Today:
- MPI concepts
- Communicators, broadcast, reduce

Next week:
- MPI send and receive
- Iterative methods

Read: Class notes and references
$CLASSHG/codes/mpi

MPI — Message Passing Interface

OpenMP can only be used on shared memory systems with a single address space used by all threads.

Distributed memory systems require a different approach.
e.g. clusters of computers, supercomputers, heterogeneous networks.

Message Passing:
SPMD model: All processors execute same program, but with different data.
Program manages memory by placing data in processes.
Data that must be shared is explicitly sent between processes.

MPI References

See the class notes: MPI section.
There are several implementations of MPI available.
The VM has Open MPI installed, see www.open-mpi.org.
The Argonne National Lab version MPICH is also widely used.
See also the MPI Standard

Standard reference book:
Some of my slides are from Bill Gropp's tutorials
MPI — Simple example

```fortran
program test1
    use mpi
    implicit none
    integer :: ierr, numprocs, proc_num,
    call mpi_init(ierr)
    call mpi_comm_size(MPI_COMM_WORLD, numprocs, ierr)
    call mpi_comm_rank(MPI_COMM_WORLD, proc_num, ierr)
    print *, 'Hello from Process ', proc_num, ' of ', numprocs, ' processes'
    call mpi_finalize(ierr)
end program test1
```

Always need to:  use mpi,
Start with     mpi_init,
End with      mpi_finalize.

Compiling and running MPI code (Fortran)

Try this test:

```
$ cd $CLASSHG/codes/mpi
$ mpif90 test1.f90
$ mpiexec -n 4 a.out
```

You should see output like:

```
Hello from Process number 1 of 4 processes
Hello from Process number 3 of 4 processes
Hello from Process number 0 of 4 processes
Hello from Process number 2 of 4 processes
```

Note: Number of processors is specified with mpiexec.

MPI Communicators

All communication takes place in *groups of processes.*

Communication takes place in some *context.*

A group and a context are combined in a *communicator.*

**MPI_COMM_WORLD** is a communicator provided by default that includes all *processors.*

**MPI_COMM_SIZE**(comm, numprocs, ierr) returns the number of *processors* in communicator comm.

**MPI_COMM_RANK**(comm, proc_num, ierr) returns the rank of this processor in communicator comm.
mpi module

The mpi module includes:

Subroutines such as mpi_init, mpi_comm_size, mpi_comm_rank, ...

Global variables such as
  MPI_COMM_WORLD: a communicator,
  MPI_INTEGER: used to specify the type of data being sent
  MPI_SUM: used to specify a type of reduction

Remember: Fortran is case insensitive:
  mpi_init is the same as MPI_INIT.

MPI functions

There are 125 MPI functions.
Can write many program with these 8:
  • MPI_INIT(ierr) Initialize
  • MPI_FINALIZE(ierr) Finalize
  • MPI_COMM_SIZE(...) Number of processors
  • MPI_COMM_RANK(...) Rank of this processor
  • MPI_SEND(...) Send a message
  • MPI_RCV(...) Receive a message
  • MPI_BCAST(...) Broadcast to other processors
  • MPI_REDUCE(...) Reduction operation

Example: Approximate \( \pi \)

Use

\[
\pi = 4 \int_{0}^{1} \frac{1}{1 + x^2} \, dx \\
\approx 4 \Delta x \sum_{i=1}^{n} \frac{1}{1 + x_i^2} \tag{midpoint rule}
\]

where \( \Delta x = 1/n \) and \( x_i = (i - 1/2) \Delta x \).

Fortran:

```
dx = 1.d0 / n 
pisum = 0.d0 
do i=1,n 
  x = (i-0.5d0) * dx 
pisum = pisum + 1.d0 / (1.d0 + x**2)
enddo 
pi = 4.d0 * dx * pisum
```
Approximate $\pi$ using OpenMP parallel do

\begin{verbatim}
dx = 1.d0 / n
pisum = 0.d0
!$omp parallel do reduction(+: pisum) &
!$omp private(x)
do i=1,n
 x = (i-0.5d0) * dx
   pisum = pisum + 1.d0 / (1.d0 + x**2)
enddo
pi = 4.d0 * dx * pisum
\end{verbatim}

Approximate $\pi$ using OpenMP — parallel chunks

\begin{verbatim}
points_per_thread = (n + nthreads - 1) / nthreadspisum = 0.d0
!$omp parallel private(i,pisum_thread, &
!$omp istart,iend,thread_num)
!$ thread_num = omp_get_thread_num()
istart = thread_num * points_per_thread + 1iend = min((thread_num+1) * points_per_thread, n)
pisum_thread = 0.d0do i=istart,iendx = (i-0.5d0)*dxpisum_thread = pisum_thread + &1.d0 / (1.d0 + x**2)enddo
!$omp critical
   pisum = pisum + pisum_thread
!$omp end critical
!$omp end parallel
pi = 4.d0 * dx * pisum
\end{verbatim}

