

# Key Concepts of Monday

- How can we search for the center of the cosmos?
- Charting the universe
  - Finding distances (our tool: Standard Candles)
  - Finding speeds (our tool: Doppler Shift,  $z$ )
  - Relationship between  $z$  and speed (low/high speeds)
  - Correlating distances and speeds (Hubble Diagram)

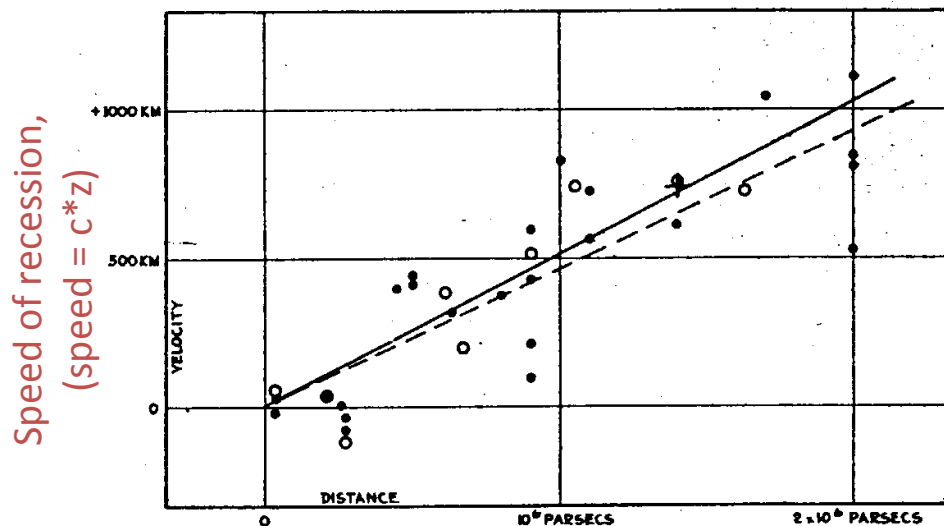


FIGURE 1

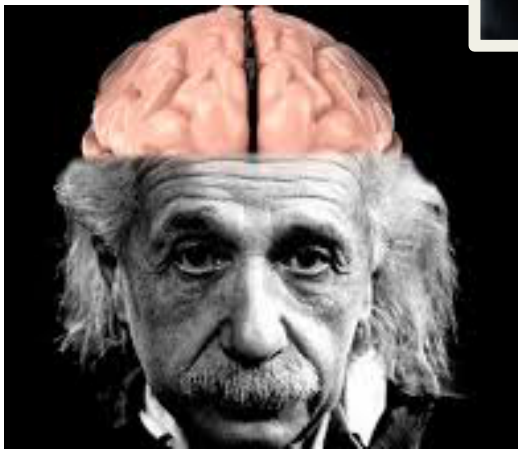
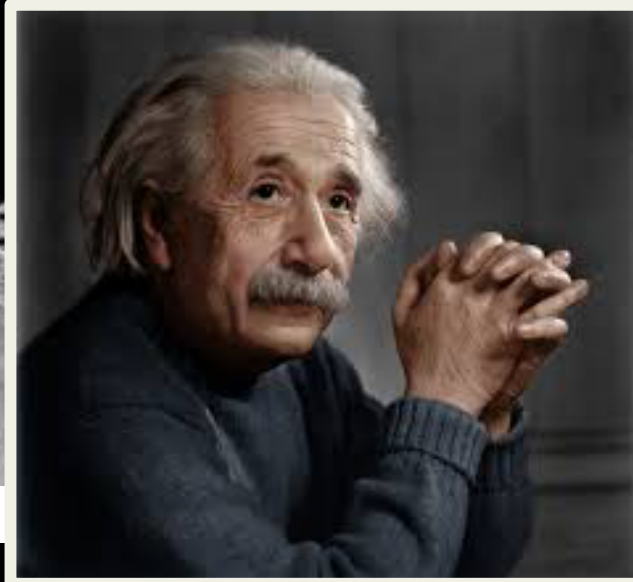
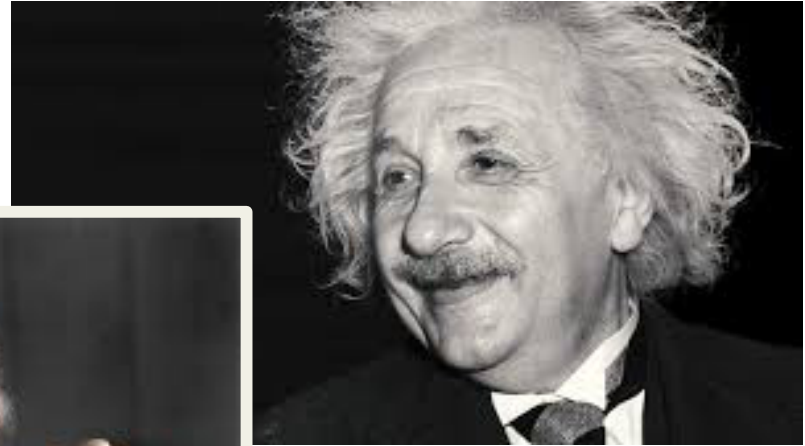
Distance from Milky Way

Coming soon  
(Homework 3)  
Does the Hubble  
Diagram require  
that we are at the  
cosmic center?

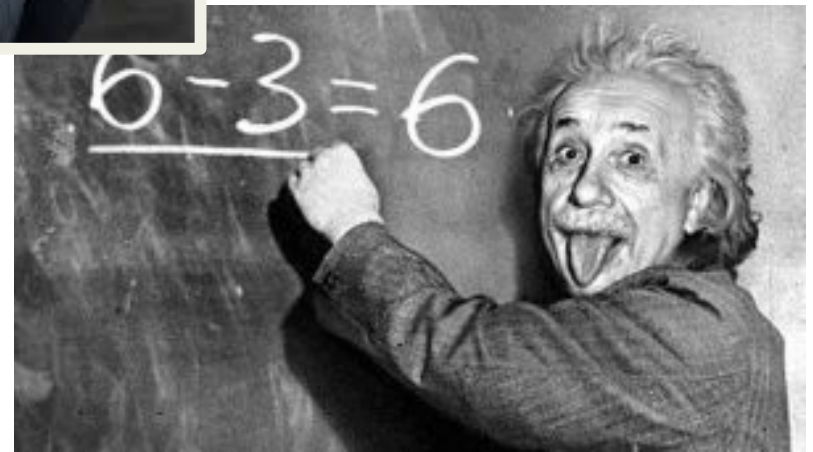
Enter Einstein 1905+

The Shape of Space

Highlights of Text Chapter 1



14 March 1879  
– 18 April 1955



# Einstein and a radical new view of space and time

## Einstein's ANNUS MIRABILIS papers (1905-06)

([https://en.wikipedia.org/wiki/Annus\\_Mirabilis\\_papers](https://en.wikipedia.org/wiki/Annus_Mirabilis_papers))

### Four Revolutionary Papers:

(Measurement of the sizes of molecules)

1. Brownian motion (heated atoms migrate throughout a containing vessel)
2. Photoelectric effect (introduction of "photons"), **Nobel Prize, 1922**
3. Special Relativity (meaning of "simultaneity" and inertial reference frames)
4. Mass-energy equivalence ( $E_{\text{rest}} = mc^2$ )

### Principles of special relativity

- the laws of physics remain the same for any "inertial" (non-accelerating) frame of reference
- the speed of light has the same value in all inertial frames of reference, independent of the state of motion of the emitting body
- there is no absolute frame of reference

### Principles of general relativity

- experiment cannot distinguish causes of acceleration (springs, gravity, etc)
- the paths of light are influenced by gravity (globally and near masses)

# Einstein Sets the Stage

$$E = mc^2$$

Mass and energy are equivalent

Let's look under the hood.

