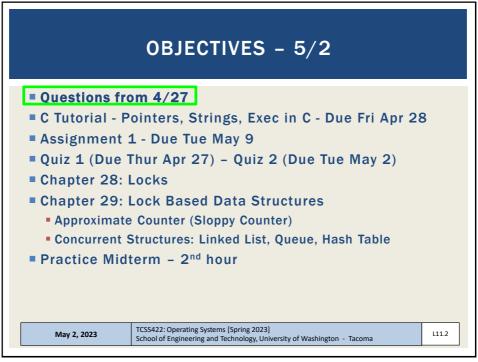
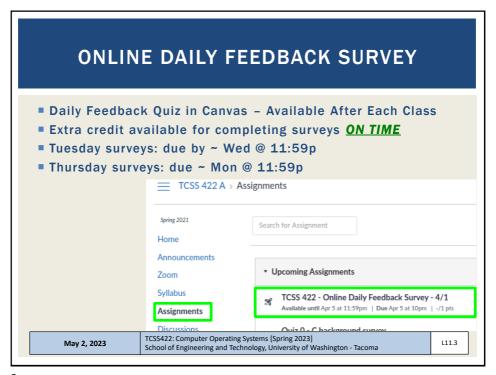
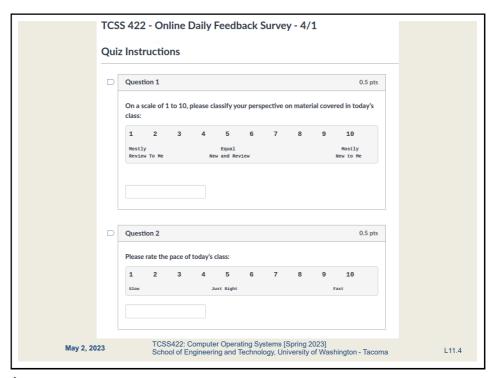


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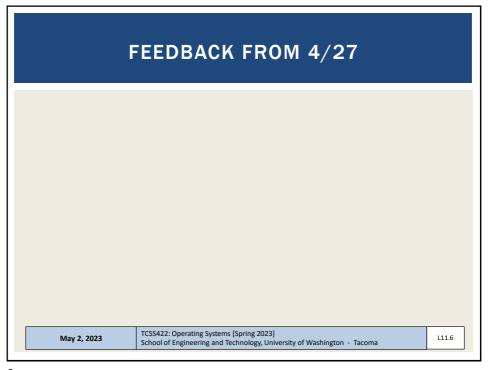






MATERIAL / PACE Please classify your perspective on material covered in today's class (43 respondents): 1-mostly review, 5-equal new/review, 10-mostly new Average - 6.98 (↓ - previous 7.30) Please rate the pace of today's class: 1-slow, 5-just right, 10-fast Average - 6.07 (↑ - previous 5.70)

5



OBJECTIVES - 5/2 Questions from 4/27 C Tutorial - Pointers, Strings, Exec in C - Due Fri Apr 28 Assignment 1 - Due Tue May 9 Quiz 1 (Due Thur Apr 27) - Quiz 2 (Due Tue May 2) Chapter 28: Locks Chapter 29: Lock Based Data Structures Approximate Counter (Sloppy Counter) Concurrent Structures: Linked List, Queue, Hash Table Practice Midterm - 2nd hour

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OBJECTIVES - 5/2 Questions from 4/27 C Tutorial - Pointers, Strings, Exec in C - Due Fri Apr 28 Assignment 1 - Due Tue May 9 Quiz 1 (Due Thur Apr 27) - Quiz 2 (Due Tue May 2) Chapter 28: Locks Chapter 29: Lock Based Data Structures Approximate Counter (Sloppy Counter) Concurrent Structures: Linked List, Queue, Hash Table Practice Midterm - 2nd hour

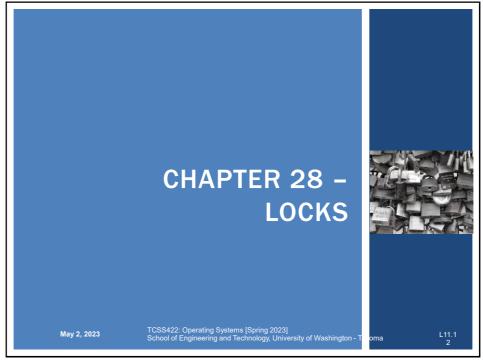
OBJECTIVES - 5/2 Questions from 4/27 C Tutorial - Pointers, Strings, Exec in C - Due Fri Apr 28 Assignment 1 - Due Tue May 9 Quiz 1 (Due Thur Apr 27) - Quiz 2 (Due Tue May 2) Chapter 28: Locks Chapter 29: Lock Based Data Structures Approximate Counter (Sloppy Counter) Concurrent Structures: Linked List, Queue, Hash Table Practice Midterm - 2nd hour

