Today:
- OpenMP

Friday:
- More OpenMP

Read: Class notes and references

Homework 4 is posted, due next Thursday.

Memory stack

Note: Parallel threads use stack and you may need to increase the limit (e.g. on the VM):

```
$ gfortran -fopenmp yeval.f90
$ ./a.out
Segmentation fault

$ ulimit -s
8192

$ ulimit -s unlimited

$ ./a.out
Using OpenMP with 2 threads
Filled vector y of length 10000000
```

OpenMP compiler directives

Uses compiler directives that start with !$ (pragmas in C.) These look like comments to standard Fortran but are recognized when compiled with the flag `-fopenmp`.

OpenMP statements:

Ordinary Fortran statements conditionally compiled:

```
!$ print *, "Compiled with -fopenmp"
```

OpenMP compiler directives, e.g.

```
!$omp parallel do
```

Calls to OpenMP library routines:

```
use omp_lib ! need this module
!$ call omp_set_num_threads(2)
```

Memory: Heap and Stack

Memory devoted to data for a program is generally split up:

**Heap**: Dynamically allocated memory — memory allocator looks for free block of memory, keeps track of free list, does garbage collection, etc.

**Stack**: Block of memory where space is allocated on “top” of the stack as needed and “popped” off the stack when no longer needed. Last in — first out (LIFO).

Fast relative to heap allocation.

Natural way to allocate storage for nested subroutine or function calls: If A calls B calls C, then when the variables used by C are popped off the stack, we’re back to the variables of B.

Private variables for threads also put on stack, popped off when parallel block ends.
OpenMP test code

```fortran
program test
    use omp_lib
    integer :: thread_num

    ! Specify number of threads to use:
    !$ call omp_set_num_threads(2)

    print *, "Testing openmp ..."

    !$omp parallel
    !$omp critical
    thread_num = omp_get_thread_num()
    !$ print *, "This thread = ", thread_num
    !$omp end critical
    !$omp end parallel
end program test
```

Could change to add a `private` clause:

```fortran
!$omp parallel private(thread_num)
!
thread_num = omp_get_thread_num()
!
$ print *, "This thread = ", thread_num
!$omp end critical
!$omp end parallel
```

Then each thread has its own version of the `thread_num` variable.

OpenMP parallel do loops

```fortran
!$omp parallel do
    do i=1,n
        ! do stuff for each i
    enddo
!
!$omp end parallel do    ! OPTIONAL
```

indicates that the do loop can be done in parallel.

**Requires:**

- what's done for each value of `i` is independent of others
- Different values of `i` can be done in any order.

The iteration variable `i` is `private` to the thread: each thread has its own version.

By default, all other variables are `shared` between threads unless specified otherwise.

This code fills a vector `y` with function values that take a bit of time to compute:

```fortran
dx = 1.d0 / (n+1.d0)

!$omp parallel do private(x)
    do i=1,n
        x = i*dx
        y(i) = exp(x)*cos(x)*sin(x)*sqrt(5*x+6.d0)
    enddo
!
```

Elapsed time for `n = 10^8`, without OpenMP: about 9.3 sec.

Elapsed time using OpenMP on 2 processors: about 5.0 sec.
This code is not correct:

```fortran
!$omp parallel do
do i=1,n
  x = i*dx
  y(i) = exp(x)*cos(x)*sin(x)*sqrt(5*x+6.d0)
enddo
```

By default, \( x \) is a shared variable.

Might happen that:
- Processor 0 sets \( x \) properly for one value of \( i \),
- Processor 1 sets \( x \) properly for another value of \( i \),
- Processor 0 uses \( x \) but is now incorrect.

Correct version:

```fortran
!$omp parallel do private(x)
do i=1,n
  x = i*dx
  y(i) = exp(x)*cos(x)*sin(x)*sqrt(5*x+6.d0)
enddo
```

Now each thread has its own version of \( x \).

Iteration counter \( i \) is private by default.

Note that \( dx, n, y \) are shared by default.

\( dx, n \) are used but not changed,
\( y \) is changed, but independently for each \( i \)

Incorrect code:

```fortran
dx = 1.d0 / (n+1.d0)
!$omp parallel do private(x,dx)
do i=1,n
  x = i*dx
  y(i) = exp(x)*cos(x)*sin(x)*sqrt(5*x+6.d0)
enddo
```

Specifying \( dx \) private won’t work here.

This will create a private variable \( dx \) for each thread but it will be uninitialized.

Will run but give garbage.

Could fix with:

```fortran
dx = 1.d0 / (n+1.d0)
!$omp parallel do firstprivate(dx)
do i=1,n
  x = i*dx
  y(i) = exp(x)*cos(x)*sin(x)*sqrt(5*x+6.d0)
enddo
```

The firstprivate clause creates private variables and initializes to the value from the master thread prior to the loop.