# Energy of Motion: Classical Physics

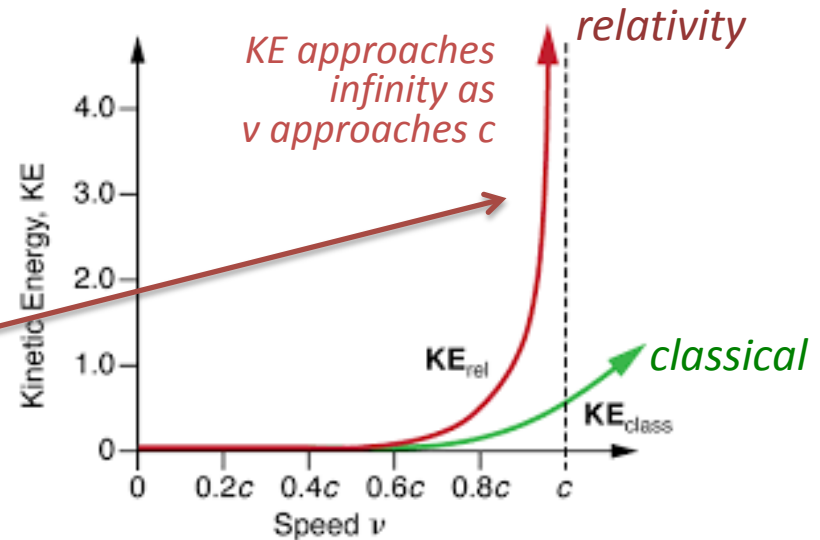
$$KE = \frac{1}{2}mv^2$$

Kinetic energy is energy of motion

# Energy of Motion: Relativity (1906)

$$\text{total energy } E = \text{“rest energy”} + KE$$

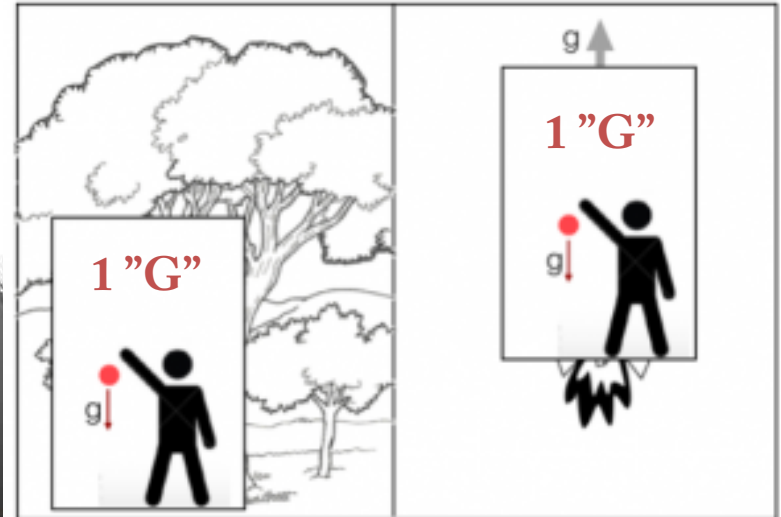
$$E_{rest} = mc^2$$
$$KE = \frac{mc^2}{\sqrt{1 - v^2/c^2}}$$



*This is why mass can't be accelerated to the speed of light: Requires infinite energy!*

# Scales measure force

Equivalence  
Principle



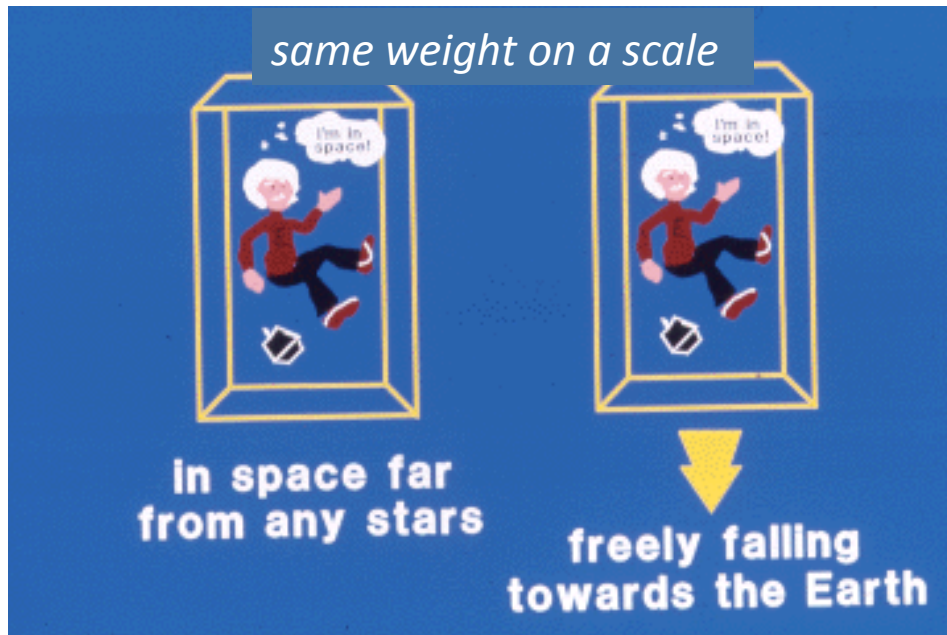
Scales respond equivalently in gravity or an accelerating reference frame.  
Weight and acceleration are the same.

## EASY TO USE

Step and Read-Immediate readings as soon as you step on the bathroom scale

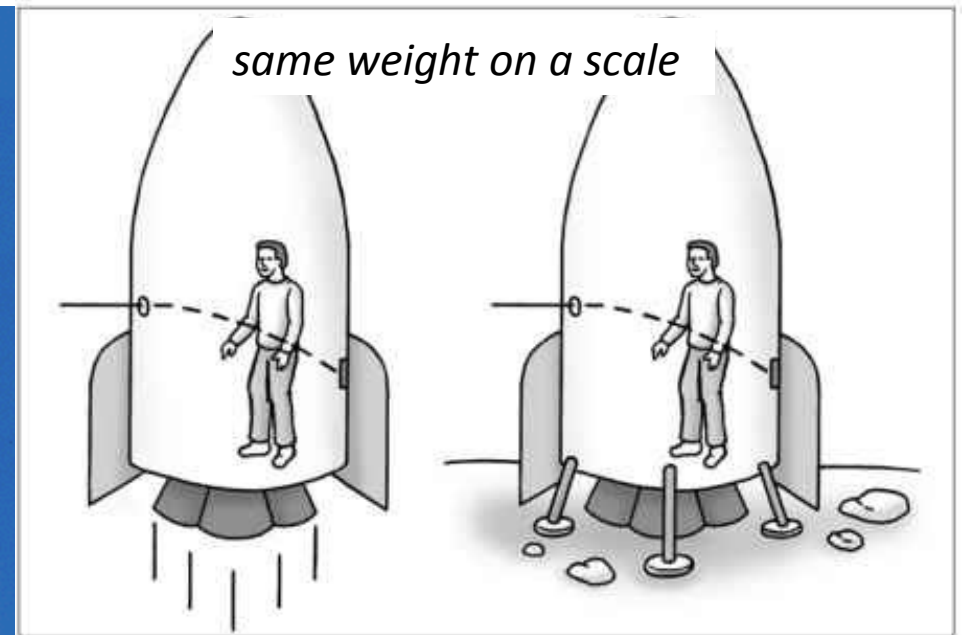
# Einstein's Equivalence Principles

You can't tell the difference



weightlessness

Weightlessness is possible with or without gravity. *You can't tell if you're in an empty universe or a free-falling elevator.*

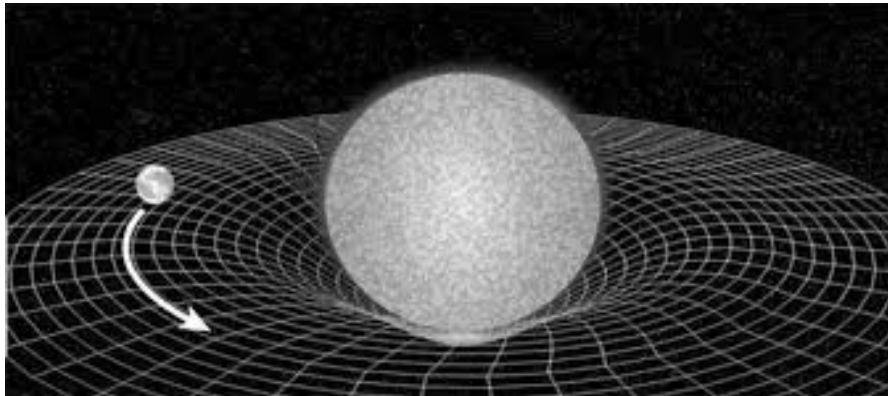


weight and curvature

Light traversing an accelerating rocket **OR** under the influence of gravity follows a curved path. *You can't tell the difference.*