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QUIZ 2 Canvas Quiz - Practice CPU Scheduling Problems Posted in Canvas Unlimited attempts permitted Provides CPU scheduling practice problems FIFO, SJF, STCF, RR, MLFQ (Ch. 7 & 8) Multiple choice and fill-in the blank Quiz automatically scored by Canvas Please report any grading problems Due Tuesday May 2nd at 11:59pm Link: https://canvas.uw.edu/courses/1642522/assignments/8316759 May 2, 2023 TCSS422: Operating Systems (Spring 2023) School of Engineering and Technology, University of Washington - Tacoma

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"LOCK BUILDING" CPU INSTRUCTIONS ON ARM PROCESSORS

- Two instructions used together to support synchronization on RISC systems
- These instructions are not on x86 processors
- They are on RISC CPUs: Alpha, PowerPC, ARM
- Load-linked (LL)
 - Loads value into register
 - Same as typical load
 - Used as a mechanism to track competition
- Store-conditional (SC)
 - Performs "mutually exclusive" store
 - Allows only one thread to store value

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L11.13

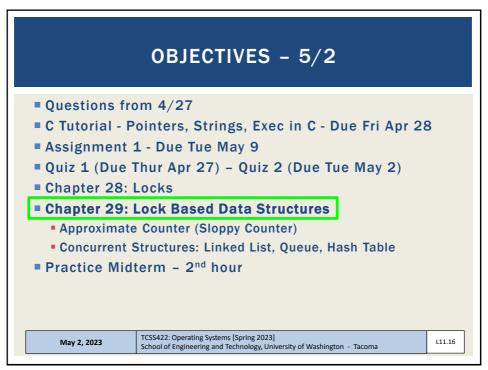
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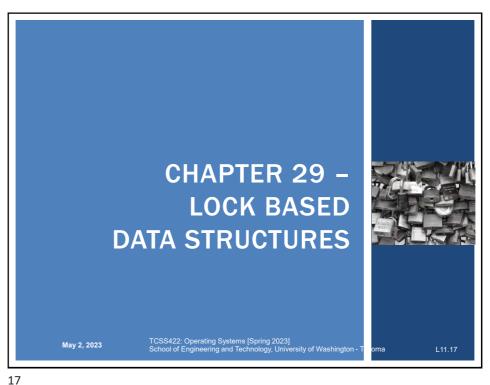
LL/SC LOCK

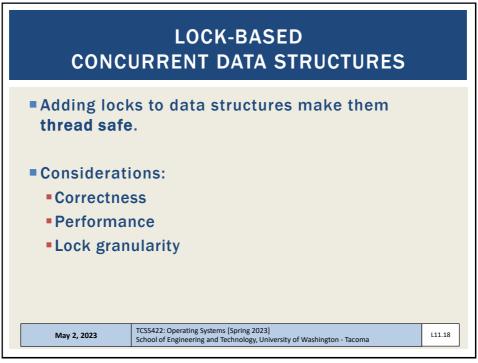
- LL instruction loads pointer value (ptr)
- SC only stores if the load link pointer has not changed
- Requires HW support
 - C code is psuedo code

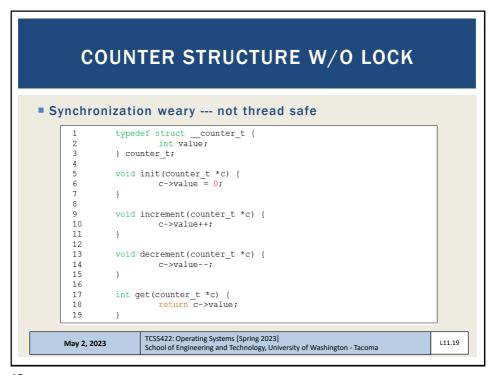
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```
LL/SC LOCK - 2
       void lock(lock t *lock) {
           while (1) {
                    while (LoadLinked(&lock->flag) == 1)
                             ; // spin until it's zero
                    if (StoreConditional(&lock->flag, 1) == 1)
                        return; // if set-it-to-1 was a success: all done
                                     otherwise: try it all over again
   10
   11 void unlock(lock_t *lock) {
   12
           lock -> flag = 0;
   13 }
Provides a two instruction lock
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```

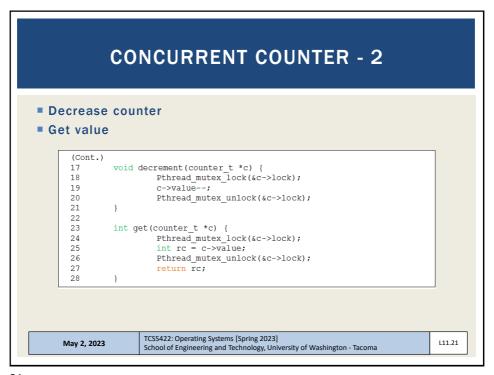


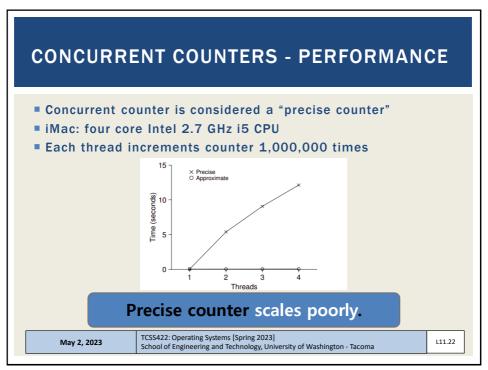






```
CONCURRENT COUNTER
               typedef struct __counter_t {
                       int value;
      3
                       pthread lock t lock;
              } counter_t;
               void init(counter_t *c) {
                       c->value = 0;
      8
                       Pthread_mutex_init(&c->lock, NULL);
      10
             void increment(counter_t *c) {
               Pthread_mutex_lock(&c->lock);
      13
                       c->value++;
      14
                       Pthread_mutex_unlock(&c->lock);
      15
Add lock to the counter
Require lock to change data
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                                                                                  L11.20
```





