrimination?)



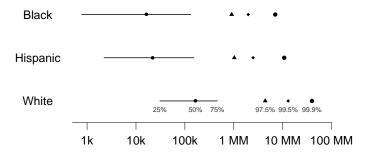
What can we say about the three-way comparison of whites, blacks, and Hispanics?

It would be nice to summarize the key points in a single graphic



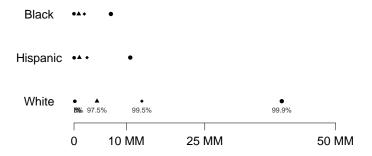
The above plot is known as a dotplot.

Similar to a barchart and to a boxplot (covered in section)



Not as much detail as histograms or densities, but a good compromise for side-by-side comparison.

All good data graphics facilitate comparison of variables or their conditional central tendencies or variances



Why logging is important: Unlogged, almost every household in the US vanishes into a single dot

You won't always log your variables, but if you can "count" it, you probably should try logging it