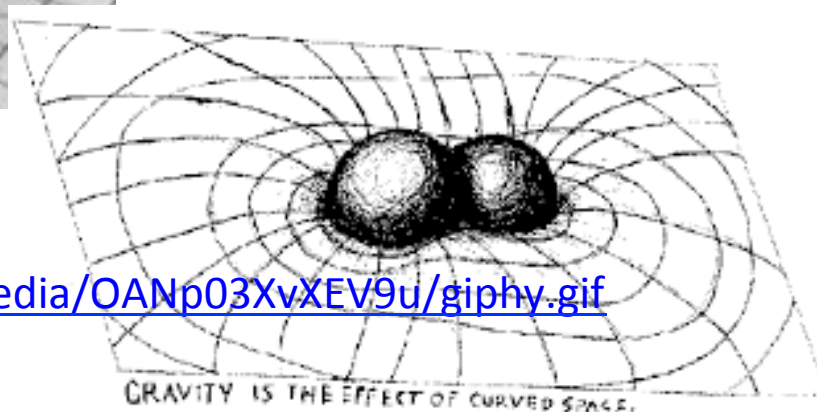
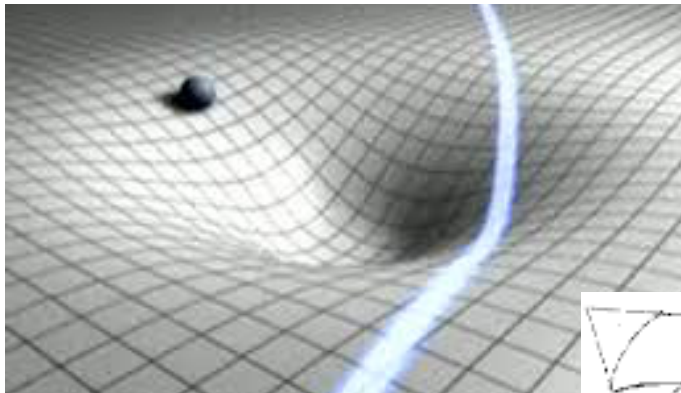
# The Curvature of Space



Masses bend space locally.

***Gravity and the curvature of space are equivalent.***

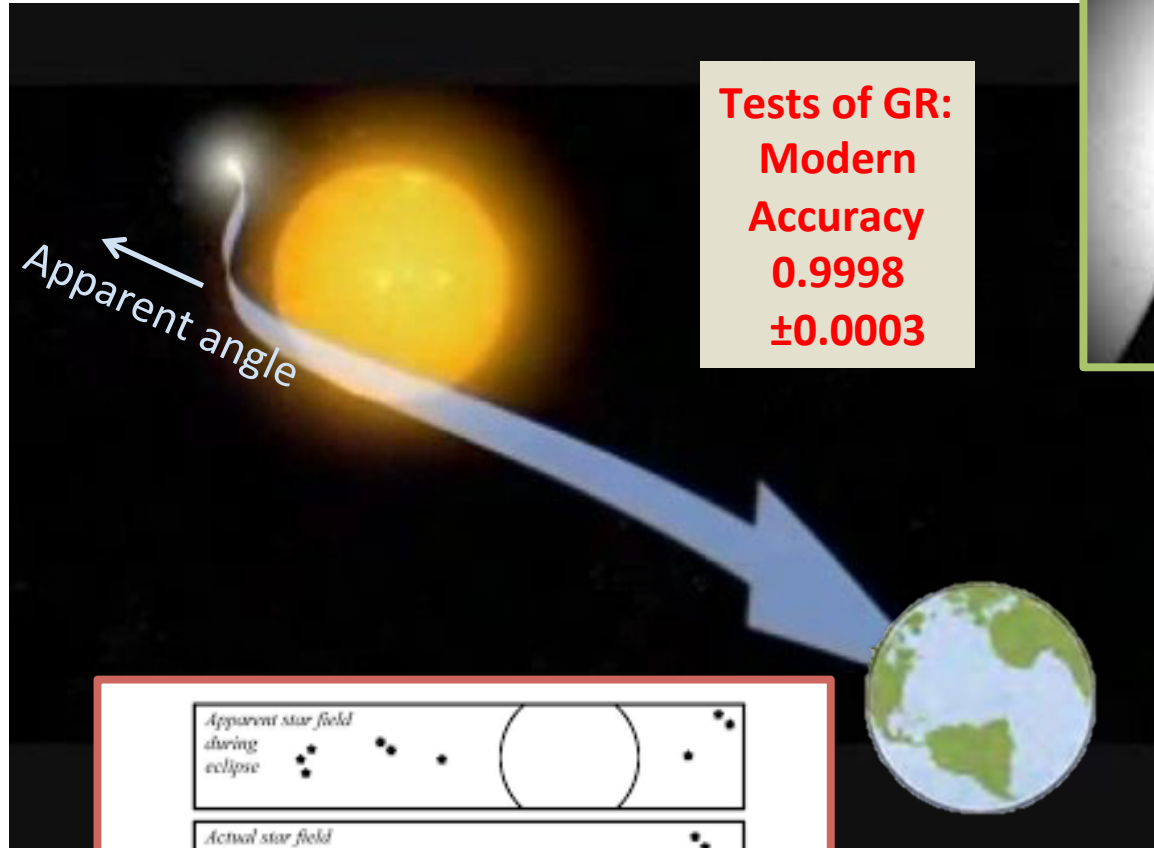
Since space is curved, all paths through space (including light rays) are also curved.



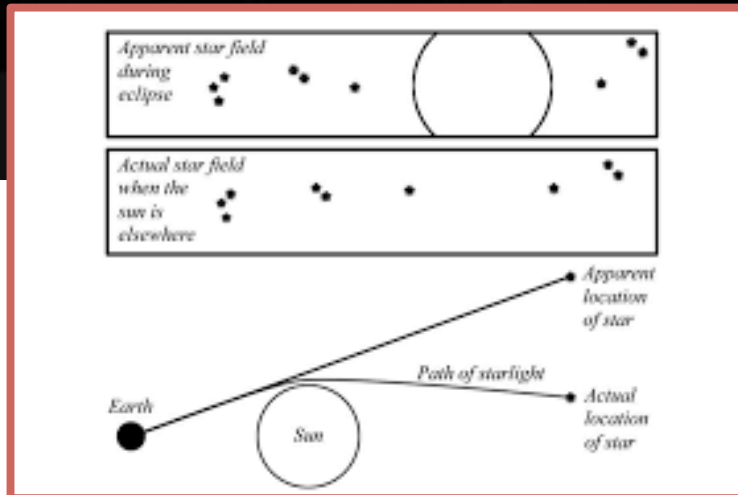
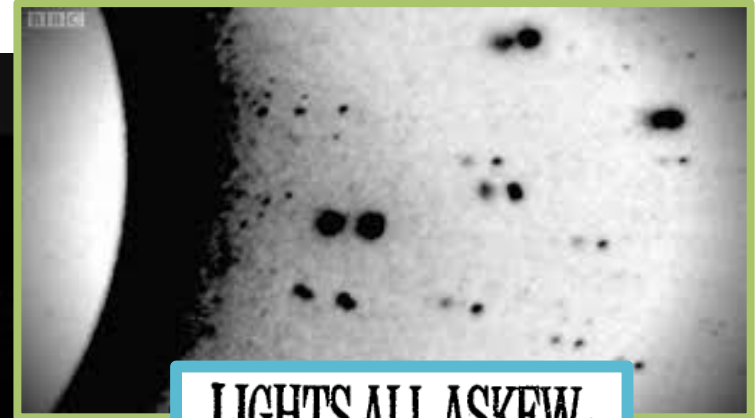
**Black Holes merging**

<https://media.giphy.com/media/OANp03XvXEV9u/giphy.gif>

**Einstein's famous prediction was verified.  
He became an instant rock star!**



**Tests of GR:  
Modern  
Accuracy  
0.9998  
 $\pm 0.0003$**



## LIGHTS ALL ASKEW IN THE HEAVENS

Men of Science More or Less  
Agog Over Results of Eclipse  
Observations.

