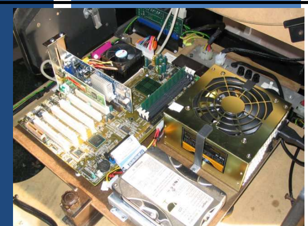
TCSS 422: OPERATING SYSTEMS



Memory Virtualization, Segmentation, Memory Paging

Wes J. Lloyd
School of Engineering and Technology,
University of Washington - Tacoma

FEEDBACK FROM 11/20

- Binary buddy allocation:
  - **How does buddy allocation coalesce fragmented memory?**
- **Buddy allocation: Freeing memory blocks:**
  - 1- Free the block of memory
  - 2- Check the neighboring block - is it free too?
  - 3- If free, combine the two, and repeat step 2 until all memory is freed, or until a non-free neighbor block is encountered

5.2	A: 2^0	C: 2^0	B: 2^1	D: 2^1	2^1	2^3
6	A: 2^0	C: 2^0	2^1	D: 2^1	2^1	2^3
7.1	A: 2^0	C: 2^0	2^1	2^1	2^1	2^3
7.2	A: 2^0	C: 2^0	2^1	2^2		2^3
8	2^0	C: 2^0	2^1	2^2		2^3
9.1	2^0	2^0	2^1	2^2		2^3
9.2	2^1		2^1	2^2		2^3
9.3	2^2			2^2		2^3
9.4	2^3					2^3
9.5	2^4					

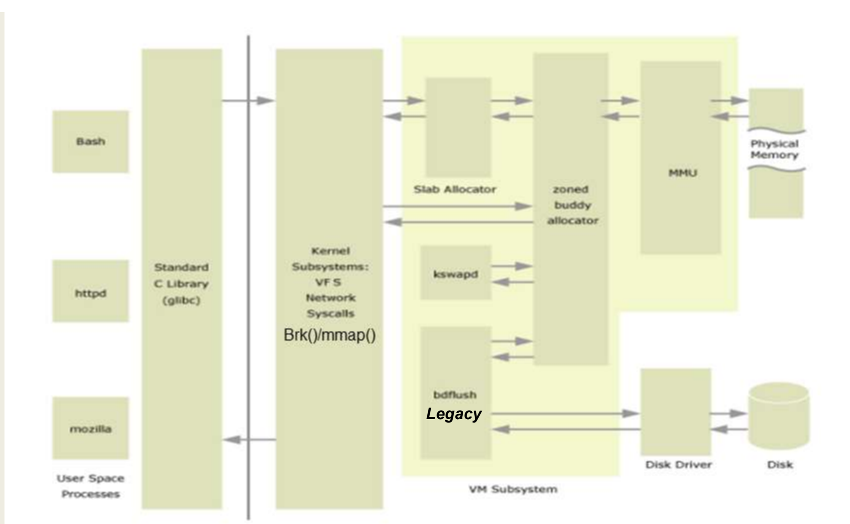
From: https://en.wikipedia.org/wiki/Buddy_memory_allocation

FEEDBACK - 2

- **Which (free space) memory allocation strategy does Ubuntu use?**

- Overview from:
- https://en.wikibooks.org/wiki/The_Linux_Kernel/Memory
- https://zgqallen.github.io/2017/08/03/linux-glic-mm-overview/

OVERVIEW OF VM SYSTEM IN LINUX



COMPONENTS

- **Memory Management Unit (MMU)** – HW module on CPU, integrates "TLB", supports virtual memory address translation
- **Buddy Allocator** – Algorithm to allocate/reclaim page frames from physical memory
  - Provides memory pages to consumers such as OS slab allocators (obj caches), kmalloc
  - Page frames managed in a group for buddy allocation in sizes of 2^n where (size=1,2,4,8,16,32,64,128,256,512,1024…)
  - Memory Zones: DMA/DMA32 (Direct Memory Access) for device I/O, NORMAL, and HIGHMEM (32-bit machines)
  - See /proc/zoneinfo
- **Slab Allocator** – allocates OS object caches – OS structs less than 4kb – provides efficient memory mgmt. for frequently used OS structs

COMPONENTS - 2

- **Kswapd** – kernel swap daemon - maintains memory swap space in response to memory demands exceeding physical memory capacity
- Pages can be swapped to disk to reclaim physical memory
- Page frames carry state info to track what to do w/ a page
  - FREE: available
  - ACTIVE: can't swap
  - INACTIVE DIRTY: no longer used, but modified page
  - INACTIVE LAUNDERED: modified page, currently updating to disk
  - INACTIVE CLEAN: no longer being used, can be swapped out
- **Bdflush** – legacy, simple kernel daemon (pdflush thread) to ensure that dirty pages were periodically written to the underlying storage device – now a separate thread is maintained per device

PAGING TO DISK ?

- Looking for free space?
- ***What is a likely order of preferred states for selecting a page frame?***
- Page frame state
  - FREE: available
  - ACTIVE: can't swap
  - INACTIVE DIRTY: no longer used, but modified page
  - INACTIVE LAUNDERED: modified page, currently updating to disk
  - INACTIVE CLEAN: no longer being used, can be swapped out

PAGE TRANSLATION EXAMPLE

- **Can you go over an example of the page table (address) translation?**
- REVIEW Chapter 18…

REVIEW OF CHAPTER 18: INTRODUCTION TO PAGING

PAGING

- Split up address space of process into ***fixed sized pieces*** called **pages**
- Alternative to ***variable sized pieces*** (Segmentation) which suffers from significant fragmentation
- Physical memory is split up into an array of fixed-size slots called **page frames**.
- Each process has a **page table** which translates virtual addresses to physical addresses

ADVANTAGES OF PAGING

- Flexibility
  - Abstracts the process address space into pages
  - No need to track direction of HEAP / STACK growth
    - *Just add more pages…*
  - No need to store unused space
    - *As with segments…*
- Simplicity
  - Pages and page frames are the same size
  - Easy to allocate and keep a free list of pages