PERFECT SCALING Achieve (N) performance gain with (N) additional resources Throughput: Transactions per second (tps) 1 core N = 100 tps 10 cores (x10) N = 1000 tps (x10) Is parallel counting with a shared counter an embarrassingly parallel problem? May 2, 2023 TCSS422: Operating Systems [Spring 2023] School of Engineering and Technology, University of Washington - Tacoma

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APPROXIMATE (SLOPPY) COUNTER

- Provides single logical shared counter
 - Implemented using local counters for each ~CPU core
 - 4 CPU cores = 4 local counters & 1 global counter
 - Local counters are synchronized via local locks
 - Global counter is updated periodically
 - Global counter has lock to protect global counter value
 - Update threshold (S) referred to as sloppiness threshold: How often to push local values to global counter
 - Small (S): more updates, more overhead
 - Large (S): fewer updates, more performant, less synchronized
- Why this implementation?

Why do we want counters local to each CPU Core?

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L11.25

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APPROXIMATE COUNTER - MAIN POINTS

- Idea of the Approximate Counter is to <u>RELAX</u> the synchronization requirement for counting
 - Instead of synchronizing global count variable each time: counter=counter+1
 - Synchronization occurs only every so often:
 e.g. every 1000 counts
- Relaxing the synchronization requirement <u>drastically</u> reduces locking API overhead by trading-off split-second accuracy of the counter
- Approximate counter: trade-off accuracy for speed
 - It's approximate because it's not so accurate (until the end)

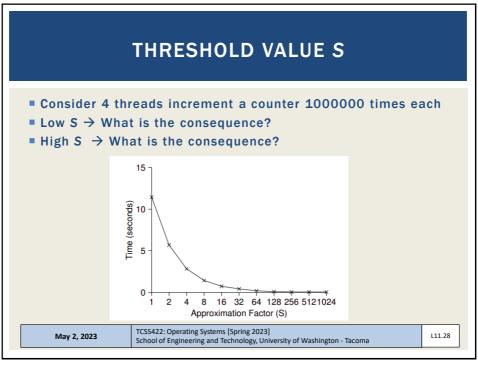
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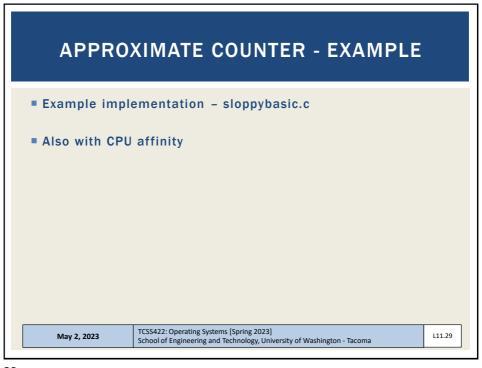
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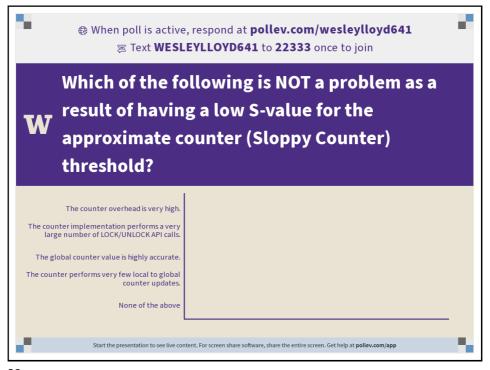
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L11.26

APPROXIMATE COUNTER - 2 ■ Update threshold (S) = 5 Synchronized across four CPU cores ■ Threads update local CPU counters Time $\mathbf{L_1}$ L_3 G L_4 $5 \rightarrow 0$ 5 (from L_1) $5 \rightarrow 0$ 10 (from L_4) TCSS422: Operating Systems [Spring 2023] May 2, 2023 School of Engineering and Technology, University of Washington - Tacoma







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CONCURRENT LINKED LIST - 1 Simplification - only basic list operations shown Structs and initialization: // basic node structure typedef struct __node_t { int key; 3 struct __node_t *next; } node_t; // basic list struct typedef struct _ list_t { node_t *head; red mutex t : // basic list structure (one used per list) 8 9 10 pthread_mutex_t lock; } list_t; 12 13 void List Init(list t *L) { L->head = NULL; 14 pthread_mutex_init(&L->lock, NULL); 15 16 } 17 (Cont.) TCSS422: Operating Systems [Spring 2023] May 2, 2023 L11.32 School of Engineering and Technology, University of Washington - Tacoma