### EINSTEIN THEORY TRIUMPHS

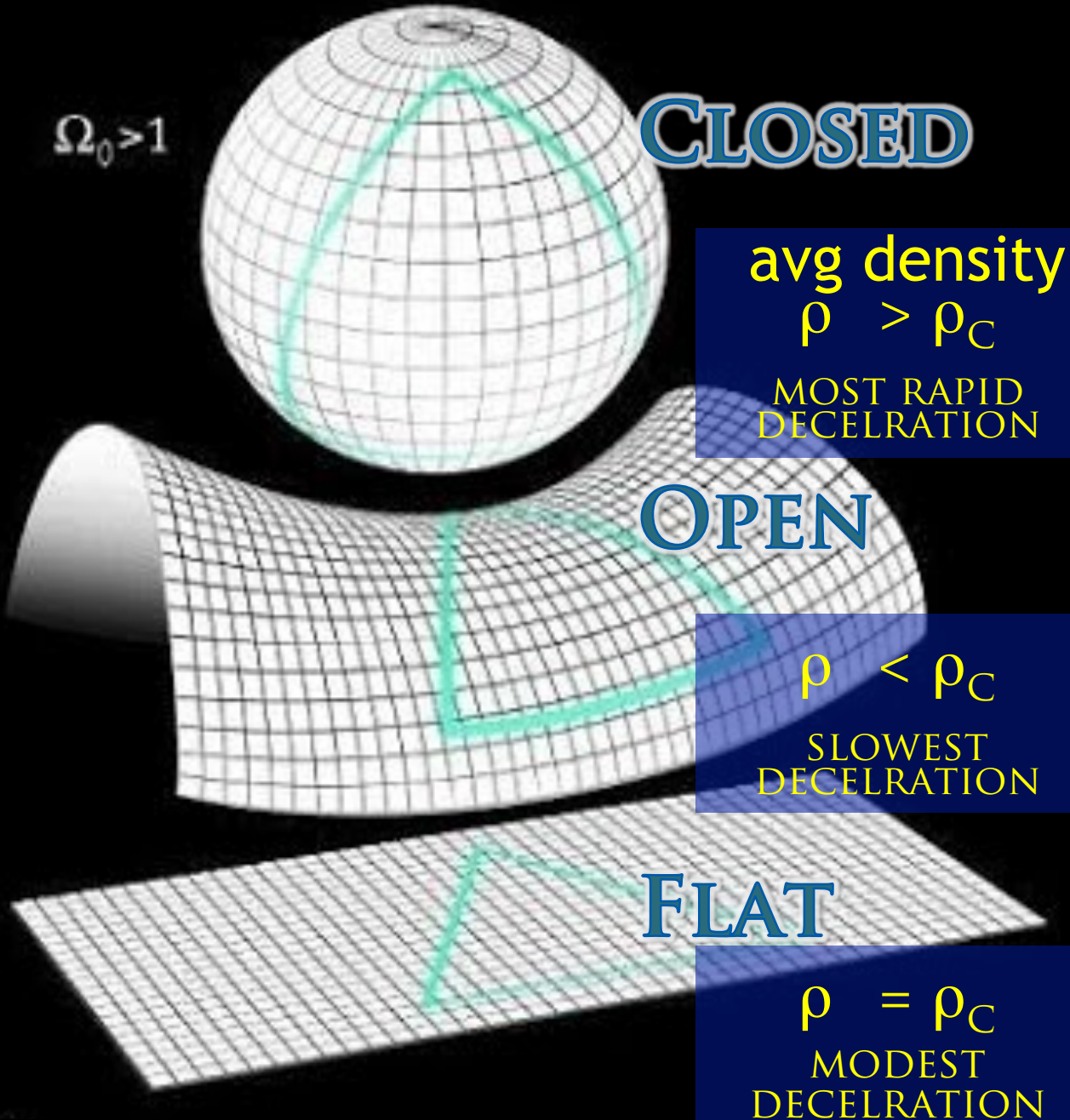
Stars Not Where They Seemed  
or Were Calculated to be,  
but Nobody Need Worry.

### A BOOK FOR 12 WISE MEN

No More in All the World Could  
Comprehend It, Said Einstein When  
His Daring Publishers Accepted It.

# EINSTEIN: POSSIBLE SHAPES OF SPACE

$$\Omega_0 > 1$$



**CLOSED**

avg density  
 $\rho > \rho_C$

MOST RAPID  
DECELERATION

**OPEN**

$\rho < \rho_C$

SLOWEST  
DECELERATION

**FLAT**

$\rho = \rho_C$

MODEST  
DECELERATION

## 1917: General Relativity: The Field Equation(Cosmic & Local)

“A gravitational field acts on matter telling it how to move. . .  
matter generates gravitational fields in space-time, telling  
it how to curve”

Text, middle of page 40

$$R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R = \frac{8\pi G}{c^4} T_{\mu\nu}$$

Left side: the shape of space  
Used to derive the shortest path between  
points  $\mathbf{x}$  and  $\mathbf{y}$  (light must take it)

Right side: The directional “stresses”  
on space imposed by gravity

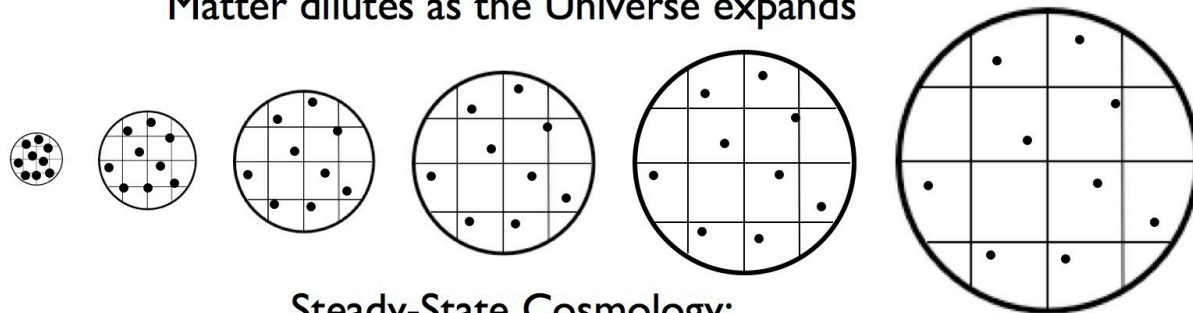
**Note: cause and effect are not distinguished: mass bends space; the bending of space causes acceleration (deviations from uniform motion); accelerations and bending of space are equivalent**

# *Expanding for sure! Even so, does the Universe actually change???*

## Big Bang

Uniformity required, but evolution of the gross properties of the Universe is OK.

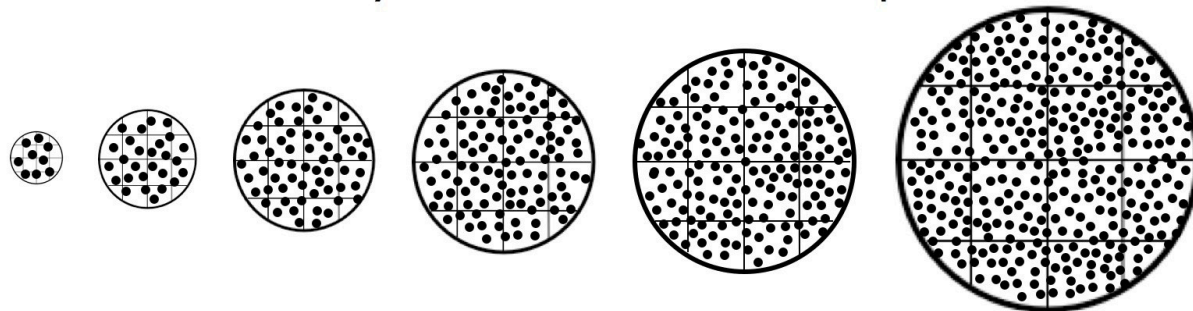
Big Bang Cosmology  
Matter dilutes as the Universe expands



## Steady State

Uniformity required, and no evolution of the gross properties of the Universe

Steady-State Cosmology:  
Matter is constantly created as the Universe expands



*SS: If cosmic density is really constant and its volume increases then new matter must constantly be created in situ!*