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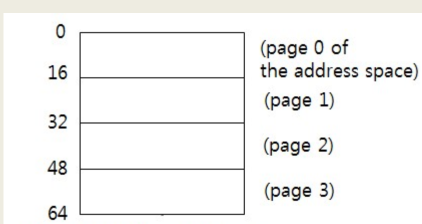
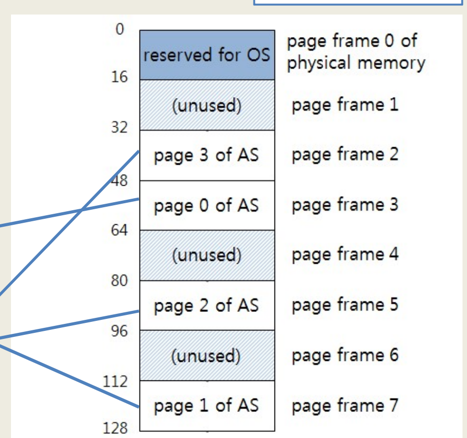
PAGING: EXAMPLE

Page Table:
VP0 → PF3
VP1 → PF7
VP2 → PF5
VP3 → PF2

- Consider a 128 byte address space with 16-byte pages
- Consider a 64-byte program address space



A Simple 64-byte Address Space



64-Byte Address Space Placed In Physical Memory

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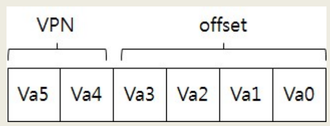
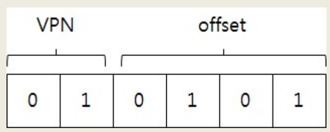
PAGING: ADDRESS TRANSLATION

- PAGE: Has two address components
  - VPN: Virtual Page Number
  - Offset: Offset within a Page



- Example:
  Page Size: 16-bytes, Address Space: 64-bytes



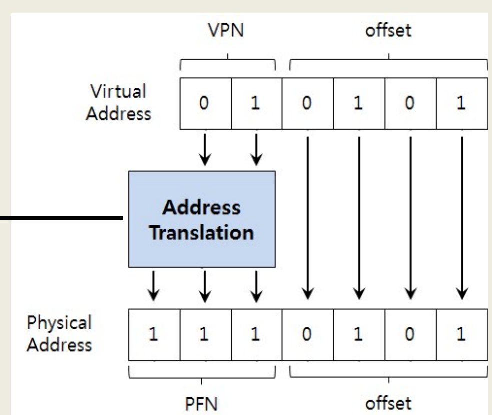
Here there are just four pages...

EXAMPLE: PAGING ADDRESS TRANSLATION

- Consider a 64-byte program address space (4 pages)
- Stored in 128-byte physical memory (8 frames)

- Offset is preserved
- VPN is looked up

Page Table:
VP0 → PF3
VP1 → PF7
VP2 → PF5
VP3 → PF2

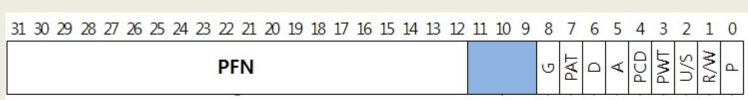


PAGE TRANSLATION EXAMPLE

- Can you go over an example of the page table (address) translation?
- Example:
- Consider a 64kb computer with 256-byte pages
- Consider a simple hello world program
  - Program has only 4 memory pages
  - 1 code page, 1 stack page, 1 heap page, 1 data segment page
- (1) How many 256-byte memory pages can the computer hold?
- (VPN) The operating system provides each user program a 64kb virtual address space.
- (2) How many VPN bits are required to index any virtual page?

EXAMPLE - 2

- (3) To reference any individual byte on a 256-byte page, how many bits are required (OFFSET bits)?
- A single-level page table provides a one-dimensional array to look up the physical frame number of each virtual memory page
- Each page table entry (PTE) is like a record. It contains the Physical Frame Number (PFN) and status bits for the page
- PTE example with 20-bit PTE:



An x86 Page Table Entry(PTE)

EXAMPLE - 3

- Now consider our Page Table Entry (PTE) for our 64kb computer
- (4) How bits are required for the PFN?
- (5) Assuming there are 8 status bits, what is the PTE size in bits? Bytes?
- (6) What is the storage requirement for a 1-level page table?
- (7) Using 1-level page tables to index memory, how many process would fill main memory with page tables!!??

OBJECTIVES

- Quiz 4
- Quiz 5
- Program 3
- **Paging**
- Chapter 18 – Introduction to Paging (*finish…*)
- Chapter 19 – Translation Lookaside Buffer
- Chapter 20 – Paging Smaller Tables
- Chapter 21/22 – Beyond Physical Memory

CHAPTER 18: INTRODUCTION TO PAGING

PAGING DESIGN QUESTIONS

- (1) Where are page tables stored?
- (2) What are the typical contents of the page table?
- (3) How big are page tables?
- (4) Does paging make the system too slow?

(1) WHERE ARE PAGE TABLES STORED?

- Example:
  - Consider a 32-bit process address space (up to 4GB)
  - With 4 KB pages
  - 20 bits for VPN (2^{20} pages)
  - 12 bits for the page offset (2^{12} unique bytes in a page)

- Page tables for each process are stored in RAM
  - Support potential storage of 2^{20} translations = 1,048,576 pages per process
  - Each page has a page table entry size of 4 bytes

PAGE TABLE EXAMPLE

- With 2^{20} slots in our page table for a single process
- Each slot dereferences a VPN
- Provides physical frame number
- Each slot requires 4 bytes (32 bits)
  - 20 for the PFN on a 4GB system with 4KB pages
  - 12 for the offset which is preserved
  - (note we have no status bits, so this is unrealistically small)

VPN_0
VPN_1
VPN_2
…
…
$VPN_{1048576}$

- How much memory to store page table for 1 process?
  - 4,194,304 bytes (or 4MB) to index one process

NOW FOR AN ENTIRE OS

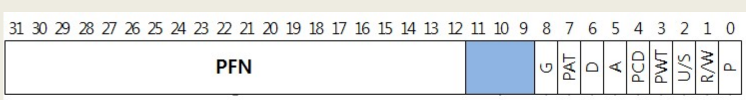
- If 4 MB is required to store one process
- Consider how much memory is required for an entire OS?
  - With for example 100 processes…
- Page table memory requirement is now 4MB x 100 = 400MB
- If computer has 4GB memory (maximum for 32-bits), the page table consumes 10% of memory

400 MB / 4000 GB

- Is this efficient?