CONCURRENT LINKED LIST - 2 Insert - adds item to list Everything is critical! There are two unlocks 18 int List Insert(list t *L, int key) { pthread_mutex_lock(&L->lock); 19 20 node_t *new = malloc(sizeof(node_t)); if (new == NULL) { 21 perror("malloc"); 22 23 pthread_mutex_unlock(&L->lock); return -1; // fail } 24 new->key = key; new->next = L->head; 28 L->head = new; pthread mutex unlock(&L->lock); 29 30 return 0; // success 31 (Cont.) TCSS422: Operating Systems [Spring 2023] May 2, 2023 L11.33 School of Engineering and Technology, University of Washington - Tacoma

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CONCURRENT LINKED LIST - 3 Lookup - checks list for existence of item with key Once again everything is critical Note - there are also two unlocks (Cont.) 32 int List_Lookup(list_t *L, int key) { 32 33 pthread_mutex_lock(&L->lock); 34 node_t *curr = L->head; while (curr) { 35 36 if (curr->key == key) { 37 pthread mutex unlock(&L->lock); 38 return 0; // success 39 40 curr = curr->next; 41 42 pthread_mutex_unlock(&L->lock); 43 return -1; // failure 44 TCSS422: Operating Systems [Spring 2023] May 2, 2023 L11.34 School of Engineering and Technology, University of Washington - Tacoma

CONCURRENT LINKED LIST First Implementation: Lock everything inside Insert() and Lookup() If malloc() fails lock must be released Research has shown "exception-based control flow" to be error prone 40% of Linux OS bugs occur in rarely taken code paths Unlocking in an exception handler is considered a poor coding practice There is nothing specifically wrong with this example however Second Implementation ...

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CCL - SECOND IMPLEMENTATION Init and Insert void List_Init(list_t *L) { L->head = NULL; pthread_mutex_init(&L->lock, NULL); void List_Insert(list_t *L, int key) { node_t *new = malloc(sizeof(node_t)); if (new == NULL) { 10 perror("malloc"); 11 return; 12 new->key = key; 13 14 15 // just lock critical section 16 pthread_mutex_lock(&L->lock); new->next = L->head; 18 L->head = new; 19 pthread_mutex_unlock(&L->lock); 20 21 TCSS422: Operating Systems [Spring 2023] May 2, 2023 L11.36 School of Engineering and Technology, University of Washington - Tacoma

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CCL - SECOND IMPLEMENTATION - 2 Lookup (Cont.) 22 int List_Lookup(list_t *L, int key) { 23 int rv = -1; 24 pthread mutex lock(&L->lock); 25 node_t *curr = L->head; 26 while (curr) { 27 if (curr->key == key) { 28 rv = 0;29 break; 30 31 curr = curr->next; 32 pthread_mutex_unlock(&L->lock); 33 34 return rv; // now both success and failure 35 TCSS422: Operating Systems [Spring 2023] L11.37 May 2, 2023 School of Engineering and Technology, University of Washington - Tacoma

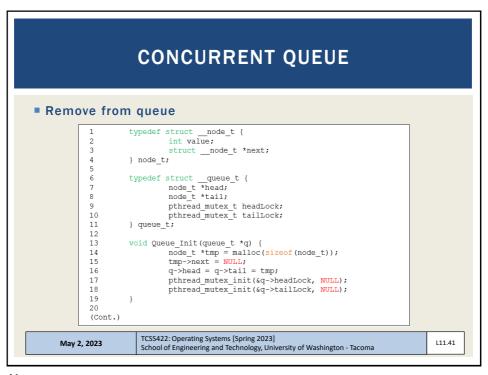
37

CONCURRENT LINKED LIST PERFORMANCE Using a single lock for entire list is not very performant Users must "wait" in line for a single lock to access/modify any item Hand-over-hand-locking (lock coupling) Introduce a lock for each node of a list Traversal involves handing over previous node's lock, acquiring the next node's lock... Improves lock granularity Degrades traversal performance Consider hybrid approach Fewer locks, but more than 1 Best lock-to-node distribution? TCSS422: Operating Systems [Spring 2023] May 2, 2023 L11.38 School of Engineering and Technology, University of Washington - Tacoma

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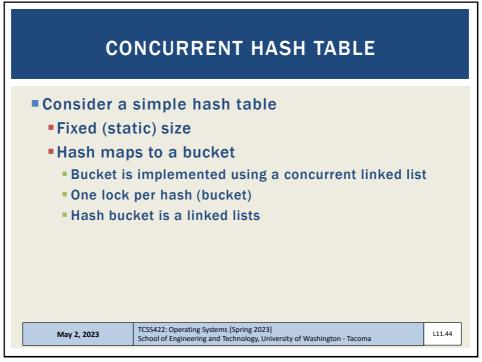
| Improvement beyond a single master lock for a queue (FIFO) | Two locks: | One for the head of the queue | One for the tall | Synchronize enqueue and dequeue operations | Add a dummy node | Allocated in the queue initialization routine | Supports separation of head and tail operations | Items can be added and removed by separate threads at the same time | May 2, 2023 | TCSS422: Operating Systems [Spring 2023] | School of Engineering and Technology, University of Washington - Tacoma | 111.40 | 111.40 |