# Early Theoretical Cosmology

## A Universe that can't sit still: from Einstein to LeMaitre

Everyone had long believed in a static Universe

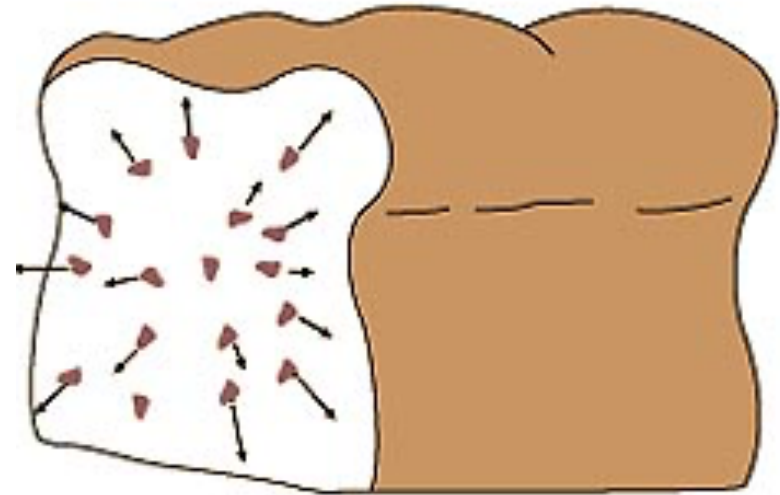
- When he derived General Relativity Einstein realized that his equations had the same problem as Newton's falling sky:  
**imminent gravitational collapse!**
- DeSitter showed that an empty universe with matter was stable if it expanded fast enough. Friedman (others) . . .
- In 1927 Lemaitre proposed that Hubble's observations of increasing galaxy-distances was the result of the expansion of space itself (**raisin cake, balloon, and trampoline analogies**)
  - *Nothing can move through space faster than light,*
  - ***but this restriction doesn't apply to space itself!***
  - *Galaxies don't move **THROUGH** space, they move **WITH** it.*

***Important!***

# *Expanding Space or Flying Galaxies: They aren't equivalent.*



Einstein-de Sitter



Lemaitre

*How can we rule one (or both) out?*

# The Restless Universe

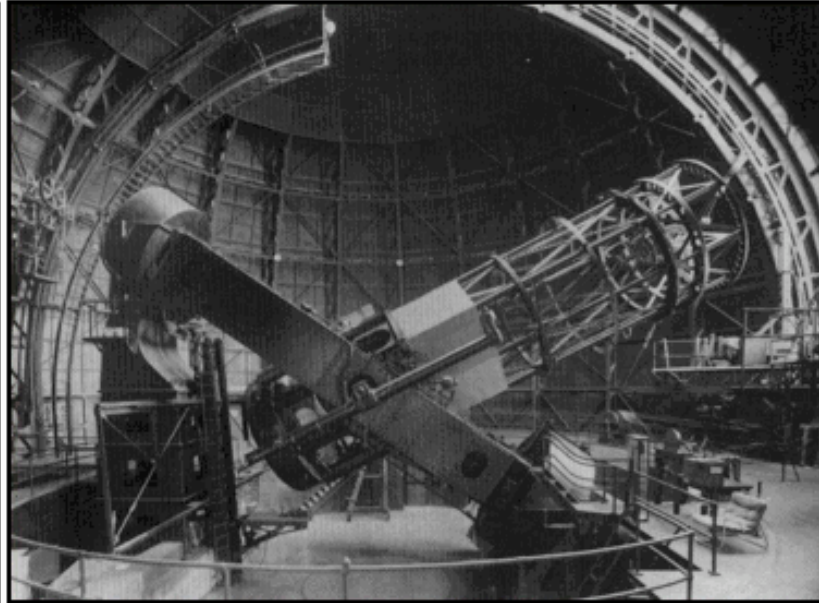
## Hubble (and colleagues)