(2) WHAT'S ACTUALLY IN THE PAGE TABLE

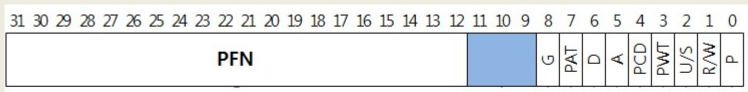
- Page table is data structure used to map virtual page numbers (VPN) to the physical address (Physical Frame Number PFN)
  - Linear page table → simple array
- Page-table entry
  - 32 bits for capturing state



An x86 Page Table Entry(PTE)

PAGE TABLE ENTRY

- P: present
- R/W: read/write bit
- U/S: supervisor
- A: accessed bit
- D: dirty bit
- PFN: the page frame number



An x86 Page Table Entry(PTE)

PAGE TABLE ENTRY - 2

- Common flags:
- **Valid Bit:** Indicating whether the particular translation is valid.
- **Protection Bit:** Indicating whether the page could be read from, written to, or executed from
- **Present Bit:** Indicating whether this page is in physical memory or on disk(swapped out)
- **Dirty Bit:** Indicating whether the page has been modified since it was brought into memory
- **Reference Bit(Accessed Bit):** Indicating that a page has been accessed

(3) HOW BIG ARE PAGE TABLES?

- Page tables are too big to store on the CPU
- Page tables are stored using physical memory
- Paging supports efficiently storing a sparsely populated address space
  - Reduced memory requirement
    Compared to base and bounds, and segments

(4) DOES PAGING MAKE THE SYSTEM TOO SLOW?

- Translation
- **Issue #1:** Starting location of the page table is needed
  - HW Support: Page-table base register
    - stores active process
    - Facilitates translation

Stored in RAM →

Page Table:
VP0 → PF3
VP1 → PF7
VP2 → PF5
VP3 → PF2

- **Issue #2:** Each memory address translation for paging requires an extra memory reference
  - HW Support: TLBs (Chapter 19)

PAGING MEMORY ACCESS

```
// Extract the VPN from the virtual address
VPN = (VirtualAddress & VPN_MASK) >> SHIFT

// Form the address of the page-table entry (PTE)
PTEAddr = PTBR + (VPN * sizeof(PTE))

// Fetch the PTE
PTE = AccessMemory(PTEAddr)

// Check if process can access the page
if (PTE.Valid == False)
        RaiseException(SEGMENTATION_FAULT)
else if (CanAccess(PTE.ProtectBits) == False)
        RaiseException(PROTECTION_FAULT)
else
        // Access is OK: form physical address and fetch it
        offset = VirtualAddress & OFFSET_MASK
        PhysAddr = (PTE.PFN << PFN_SHIFT) | offset
        Register = AccessMemory(PhysAddr)
```


COUNTING MEMORY ACCESSES

- Example: Use this Array initialization Code

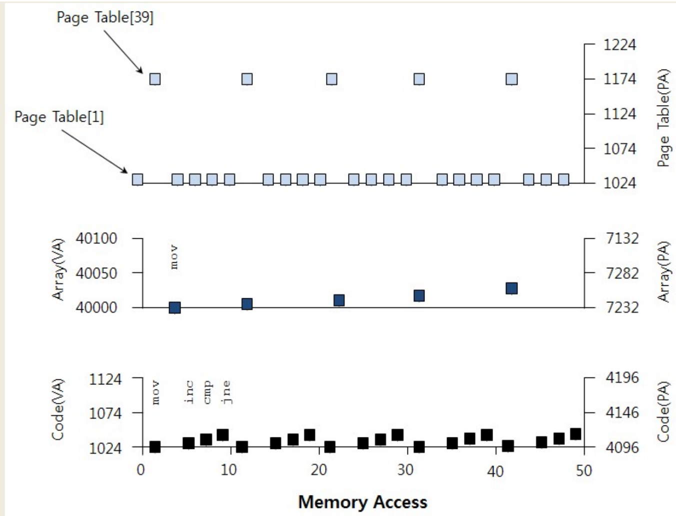
```
int array[1000];
...
for (i = 0; i < 1000; i++)
        array[i] = 0;
```

- Assembly equivalent:

```
0x1024 movl $0x0,(%edi,%eax,4)
0x1028 incl %eax
0x102c cmpl $0x03e8,%eax
0x1030 jne 0x1024
```

VISUALIZING MEMORY ACCESSES:
FOR THE FIRST 5 LOOP ITERATIONS

- Locations:
  - Page table
  - Array
  - Code
- 50 accesses for 5 loop iterations



PAGING SYSTEM EXAMPLE

- Consider a 4GB Computer:
- With a 4096-byte page size (4KB)
- How many pages would fit in physical memory?

- Now consider a page table:
- For the page table entry, how many bits are required for the VPN?
- If we assume the use of 4-byte (32 bit) page table entries, how many bits are available for status bits?
- How much space does this page table require?
  Page Table Entries x Number of pages
- How many page tables (for user processes) would fill the entire 4GB of memory?