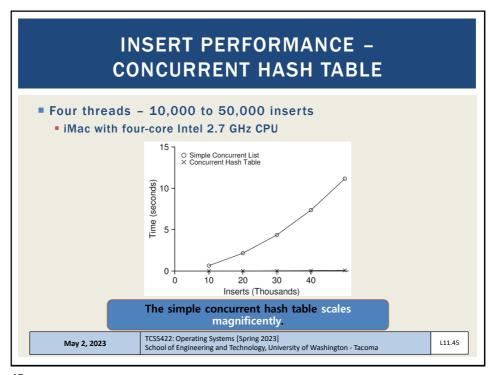


```
CONCURRENT QUEUE - 2
Add to queue
          (Cont.)
         21
                    void Queue_Enqueue(queue_t *q, int value) {
     node_t *tmp = malloc(sizeof(node_t));
         22
                              assert(tmp != NULL);
         23
         24
         25
                             tmp->value = value;
         26
                             tmp->next = NULL;
         27
         28
                             pthread mutex lock(&g->tailLock);
                             q->tail->next = tmp;
         30
                             q->tail = tmp;
         31
                             pthread_mutex_unlock(&q->tailLock);
         32
          (Cont.)
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                                                                                                L11.42
```

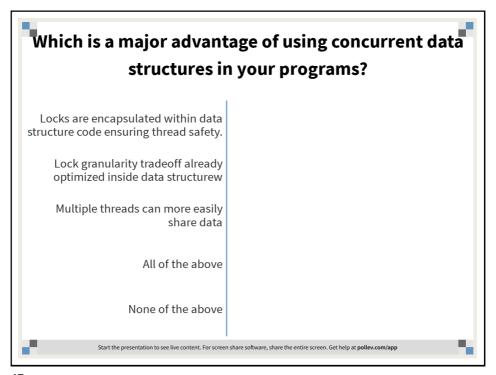
OBJECTIVES - 5/2 Questions from 4/27 C Tutorial - Pointers, Strings, Exec in C - Due Fri Apr 28 Assignment 1 - Due Tue May 9 Quiz 1 (Due Thur Apr 27) - Quiz 2 (Due Tue May 2) Chapter 28: Locks Chapter 29: Lock Based Data Structures Sloppy Counter Concurrent Structures: Linked List, Queue, Hash Table Practice Midterm - 2nd hour

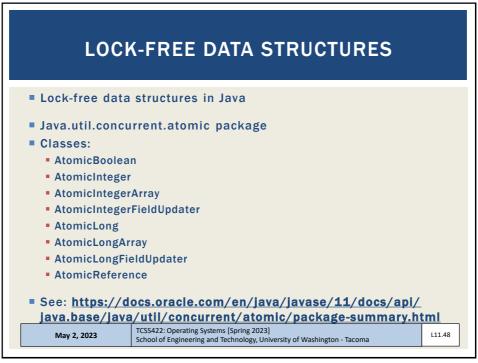
43

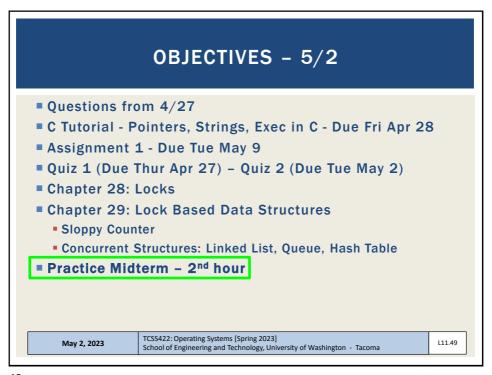




```
CONCURRENT HASH TABLE
               #define BUCKETS (101)
               typedef struct __hash_t {
    list_t lists[BUCKETS];
   3
               } hash_t;
               void Hash_Init(hash_t *H) {
                          int i;
                          for (i = 0; i < BUCKETS; i++) {</pre>
                                     List_Init(&H->lists[i]);
   11
   12
               }
   13
               int Hash_Insert(hash_t *H, int key) {
    int bucket = key % BUCKETS;
   14
   15
   16
                         return List_Insert(&H->lists[bucket], key);
   17
   18
               int Hash_Lookup(hash_t *H, int key) {
    int bucket = key % BUCKETS;
   19
   20
    21
                          return List Lookup(&H->lists[bucket], key);
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                                                                                                 L11.46
```