Highlights of Text Chapter 2





Edwin Hubble  
1889 – 1953



100 inch Mt Wilson Telescope



Milton Humason  
1891 – 1972



Vesto Slipher  
1875 – 1969

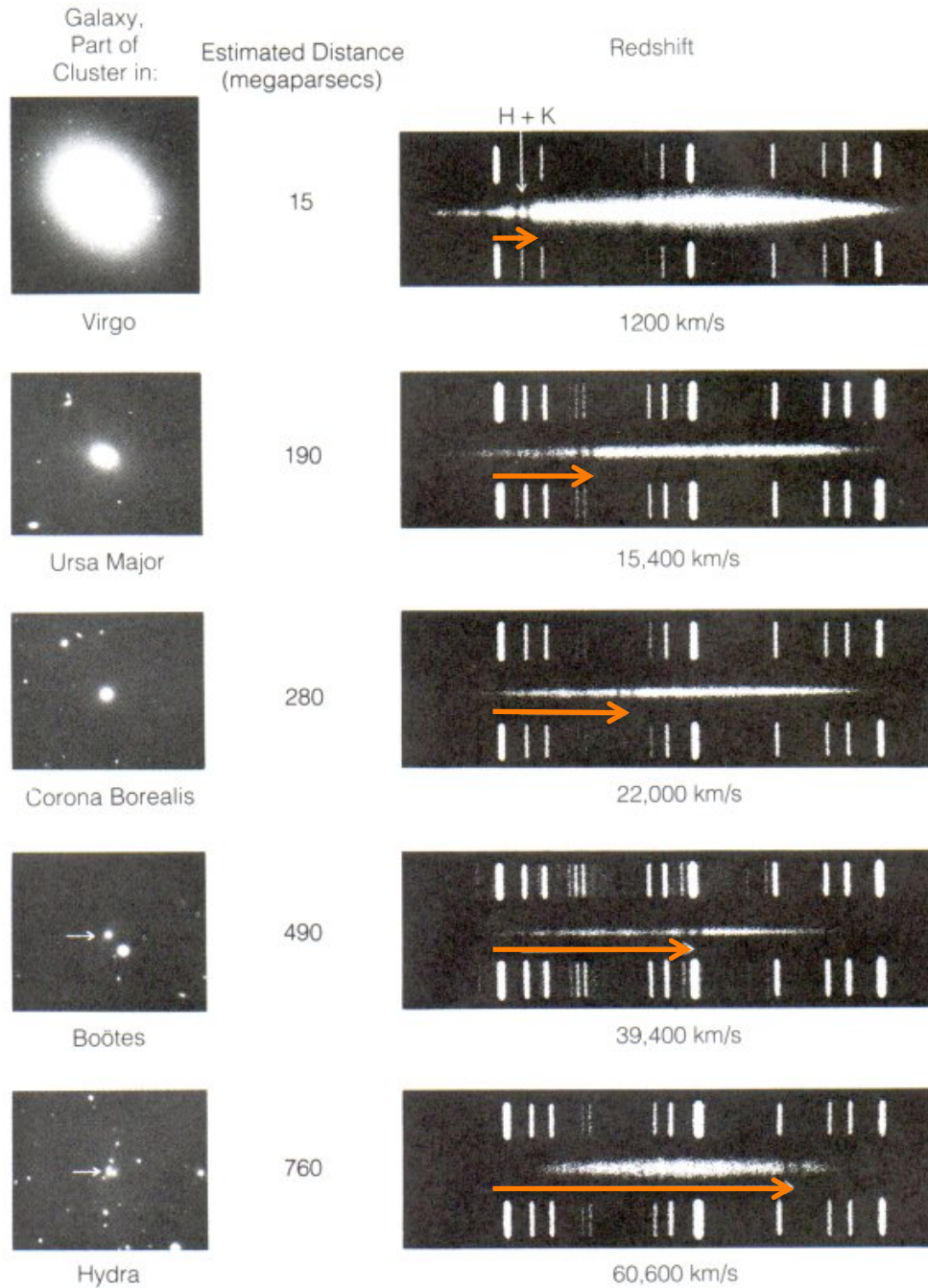


Fritz Zwicky 1898 – 1974

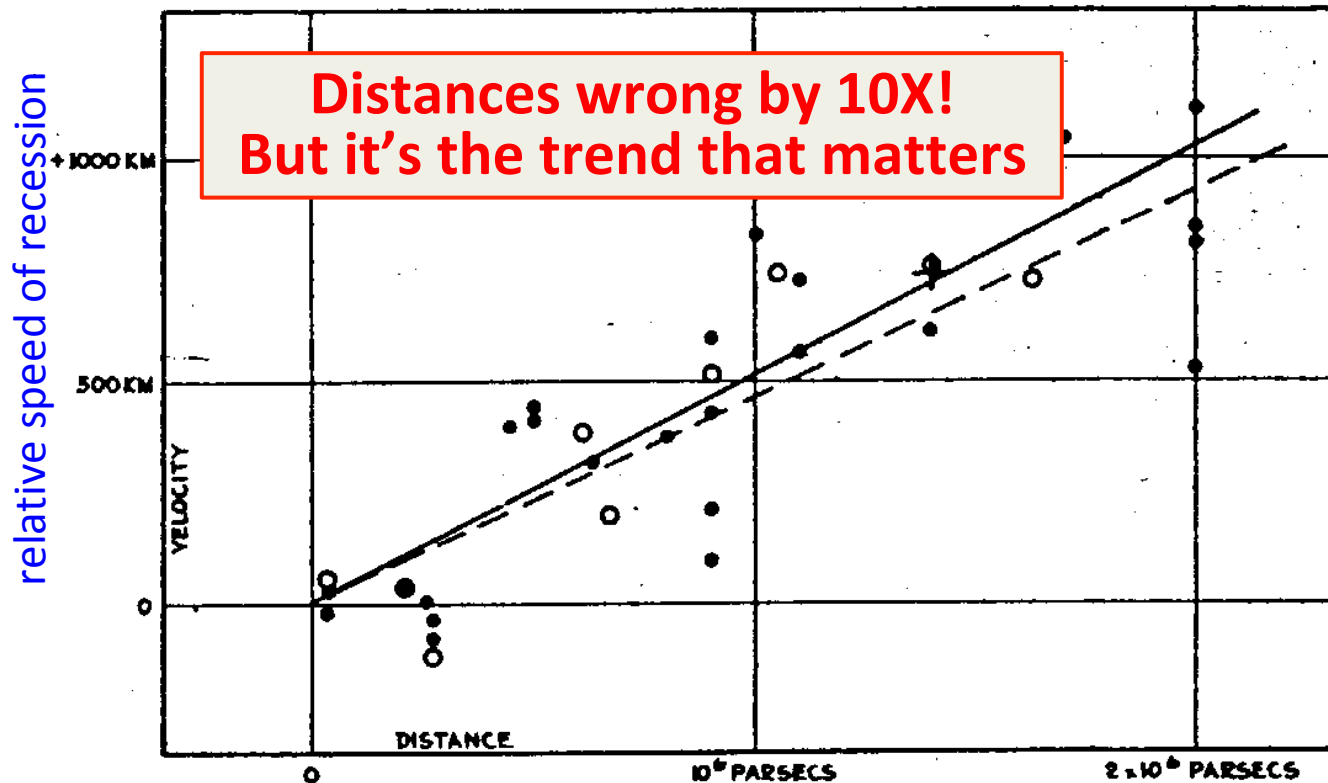


Allan Sandage 1926 – 2010

# 1920s: Slipher and his spectra



# 1920s: Hubble and his first diagram

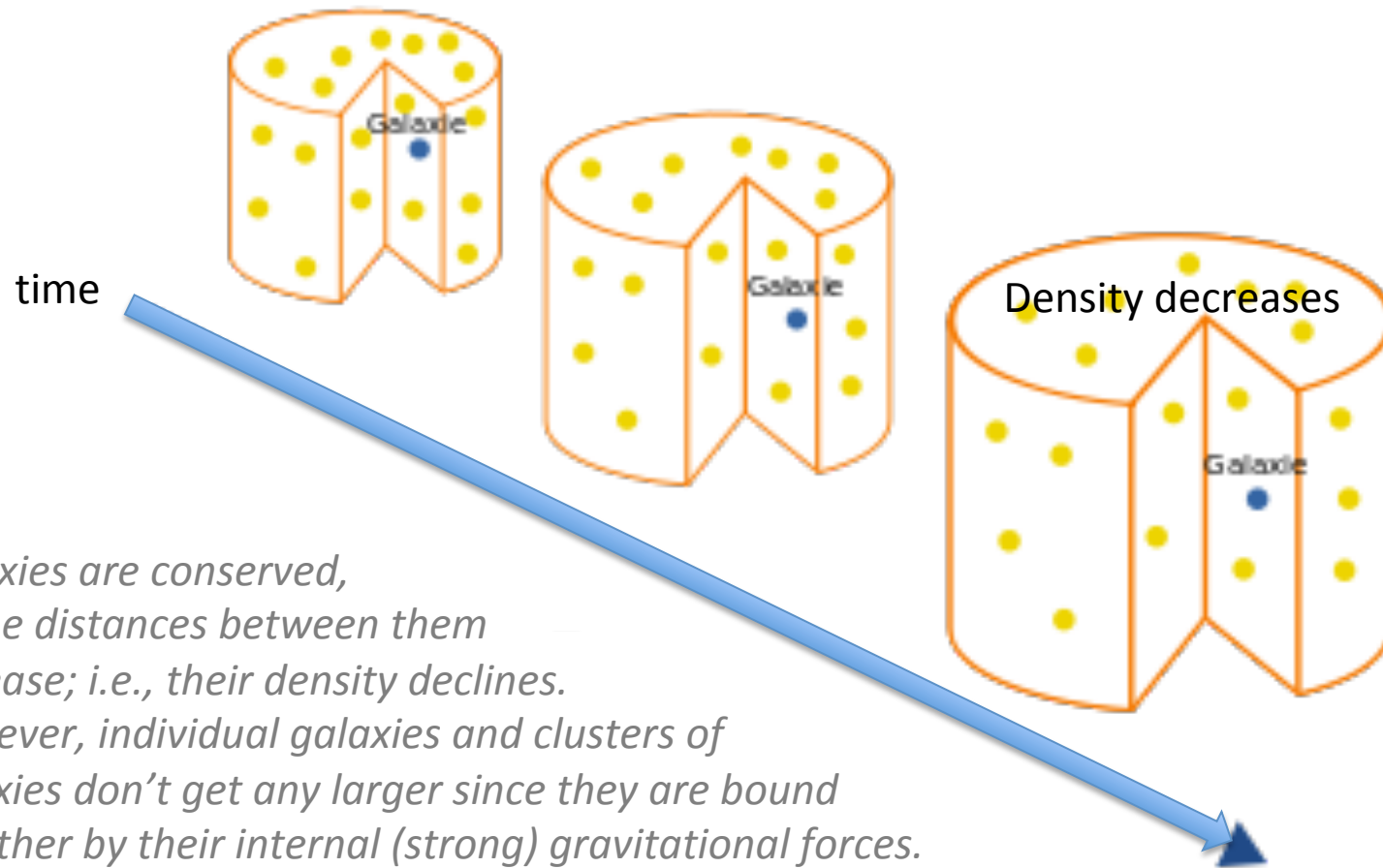


Hubble correlated the Doppler shifts and distances of galaxies

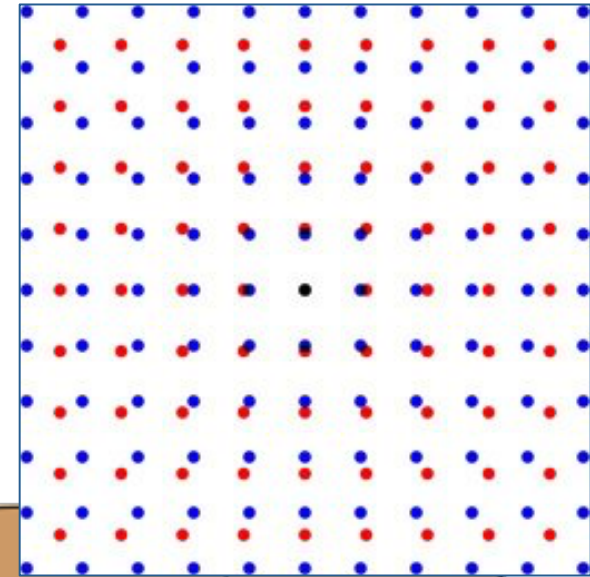
FIGURE 1  
Distance from Milky Way

*Hubble's distances,  
Slipher's Doppler shifts,  
Humason's observing skills  
Hubble presents the "Hubble Diagram"*