There is also a lastprivate clause to indicate that the last value computed by a thread (for \( i = n \)) should be copied to the master thread’s copy for continued execution.
OpenMP parallel do loops

! from $CLASSHG/codes/openmp/private1.f90

n = 7
y = 2.d0
!$omp parallel do firstprivate(y) lastprivate(y)
do i=1,n
  y = y + 10.d0
  x(i) = y
!omp critical
    print *, "i = ",i," x(i) = ",x(i)
!omp end critical
enddo
print *, "At end, y = ",y

might produce:
i = 1  x(i) = 12.0000000000000
i = 5  x(i) = 12.0000000000000
i = 2  x(i) = 22.0000000000000
i = 6  x(i) = 22.0000000000000
i = 3  x(i) = 32.0000000000000
i = 7  x(i) = 32.0000000000000
i = 4  x(i) = 42.0000000000000
At end, y = 32.0000000000000

Order might be different but final y will be from i = 7.

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AMath 483/583, Lecture 14, April 27, 2011

OpenMP parallel do loops — changing default

Default is that loop iterator is private, other variables shared.
Can change this, e.g.

!$omp parallel do default(private) shared(x,z) &
!$omp firstprivate(y) lastprivate(y)
do i=1,n
  x(i) = y
!omp critical
    print *, "i = ",i," x(i) = ",x(i)
!omp end critical
enddo
print *, "At end, y = ",y

With this change, only x and z are shared.
Note continuation character & and continuation line.

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OpenMP synchronization

!$omp parallel do
    do i=1,n
        ! do stuff for each i
    enddo
!$omp end parallel do ! OPTIONAL

! master thread continues execution

There is an implicit barrier at the end of the loop.
The master thread will not continue until all threads have finished with their subset of 1, 2, ..., n.

Except if ended by:
    !$omp end parallel do nowait

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Conditional clause

Loop overhead may not be worthwhile for short loops.
(Multi-thread version may run slower than sequential)

Can use conditional clause:

$omp parallel do if (n > 1000)
do i=1,n
    ! do stuff
  enddo

If n ≤ 1000 then no threads are created, master thread executes loop sequentially.

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Nested loops

!$omp parallel do private(i)
do j=1,m
   do i=1,n
      a(i,j) = 0.d0
   enddo
enddo

The loop on j is split up between threads.

The thread handling j=1 does the entire loop on i, sets a(1,1), a(2,1), ..., a(n,1).

Note: The loop iterator i must be declared private!

j is private by default, i is shared by default.

Which is better? (assume \( m \approx n \))

!$omp parallel do private(i)
do j=1,m
   do i=1,n
      a(i,j) = 0.d0
   enddo
enddo

or

do j=1,m
   !$omp parallel do
      do i=1,n
         a(i,j) = 0.d0
      enddo
enddo

The first has less overhead: Threads created only once.

The second has more overhead: Threads created \( m \) times.

Regressions

Incorrect code for computing \( \|x\|_1 = \sum_i |x_i| \):

\[
\text{norm} = 0.d0
\]

!$omp parallel do
   do i=1,n
      \text{norm} = \text{norm} + \text{abs}(x(i))
   enddo

There is a race condition: each thread is updating same shared variable norm.

Correct code:

!$omp parallel do reduction(+ : norm)
doi=1,n
   \text{norm} = \text{norm} + \text{abs}(x(i))
enddo

A reduction reduces an array of numbers to a single value.

But have to make sure loop can be parallelized!

Incorrect code for replicating first column:

!$omp parallel do private(j)
do i=2,n
   do j=1,m
      a(i,j) = a(i-1,j)
   enddo
enddo

Corrected: \( j \)'s can be done in any order, \( i \)'s cannot

!$omp parallel do private(i)
do j=1,m
   do i=2,n
      a(i,j) = a(i-1,j)
   enddo
enddo

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A more complicated way to do this:

```fortran
norm = 0.d0
!$omp parallel private(mysum) shared(norm)
mysum = 0
!$omp do
do i=1,n
  mysum = mysum + abs(x(i))
enddo

!$omp critical
norm = norm + mysum
!$omp end critical
!$omp end parallel
```

Some other reductions

Can do reductions using +, −, ∗, min, max, .and., .or., some others

**General form:**

```fortran
!$omp parallel do reduction(operator : list)
```

**Example with max:**

```fortran
y = -1.d300 ! very negative value
!$omp parallel do reduction(max: y)
do i=1,n
  y = max(y, x(i))
enddo
print *, 'max of x = ', y
```

**Example with .or.**

```fortran
logical anyzero
! set x...
anyzero = .false.

!$omp parallel do reduction(.or.: anyzero)
do i=1,n
  anyzero = anyzero .or. (x(i) == 0.d0)
enddo
print *, 'anyzero = ', anyzero
```

Prints T if any \( x(i) \) is zero, F otherwise.