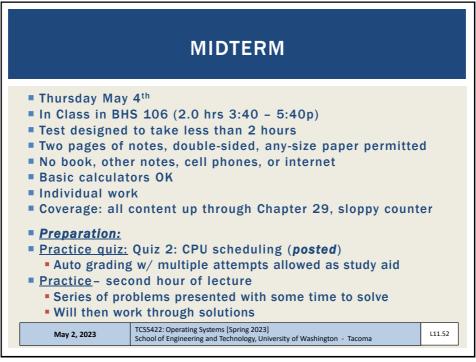


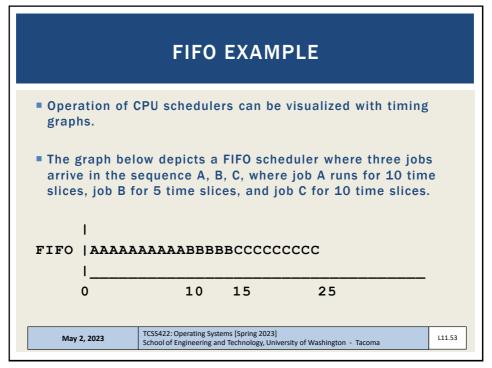


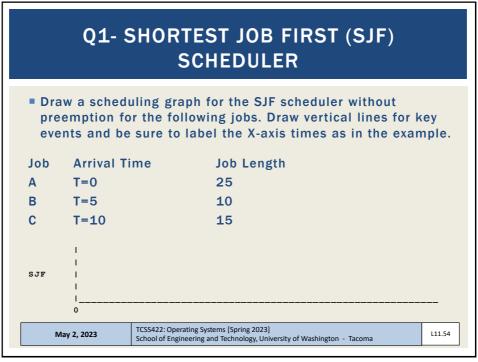












Q1 - SJF - 2				
What is the response time (RT) and turnaround time (TT) for jobs A, B, and C?				
RT Job A: TT Job A:				
RT Job B: TT Job B:				
RT Job C: TT Job C:				
What is the average response time for all jobs?				
What is the average turnaround time for all jobs?				
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Q	Q2 - SHORTEST TIME TO COMPLETION FIRST (STCF) SCHEDULER					
the fo	Draw a scheduling graph for the STCF scheduler with preemption for the following jobs. Draw vertical lines for key events and be sure to label the X-axis times as in the example.					
В	Arrival Til T=0 T=5 T=10	me Job Length 25 10 15				
СРИ	 					
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Q2 - STCF - 2				
What is the response time (RT) and turnaround time (TT) for jobs A, B, and C?				
RT Job A: TT Job A:				
RT Job B: TT Job B:				
RT Job C: TT Job C:				
■ What is the average response time for all jobs?				
■ What is the average turnaround time for all jobs?				
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Q3 -	OPERATING SYSTEM APIS			
1. Provide a definition for what is a blocking API call				
2. Provide a definition for a non-blocking API call				
3. Provide an example of a blocking API call. Consider APIs used to manage processes and/or threads.				
 Provide an example of a non-blocking API call. Consider APIs used to manage processes and/or threads. 				
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Q4 - OPERATING SYSTEM APIs - II

- 1. When implementing memory synchronization for a multi-threaded program list one advantage of combining the use of a condition variable with a lock variable via the Linux C thread API calls: pthread_mutex_lock() and pthread_cond_wait()
- 2. When implementing memory synchronization for a multi-threaded program using locks, list one disadvantage of using blocking thread API calls such as the Linux C thread API calls for: pthread_mutex_lock() and pthread_cond_wait()
- 3. List (2) factors that cause Linux blocking API calls to introduce **overhead** into programs:

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Q5 - PERFECT MULTITASKING OPERATING SYSTEM

In a perfect-multi-tasking operating system, every process of the same priority will always receive exactly $1/n^{th}$ of the available CPU time. Important CPU improvements for multi-tasking include: (1) fast context switching to enable jobs to be swapped in-and-out of the CPU very quickly, and (2) the use of a timer interrupt to preempt running jobs without the user voluntarily yielding the CPU. These innovations have enabled major improvements towards achieving a coveted "Perfect Multi-Tasking System".

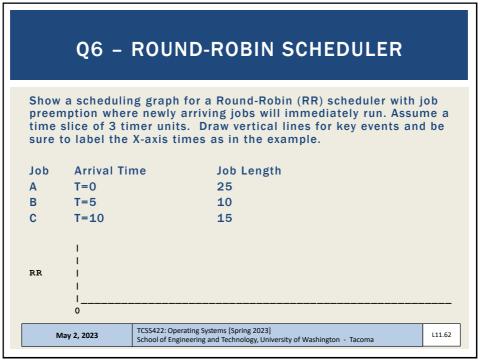
List and describe two challenges that remain complicating the full realization of a Perfect Multi-Tasking Operating System. In other words, what makes it very difficult for all jobs (for example, 10 jobs) of the same priority to receive **EXACTLY** the same runtime on the CPU? Your description must explain why the challenge is a problem for achieving perfect multi-tasking.

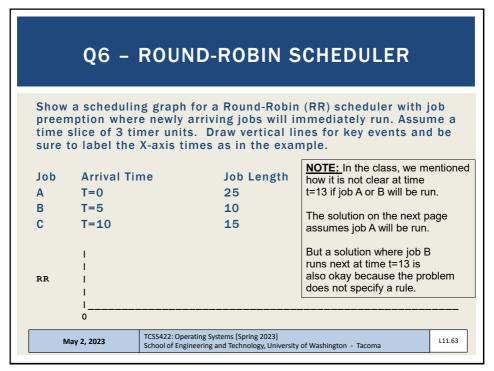
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Q6 - RR SCHEDULER - 2

Using the graph, from time t=10 until all jobs complete at t=50, evaluate Jain's Fairness Index:

Jain's fairness index is expressed as:

$$\mathcal{J}(x_1,x_2,\ldots,x_n) = rac{(\sum_{i=1}^n x_i)^2}{n \cdot \sum_{i=1}^n x_i^2}$$

Where n is the number of jobs, and x_i is the time share of each process Jain's fairness index=1 for best case fairness, and 1/n for worst case fairness.