CHAPTER 19: TRANSLATION LOOKASIDE BUFFER (TLB)

OBJECTIVES

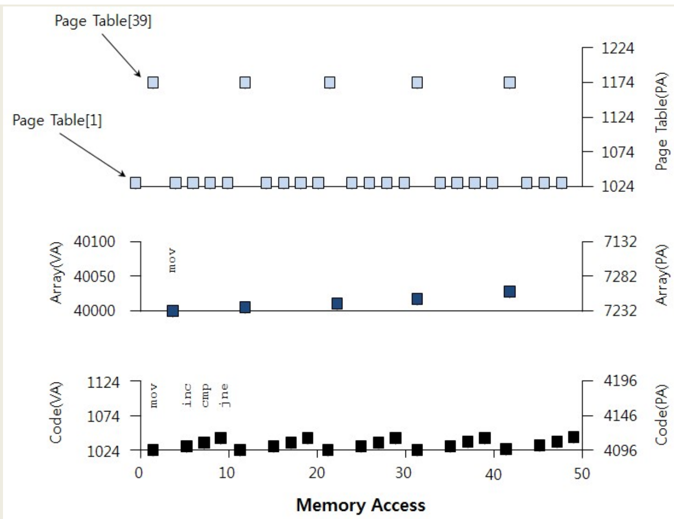
- Chapter 19
  - TLB Algorithm
  - TLB Tradeoffs
  - TLB Context Switch

TRANSLATION LOOKASIDE BUFFER

- Legacy name…
- Better name, "Address Translation Cache"
- TLB is an on CPU cache of address translations
  - virtual → physical memory

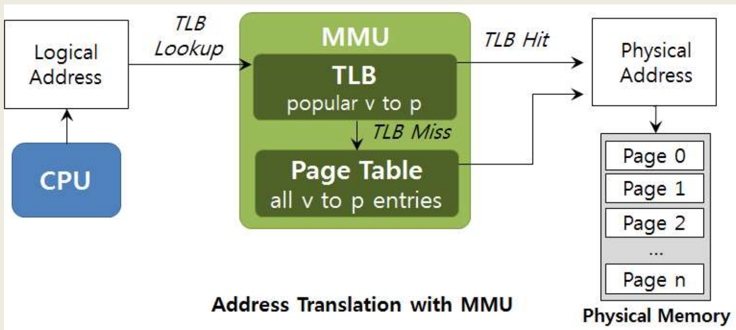
TRANSLATION LOOKASIDE BUFFER - 2

- Goal: Reduce access to the page tables
- Example: 50 RAM accesses for first 5 for-loop iterations
- Move lookups from RAM to TLB by caching page table entries



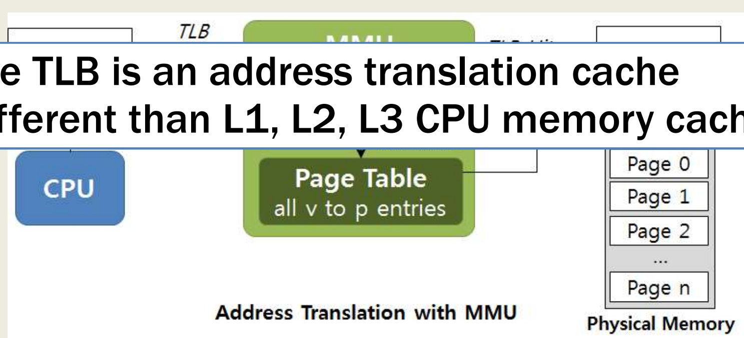
TRANSLATION LOOKASIDE BUFFER (TLB)

- Part of the CPU's Memory Management Unit (MMU)
- Address translation cache



TRANSLATION LOOKASIDE BUFFER (TLB)

- Part of the CPU's Memory Management Unit (MMU)
- Address translation cache



The TLB is an address translation cache
Different than L1, L2, L3 CPU memory caches

TLB BASIC ALGORITHM

- For: array based page table
- Hardware managed TLB

```
VPN = (VirtualAddress & VPN_MASK ) >> SHIFT
(Success , TlbEntry) = TLB_Lookup(VPN)
   if(Success == True){ // TLB Hit
   if(CanAccess(TlbEntry.ProtectBits) == True ){
       Offset = VirtualAddress & OFFSET_MASK
       PhysAddr = (TlbEntry.PFN << SHIFT) | Offset
       AccessMemory( PhysAddr )
   }else RaiseException(PROTECTION_ERROR)
```

Generate the physical address to access memory

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TLB BASIC ALGORITHM - 2

```
    else{ //TLB Miss
        PTEAddr = PTBR + (VPN * sizeof(PTE))
        PTE = AccessMemory(PTEAddr)
        (…)  // Check for, and raise exceptions…

        TLB_Insert( VPN , PTE.PFN , PTE.ProtectBits)
        RetryInstruction()
    }
}
```

Retry the instruction… (requery the TLB)

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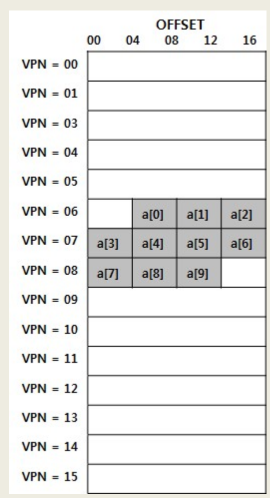
TLB – ADDRESS TRANSLATION CACHE

- **Key detail:**
- **For a TLB miss, we first access the page table in RAM to populate the TLB… we then requery the TLB**
- **All address translations go through the TLB**

TLB EXAMPLE

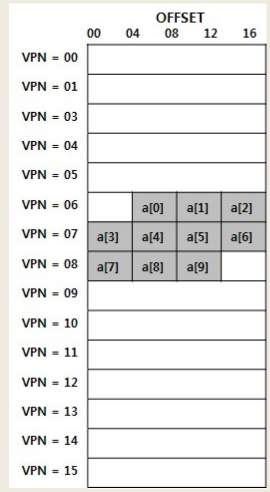
```
int sum = 0 ;
for( i=0; i<10; i++){
        sum+=a[i];
}
```



- Example:
- Program address space: 256-byte
  - Addressable using 8 total bits (2^8)
  - 4 bits for the VPN (16 total pages)
- Page size: 16 bytes
  - Offset is addressable using 4-bits
- Store an array: of (10) 4-byte integers

TLB EXAMPLE - 2

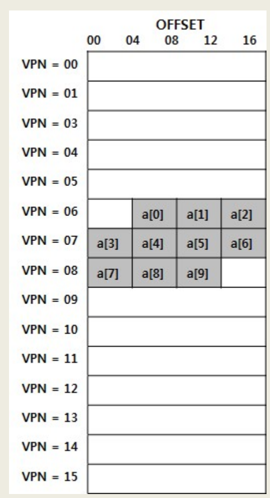
```
int sum = 0 ;
for( i=0; i<10; i++){
        sum+=a[i];
}
```



- Consider the code above:
- Initially the TLB does not know where a[] is
- Consider the accesses:
- a[0], a[1], a[2], a[3], a[4], a[5], a[6], a[7], a[8], a[9]
- How many pages are accessed?
- What happens when accessing a page not in the TLB?