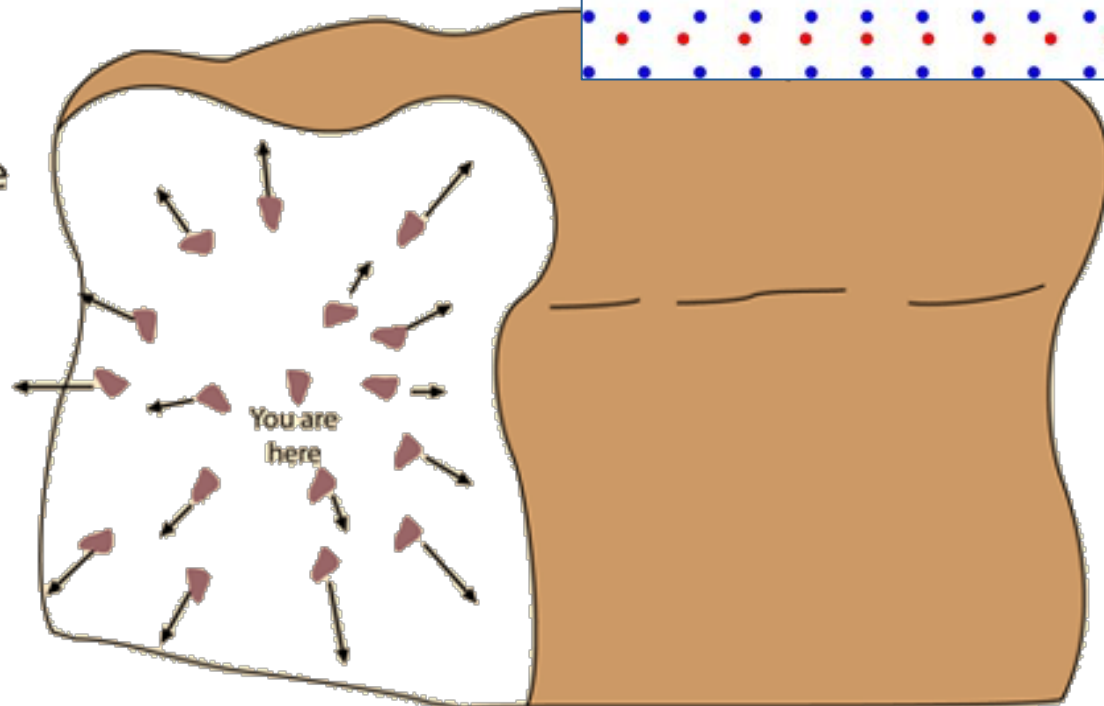
# If our view is universal then the entire Universe is expanding (with no center)!

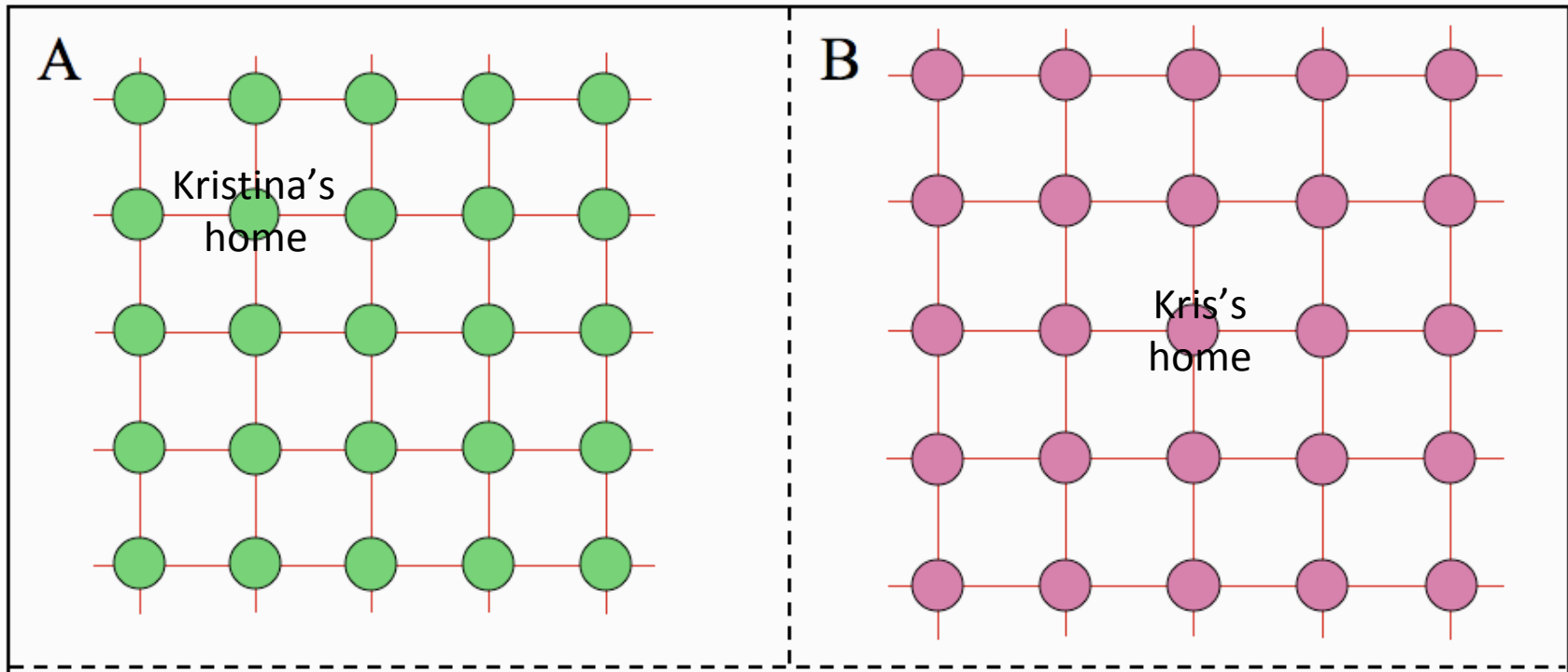


# Examples of things in an expanding space



You are sitting on one raisin in the center of a rising loaf of raisin bread. You see every other raisin receding from you, and those further away are receding faster.



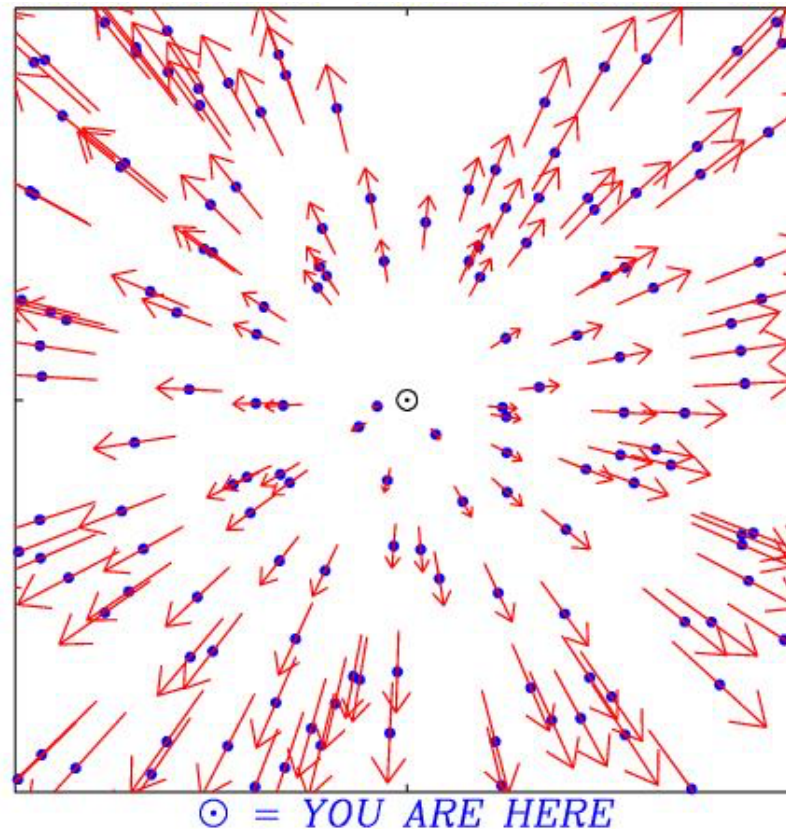


time 1

time 1 + 20%

Does expansion  
define the center  
of space?

# Hubble estimates the age of the Universe



Play it backwards!