For the time window from t=10 to t=50, what percentage of the CPU time is allocated to each of the jobs A, B, and C?

Job A: _____ Job B: ____ Job C: ____

With these values, calculate Jain's fairness index from t=10 to t=50.

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Q6 - II

$$\mathcal{J}(x_1,x_2,\ldots,x_n) = rac{(\sum_{i=1}^n x_i)^2}{n\cdot\sum_{i=1}^n x_i^2}$$

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L11.65

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Q7 - SLOPPY COUNTER

Below is a tradeoff space graph similar to those we've shown in class. Based on the sloppy counter threshold (S), add numbers on the left or right side of the graph for each of the following tradeoffs:

- 1. High number of Global Updates
- 3. High Overhead
- 5. Low number of Global Updates
- 7. Low Overhead

- 2. High Performance
- 4. High Accuracy
- 6. Low Performance
- 8. Low Accuracy

Low sloppy threshold (S)

High sloppy threshold (S)

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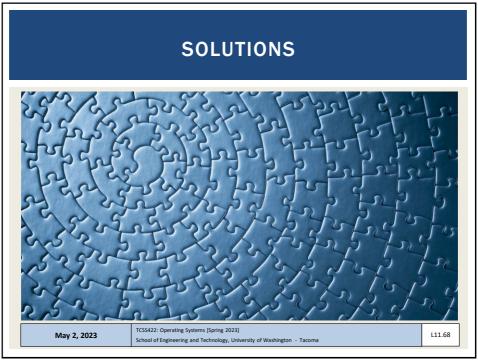
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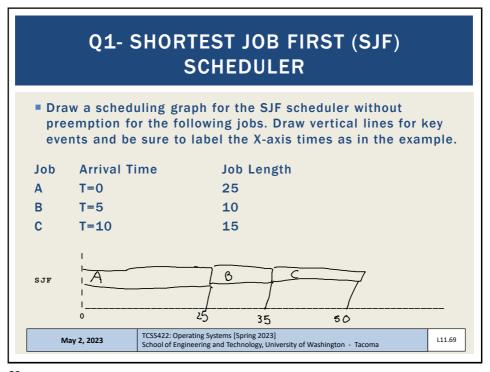
MULTI-LEVEL FEEDBACK QUEUE

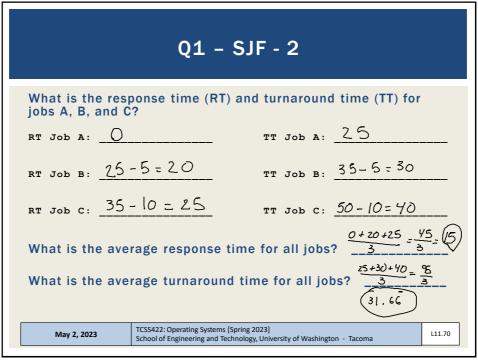
- Review the bonus lecture for scheduling examples including several Multi-level-feedback-queue problems (MLFQ)
- <u>https://tinyurl.com/4sepy582</u>

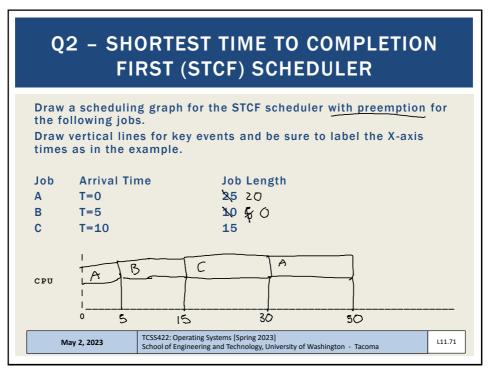
May 2, 2023

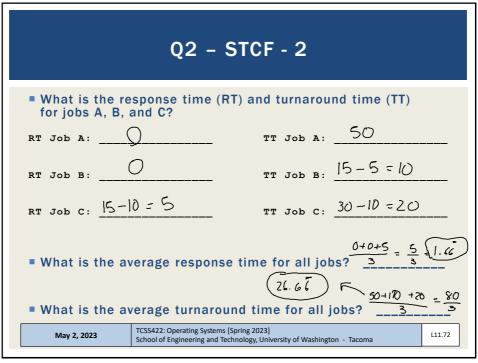
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Q3 - OPERATING SYSTEM APIS

- 1. Provide a definition for what is a blocking API call PHYRELD_MUTEX_LOCK() - PROGRAMS FREEZES AND WAITS UNTIL A RESOURCE Becomes AVAILABLE
- 2. Provide a definition for a non-blocking API call Performs It's ACTION I MMEDIA et Ly W/O WAIT
- 3. Provide an example of a blocking API call.