Approximate $\pi$ using MPI

\begin{verbatim}
call MPI_INIT(ierr)
call MPI_COMM_RANK(MPI_COMM_WORLD, proc_num, ierr)
if (proc_num == 0) n = 1000
! Broadcast to all processes:
call MPI_BCAST(n, 1, MPI_INTEGER, 0, &MPI_COMM_WORLD, ierr)
dx = 1.d0/n
points_per_proc = (n + numprocs - 1)/numprocsistart = proc_num * points_per_proc + 1iend = min((proc_num + 1) * points_per_proc, n)
pisum_proc = 0.d0do i=istart,iendx = (i-0.5d0)*dxpisum_proc = pisum_proc + 1.d0 / (1.d0 + x**2)enddo
call MPI_REDUCE(pisum_proc,pisum,1, &MPI_DOUBLE_PRECISION,MPI_SUM,0, &MPI_COMM_WORLD,ierr)
if (proc_num == 0) then
  pi = 4.d0 * dx * pisum
endif
\end{verbatim}
MPI Broadcast

Broadcast a value from Process root to all other processes.

General form:

call MPI_BCAST(start, count, &
datatype, root, &
comm, ierr)

where:
- **start**: starting address (variable, array element)
- **count**: number of elements to broadcast
- **datatype**: type of each element
- **root**: process doing the broadcast
- **comm**: communicator

**Notes:**

- R.J. LeVeque, University of Washington
- AMath 483/583, Lecture 18, May 6, 2011

MPI Broadcast Examples

call MPI_BCAST(start, count, &
datatype, root, &
comm, ierr)

Broadcast 1 double precision value:

call MPI_BCAST(x, 1, &
MPI_DOUBLE_PRECISION, 0, &
MPI_COMM_WORLD, ierr)

Broadcast jth column of a matrix (contiguous in memory):

```fortran
real(kind=8), dimension(nrows, ncols) :: a
... call MPI_BCAST(a(1,j), nrows, &
MPI_DOUBLE_PRECISION, 0, &
MPI_COMM_WORLD, ierr)
```

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Broadcast ith row of a matrix (not contiguous!):

```fortran
real(kind=8), dimension(nrows, ncols) :: a
real(kind=8), dimension(ncols) :: buffer
... do j=1,ncols
    buffer(j) = a(i,j)
  enddo

  call MPI_BCAST(buffer, ncols, &
MPI_DOUBLE_PRECISION, 0, &
MPI_COMM_WORLD, ierr)
```

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### MPI Reduce

Collect values from all processes and reduce to a scalar.

**General form:**

```fortran
    call MPI_REDUCE(sendbuf, recvbuf, count, &
       datatype, op, root, &
       comm, ierr)
```

where:
- `sendbuf`: source address
- `recvbuf`: result address
- `count`: number of elements to send / receive
- `datatype`: type of each element
- `op`: reduction operation
- `root`: process receiving and reducing
- `comm`: communicator

**A few possible reduction operations `op`:**
- `MPI_SUM`: add together
- `MPI_PROD`: multiply together
- `MPI_MAX`: take maximum
- `MPI_MIN`: take minimum
- `MPI_LAND`: logical and
- `MPI_LOR`: logical or

**Examples:** Compute $\|x\|_\infty = \max_i |x_i|$ for a distributed vector:

```fortran
    xnorm_proc = 0.d0
    do i=istart,iend
        xnorm_proc = max(xnorm_proc, abs(x(i)))
    enddo
    call MPI_REDUCE(xnorm_proc, xnorm, 1, &
       MPI_DOUBLE_PRECISION, MPI_MAX, 0, &
       MPI_COMM_WORLD, ierr)
    if (proc_num == 0) print "norm of x = ", xnorm
```

**Note:** Do not need an `MPI_BARRIER` before or after the `Reduce`.

Processors do not exit from `MPI_REDUCE` until all have called the subroutine.
MPI Reduce

This code is wrong:

```fortran
if (proc_num /= 0) then
    call MPI_REDUCE(xnorm_proc, xnorm, 1, &
    MPI_DOUBLE_PRECISION,MPI_SUM,0, &
    MPI_COMM_WORLD,ierr)
    print "Done with Reduce: ", proc_num
endif
if (proc_num == 0) print "norm of x = ", xnorm
```

With more than one process, the Reduce statement is called by all but one.

None of them will ever print the “Done with Reduce” statement or continue to run. (Code hangs.)

If only processors 1, 2, ... should participate in Reduce, need a different communicator than MPI_COMM_WORLD.

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MPI Reduce for vectors

Compute: \[ \|A\|_1 = \max_{1 \leq j \leq n} \sum_{i=1}^{m} |a_{ij}| \] for an \( m \times n \) matrix \( A \).

Suppose there are \( m \) processes and the \( i \)th process has a vector \( arow(1:n) \) containing the \( i \)th row of \( A \).

Sum the row vectors (using Reduce) and then take maximum of resulting vector...

```fortran
real(kind=8) :: arow(n), arow_abs(n), colsum(n)
    arow_abs = abs(arow)
    call MPI_REDUCE(arow_abs(1), colsum, n, &
    MPI_DOUBLE_PRECISION,MPI_SUM,0, &
    MPI_COMM_WORLD,ierr)
if (proc_num == 0) then
    anorm = 0.d0
    do j=1,n
        anorm = max(anorm, colsum(j))
    enddo
    print "1-norm of A = ", anorm
endif
```

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Notes:

R.J. LeVeque, University of Washington  AMath 483/583, Lecture 18, May 6, 2011