TLB EXAMPLE - 3

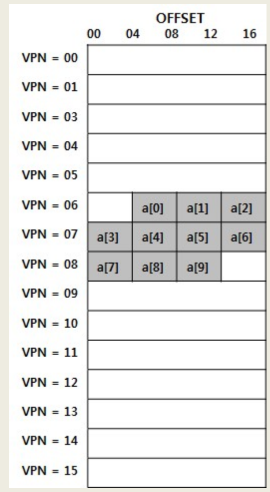
```
int sum = 0 ;
for( i=0; i<10; i++){
        sum+=a[i];
}
```



- For the accesses: a[0], a[1], a[2], a[3], a[4],
- a[5], a[6], a[7], a[8], a[9]
- How many are hits?
- How many are misses?
- What is the hit rate? (%)
  - 70% (3 misses one for each VP, 7 hits)

TLB EXAMPLE - 4

```
int sum = 0 ;
for( i=0; i<10; i++){
        sum+=a[i];
}
```



- What factors affect the hit/miss rate?
  - Page size
  - Data locality
  - Temporal locality

CHAPTER 20: PAGING: SMALLER TABLES

OBJECTIVES

- Chapter 20
  - Smaller tables
  - Hybrid tables
  - Multi-level page tables

LINEAR PAGE TABLES

- Consider array-based page tables:
  - Each process has its own page table
  - 32-bit process address space (up to 4GB)
  - With 4 KB pages
  - 20 bits for VPN
  - 12 bits for the page offset

LINEAR PAGE TABLES - 2

- Page tables stored in RAM
- Support potential storage of 2^{20} translations
  = 1,048,576 pages per process @ 4 bytes/page
- Page table size 4MB / process

$$\text{Page table size} = \frac{2^{32}}{2^{12}} * 4Byte = 4MByte$$

- Consider 100+ OS processes
  - Requires 400+ MB of RAM to store process information

LINEAR PAGE TABLES - 2

- Page tables stored in RAM
- Support potential storage of 2^{20} translations
  = 1,048,576 pages per process @ 4 bytes/page
- Page table size 4MB / process

Page tables are too big and consume too much memory.

Need Solutions …

- Consider 100+ OS processes
  - Requires 400+ MB of RAM to store process information

PAGING: USE LARGER PAGES

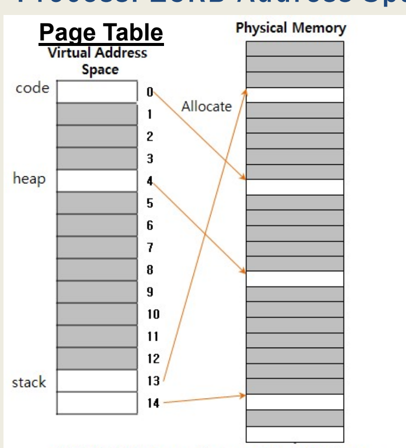
- Larger pages = 16KB = 2^{14}
- 32-bit address space: 2^{32}
- 2^{18} = 262,144 pages

$$\frac{2^{32}}{2^{14}} * 4 = 1MB \quad \text{per page table}$$

- Memory requirement cut to ¼
- However pages are huge
- Internal fragmentation results
- 16KB page(s) allocated for small programs with only a few variables

PAGE TABLES: WASTED SPACE

- Process: 16KB Address Space w/ 1KB pages



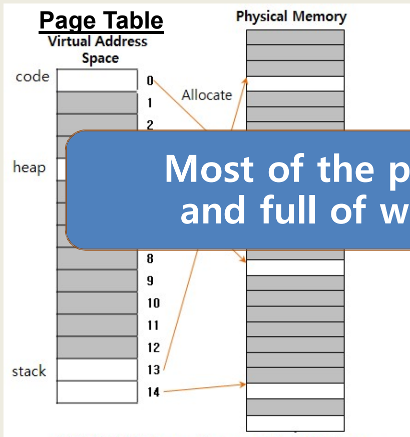
A 16KB Address Space with 1KB Pages

PFN	valid	prot	present	dirty
10	1	r-x	1	0
-	0	-	-	-
-	0	-	-	-
-	0	-	-	-
15	1	rw-	1	1
…	…	…	…	…
-	0	-	-	-
3	1	rw-	1	1
23	1	rw-	1	1

A Page Table For 16KB Address Space

PAGE TABLES: WASTED SPACE

- Process: 16KB Address Space w/ 1KB pages



A 16KB Address Space with 1KB Pages

Most of the page table is unused and full of wasted space. (73%)

PFN	valid	prot	present	dirty
				0
				-
				-
				-
15	1	rw-	1	1
…	…	…	…	…
-	0	-	-	-
3	1	rw-	1	1
23	1	rw-	1	1