Consider APIs used to manage processes and/or threads. wait() pthread-cond-wait() pthread-join

4. Provide an example of a non-blocking API call.

Consider APIs used to manage processes and/or threads. pthicad_mutex_unlock() fork() execupe)

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L11.73

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Q4 - OPERATING SYSTEM APIs - II

- 1. When implementing memory synchronization for a multi-threaded program list one advantage of combining the use of a condition variable with a lock variable via the Linux C thread API calls: pthread_mutex_lock() and pthread_cond_wait() FIFO wait queve - ASOS-threads in pridrity order when WAITING
- 2. When implementing memory synchronization for a multi-threaded program using locks, list one disadvantage of using blocking thread API calls such as the Linux C thread API calls for: pthread_mutex_lock() and pthread_cond_wait() DEADLOCK CAN OCCUR which freezes the thread when the work is
- never AVAILABLE 3. List (2) factors that cause Linux blocking API calls to

introduce overhead into programs: CONTEXT SWITCH USER -> KERNEL TO RUN THE APP LONG WAITS WHEN RESOURCE use APIS IS UNAVAILABLE

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FINE GRAINED LOCK GRANULARITY

111 74

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Q5 - PERFECT MULTITASKING OPERATING SYSTEM

In a perfect-multi-tasking operating system, every process of the same priority will always receive exactly $1/n^{\text{th}}$ of the available CPU time. Important CPU improvements for multi-tasking include: (1) fast context switching to enable jobs to be swapped in-and-out of the CPU very quickly, and (2) the use of a timer interrupt to preempt running jobs without the user voluntarily yielding the CPU. These innovations have enabled major improvements towards achieving a coveted "Perfect Multi-Tasking System".

List and describe two challenges that remain complicating the full realization of a Perfect Multi-Tasking Operating System. In other words, what makes it very difficult for all jobs (for example, 10 jobs) of the same priority to receive **EXACTLY** the same runtime on the CPU? Your description must explain why the challenge is a problem for achieving perfect multi-tasking.

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L11.75

75

Perfect FAIRNESS - Jobs of the same priority

- JOBS W/ Different centiles + Different arrival times

HS to perfectly balance their runtime

- Querread from time tracting: measuring truntime can be

INACCURATE, AND there is a cost for making

measurements (musurements may not be precise)

- Context switching how do account for overhead of

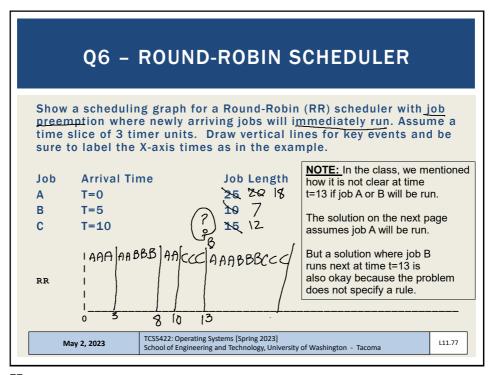
C/S when balancing runtime — A Busy system

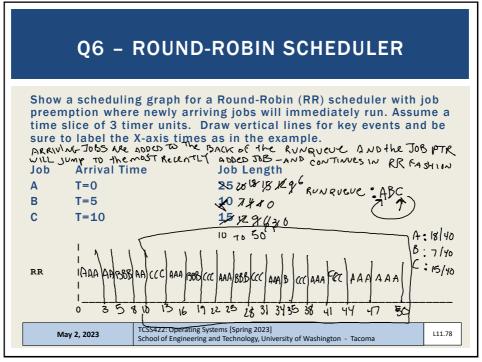
may have more context switches

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Q6 - RR SCHEDULER - 2

Using the graph, from time t=10 until all jobs complete at t=50, evaluate Jain's Fairness Index:

Jain's fairness index is expressed as:

$$\mathcal{J}(x_1,x_2,\ldots,x_n) = rac{(\sum_{i=1}^n x_i)^2}{n \cdot \sum_{i=1}^n x_i^2}$$

Where n is the number of jobs, and x_i is the time share of each process Jain's fairness index=1 for best case fairness, and 1/n for worst case fairness.

For the time window from t=10 to t=50, what percentage of the CPU time is allocated to each of the jobs A, B, and C?

Job A: $\frac{18}{10}$ Job B: $\frac{7}{10}$ Job C: $\frac{15}{10}$ 375

With these values, calculate Jain's fairness index from t=10 to t=50.

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L11.79

79

$$Q6 - II$$

$$J(x_1, x_2, ..., x_n) = \frac{(\sum_{i=1}^n x_i)^2}{n \cdot \sum_{i=1}^n x_i^2} \quad \text{west} \quad \frac{1}{3} = .333$$

$$(.45 + .75 + .375) = (.1)^2 = 1 \quad \text{prefect} \quad I$$

$$n \cdot \underbrace{\sum_{i=1}^n Y_i^2} \rightarrow 3 \cdot \left((.45)^2 + (.175)^2 + (.375)^2 \right) \quad \Rightarrow \quad \frac{1}{1.12125}$$

$$3 \cdot \left(.2025 + .030625 + .140625 \right) \quad \Rightarrow \quad .8918617$$

$$1.12125 \quad \Rightarrow \quad 89.29_6$$
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 L11.80