Any (every) pair of galaxies collide at time (separation)/(recession speed)

All pairs of galaxies collide at a universal “Hubble time” = ~~X~~ Gy ago

# Roadmap

- Density is Destiny: How can the density be measured?
- Sandage searches for signs of early gravitational deceleration. No luck.
- Measuring Galaxy Masses: it's Easy!
  - (if you know the distance)
- What's the Matter? We can feel it, but we can't see it.
  - Skip ahead to **Chapter 6**: DARK MATTER — esp. page 193-201
- Dark Matter in the Milky Way and other galaxies
- Observational 'Proof' of Dark Matter: Gravitational Lenses

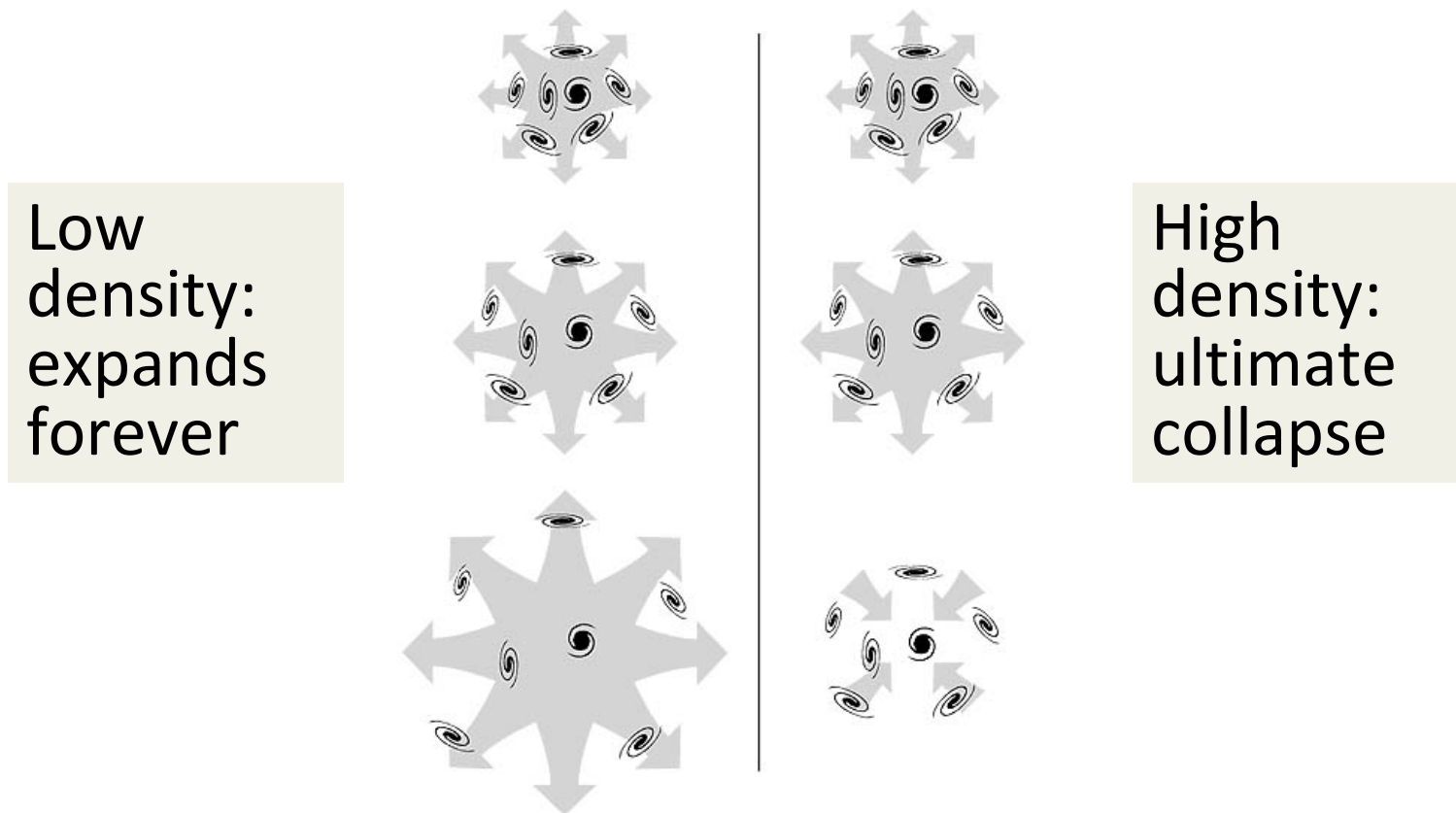


# Cosmic Expansion: Can Gravity Slow it Down?

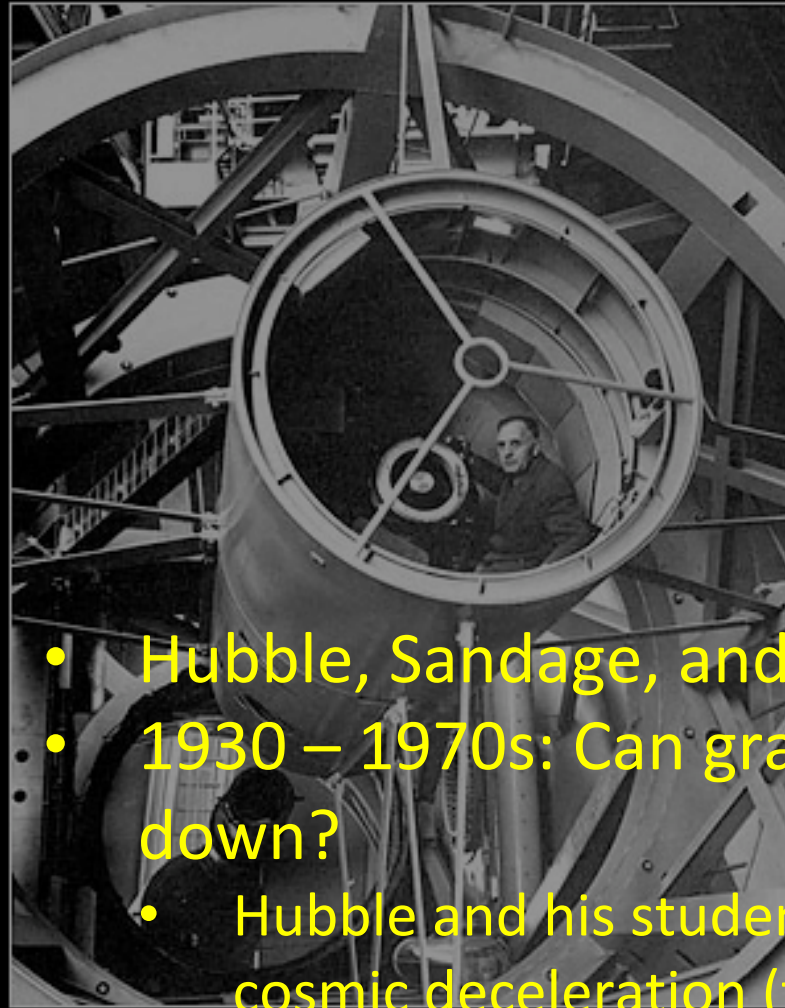


# What is the fate of the cosmos ?

*Its gravity (**aka mass density**) determines the gravitational fate of the Universe*



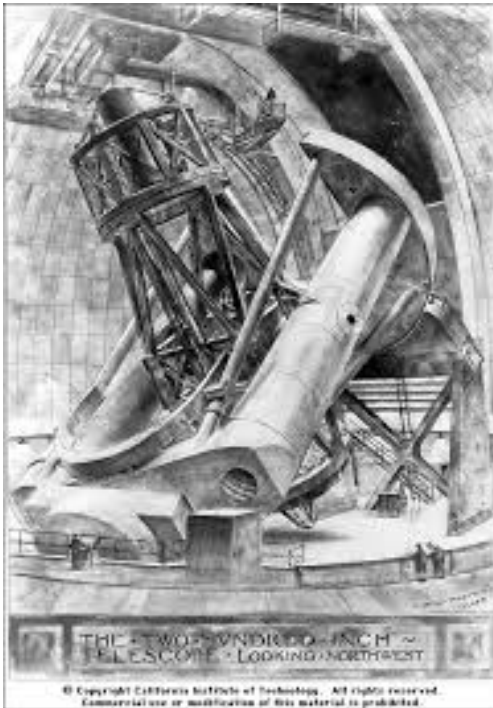
**No theory predicts the mass density.**



- Hubble, Sandage, and Collaborators
- 1930 – 1970s: Can gravity slow the expansion down?
  - Hubble and his student Alan Sandage search for cosmic deceleration (that is, curvature in the basic "Hubble Law")

*Edwin Hubble et les telescopes du Mont Palomar ...*

1950s to 1980s  
Sandage and others use the 200-inch telescope to extend Hubble's correlation plot to thousands of faint galaxies



Palomar 200-inch Telescope