A Page Table For 16KB Address Space

MULTI-LEVEL PAGE TABLES

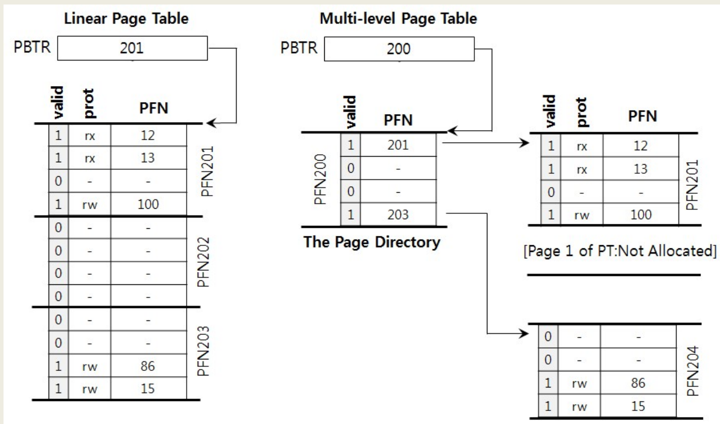
- Consider a page table:
- 32-bit addressing, 4KB pages
- 2^{20} page table entries
- Even if memory is sparsely populated the *per process* page table requires:

Page table size = $\frac{2^{32}}{2^{12}} * 4Byte = 4MByte$

- Often most of the 4MB *per process* page table is empty
- Page table must be placed in 4MB contiguous block of RAM
- MUST SAVE MEMORY!

MULTI-LEVEL PAGE TABLES - 2

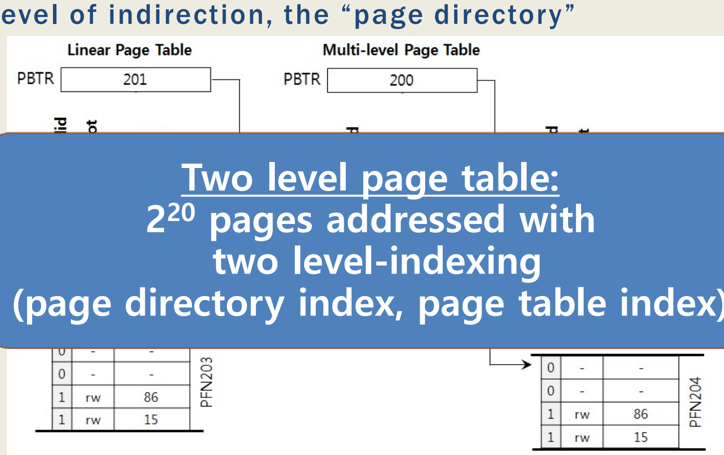
- Add level of indirection, the "page directory"



Linear (Left) And Multi-Level (Right) Page Tables

MULTI-LEVEL PAGE TABLES - 2

- Add level of indirection, the "page directory"



Two level page table:
2^{20} pages addressed with
two level-indexing
(page directory index, page table index)

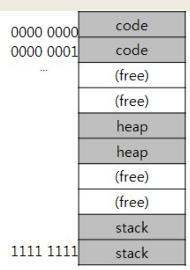
Linear (Left) And Multi-Level (Right) Page Tables

MULTI-LEVEL PAGE TABLES - 3

- Advantages
  - Only allocates page table space in proportion to the address space actually used
  - Can easily grab next free page to expand page table
- Disadvantages
  - Multi-level page tables are an example of a time-space tradeoff
  - Sacrifice address translation time (now 2-level) for space
  - Complexity: multi-level schemes are more complex

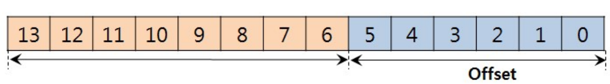
EXAMPLE

- 16KB address space, 64byte pages
- How large would a one-level page table need to be?
- 2^{14} (address space) / 2^{6} (page size) = 2^{8} = 256 (pages)



Flag	Detail
Address space	16 KB
Page size	64 byte
Virtual address	14 bit
VPN	8 bit
Offset	6 bit
Page table entry	2^8(256)

A 16-KB Address Space With 64-byte Pages

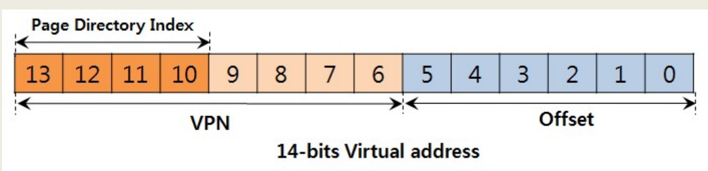


EXAMPLE - 2

- 256 total page table entries (64 bytes each)
- 1,024 bytes page table size, stored using 64-byte pages = (1024/64) = 16 page directory entries (PDEs)
- Each page directory entry (PDE) can hold 16 page table entries (PTEs) *e.g. lookups*
- 16 page directory entries (PDE) x 16 page table entries (PTE) = 256 total PTEs
- **Key idea: the page table is stored using pages too!**

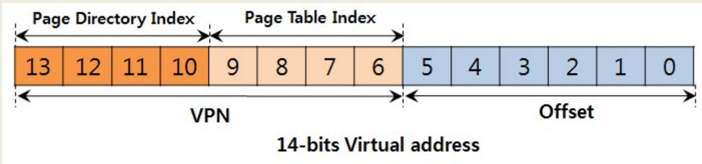
PAGE DIRECTORY INDEX

- Now, let's split the page table into two:
  - 8 bit VPN to map 256 pages
  - 4 bits for page directory index (PDI – 1^{st} level page table)
  - 6 bits offset into 64-byte page



PAGE TABLE INDEX

- 4 bits page directory index (PDI – 1st level)
- 4 bits page table index (PTI – 2nd level)



- To dereference one 64-byte memory page,
  - We need one page directory entry (PDE)
  - One page table Index (PTI) – can address 16 pages

EXAMPLE - 3

- For this example, how much space is required to store as a ***single-level*** page table with any number of PTEs?

- 16KB address space, 64 byte pages
- 256 page frames, 4 byte page size
- 1,024 bytes required (*single level*)

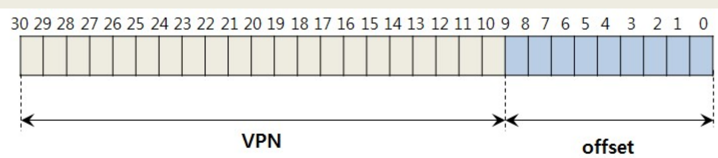
- How much space is required for a ***two-level*** page table with only 4 page table entries (PTEs) ?
- Page directory = 16 entries x 4 bytes (1 x 64 byte page)
- Page table = 4 entries x 4 bytes (1 x 64 byte page)
- 128 bytes required (2 x 64 byte pages)
  - Savings = using just 12.5% the space !!!

32-BIT EXAMPLE

- Consider: 32-bit address space, 4KB pages, 2^{20} pages
- Only 4 mapped pages
- **Single level**: 4 MB (we've done this before)
- **Two level**: (old VPN was 20 bits, split in half)
- Page directory = 2^{10} entries x 4 bytes = 1 x 4 KB page
- Page table = 4 entries x 4 bytes (mapped to 1 4KB page)
- 8KB (8,192 bytes) required
- Savings = using just .78 % the space !!!
- 100 sparse processes now require < 1MB for page tables

MORE THAN TWO LEVELS

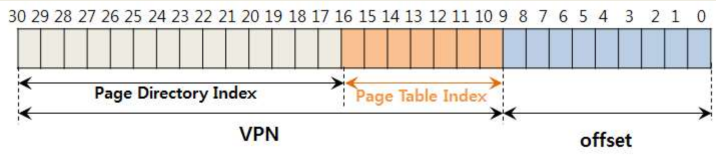
- Consider: page size is 2^9 = 512 bytes
- Page size 512 bytes / Page entry size 4 bytes
- VPN is 21 bits



Flag	Detail
Virtual address	30 bit
Page size	512 byte
VPN	21 bit
Offset	9 bit

MORE THAN TWO LEVELS - 2

- Page table entries per page = 512 / 4 = 128
- 7 bytes – for page table index (PTI)

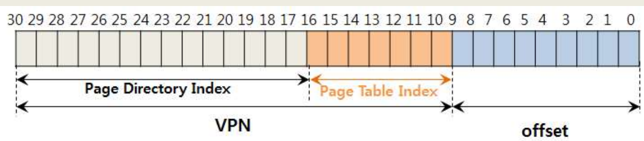


Flag	Detail
Virtual address	30 bit
Page size	512 byte
VPN	21 bit
Offset	9 bit
Page entry per page	128 PTEs

→ $\log_2 128 = 7$

MORE THAN TWO LEVELS - 3

- To map 1 GB address space (2^{30}=1GB RAM, 512-byte pages)
- 2^{14} = 16,384 page directory entries (PDEs) are required
- When using 2^7 (128 entry) page tables…
- Page size = 512 bytes / 4 bytes per addr



Flag	Detail
Virtual address	30 bit
Page size	512 byte
VPN	21 bit
Offset	9 bit
Page entry per page	128 PTEs

→ $\log_2 128 = 7$

MORE THAN TWO LEVELS - 3

- To map 1 GB address space (2^{30}=1GB RAM, 512-byte pages)
- 2^{14} = 16,384 page directory entries (PDEs) are required
- When using 2^7 (128 entry) page tables…
- Page size = 512 bytes / 4 bytes per addr

Can't Store Page Directory with 16K pages, using 512 bytes pages. Pages only dereference 128 addresses (512 bytes / 32 bytes)

Virtual address	30 bit
Page size	512 byte
VPN	21 bit
Offset	9 bit
Page entry per page	128 PTEs → $\log_2 128 = 7$

MORE THAN TWO LEVELS - 3

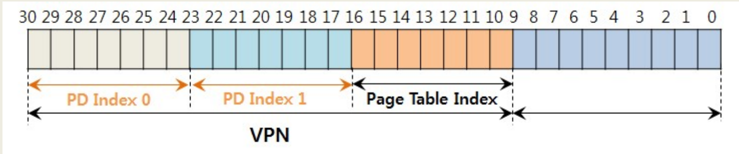
- To map 1 GB address space (2^{30}=1GB RAM, 512-byte pages)
- 2^{14} = 16,384 page directory entries (PDEs) are required
- When using 2^7 (128 entry) page tables…
- Page size = 512 bytes / 4 bytes per addr

**Need three level page table:
Page directory 0 (PD Index 0)
Page directory 1 (PD Index 1)
Page Table Index**

Virtual address	30 bit
Page size	512 byte
VPN	21 bit
Offset	9 bit
Page entry per page	128 PTEs → $\log_2 128 = 7$

MORE THAN TWO LEVELS - 4

- We can now address 1GB with“fine grained” 512 byte pages
- Using multiple levels of indirection



- Consider the implications for address translation!
- How much space is required for a virtual address space with 4 entries on a 512-byte page? (let’s say 4 32-bit integers)
- PD0 1 page, PD1 1 page, PT 1 page = 1,536 bytes
- Savings = 1,536 / 8,388,608 (8mb) = .0183% !!!

ADDRESS TRANSLATION CODE

```
// 5-level Linux page table address lookup
//
// Inputs:
// mm_struct – process’s memory map struct
// vpage – virtual page address

// Define page struct pointers
pgd_t *pgd;
p4d_t *p4d;
pud_t *pud;
pmd_t *pmt;
pte_t *pte;
struct page *page;
```

ADDRESS TRANSLATION - 2

```
pgd = pgd_offset(mm, vpage);
if (pgd_none(*pgd) || pgd_bad(*pgd))
    return 0;
p4d = p4d_offset(pgd, vpage);
if (p4d_none(*p4d) || p4d_bad(*p4d))
    return 0;
pud = pud_offset(p4d, vpage);
if (pud_none(*pud) || pud_bad(*pud))
    return 0;
pmd = pmd_offset(pud, vpage);
if (pmd_none(*pmd) || pmd_bad(*pmd))
    return 0;
if (!(pte = pte_offset_map(pmd, vpage)))
    return 0;
if (!(page = pte_page(*pte)))
    return 0;
physical_page_addr = page_to_phys(page);
pte_unmap(pte);
return physical_page_addr;  // param to send back
```

pgd_offset():
Takes a vpage address and the mm_struct for the process, returns the PGD entry that covers the requested address…

p4d/pud/pmd_offset():
Takes a vpage address and the pgd/p4d/pud entry and returns the relevant p4d/pud/pmd.

pte_unmap()
release temporary kernel mapping for the page table entry

INVERTED PAGE TABLES

- Keep a single page table for each physical page of memory
- Consider 4GB physical memory
- Using 4KB pages, page table requires 4MB to map all of RAM
- Page table stores
  - Which process uses each page
  - Which process virtual page (from process virtual address space) maps to the physical page
- All processes share the same page table for memory mapping, kernel must isolate all use of the shared structure
- Finding process memory pages requires search of 2^{20} pages
- Hash table: can index memory and speed lookups

MULTI-LEVEL PAGE TABLE EXAMPLE

- Consider a 16 MB computer which indexes memory using 4KB pages
- (#1) For a single level page table, how many pages are required to index memory?
- (#2) How many bits are required for the VPN?
- (#3) Assuming each page table entry (PTE) can index any byte on a 4KB page, how many offset bits are required?
- (#4) Assuming there are 8 status bits, how many bytes are required for each page table entry?

MULTI LEVEL PAGE TABLE EXAMPLE - 2

- (#5) How many bytes (or KB) are required for a single level page table?
- Let's assume a simple HelloWorld.c program.
- HelloWorld.c requires virtual address translation for 4 pages:
  - 1 – code page   1 – stack page
  - 1 – heap page   1 – data segment page
- (#6) Assuming a two-level page table scheme, how many bits are required for the Page Directory Index (PDI)?
- (#7) How many bits are required for the Page Table Index (PTI)?

MULTI LEVEL PAGE TABLE EXAMPLE - 3

- Assume each page directory entry (PDE) and page table entry (PTE) requires 4 bytes:
  - 6 bits for the Page Directory Index (PDI)
  - 6 bits for the Page Table Index (PTI)
  - 12 offset bits
  - 8 status bits
- (#8) How much **total** memory is required to index the HelloWorld.c program using a two-level page table when we only need to translate 4 total pages?
- HINT: we need to allocate one Page Directory and one Page Table…
- HINT: how many entries are in the PD and PT

MULTI LEVEL PAGE TABLE EXAMPLE - 4

- (#9) Using a single page directory entry (PDE) pointing to a single page table (PT), if all of the slots of the page table (PT) are in use, what is the total amount of memory a two-level page table scheme can address?
- (#10) And finally, for this example, as a percentage (%), how much memory does the 2-level page table scheme consume compared to the 1-level scheme?
- HINT: two-level memory use / one-level memory use

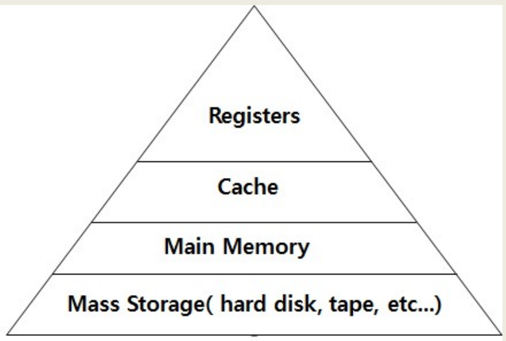
ANSWERS

- #1 – 4096 pages
- #2 – 12 bits
- #3 – 12 bits
- #4 – 4 bytes
- #5 – 4096 x 4 = 16,384 bytes (16KB)
- #6 – 6 bits
- #7 – 6 bits
- #8 – 256 bytes for Page Directory (PD) (64 entries x 4 bytes)
  256 bytes for Page Table (PT) **TOTAL = 512 bytes**
- #9 – 64 entries, where each entry maps a 4,096 byte page
  With 12 offset bits, can address 262,144 bytes (256 KB)
- #10- 512/16384 = .03125 → 3.125%

CHAPTER 21/22: BEYOND PHYSICAL MEMORY

MEMORY HIERARCHY

- Disks (HDD, SSD) provide another level of storage in the memory hierarchy



Memory Hierarchy in modern system

MOTIVATION FOR EXPANDING THE ADDRESS SPACE

- Can provide illusion of an address space larger than physical RAM
- For a single process
  - Convenience
  - Ease of use
- For multiple processes
  - Large virtual memory space for many concurrent processes

LATENCY TIMES

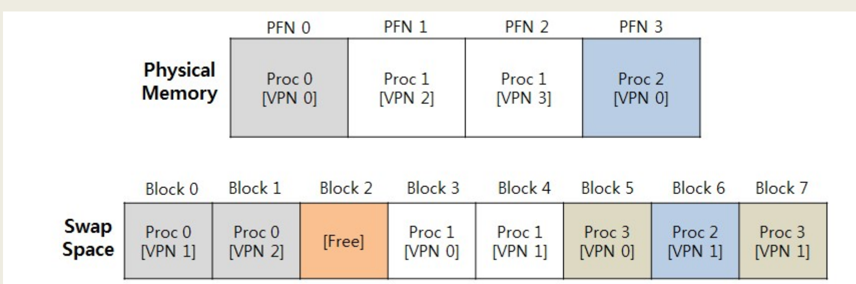
- Design considerations
  - SSDs 4x the time of DRAM
  - HDDs 80x the time of DRAM

Action	Latency (ns)	(μs)	
L1 cache reference	0.5ns		
L2 cache reference	7 ns		14x L1 cache
Mutex lock/unlock	25 ns		
Main memory reference	100 ns		20x L2 cache, 200x L1
Read 4K randomly from SSD*	150,000 ns	150 μs	~1GB/sec SSD
Read 1 MB sequentially from memory	250,000 ns	250 μs	
Read 1 MB sequentially from SSD*	1,000,000 ns	1,000 μs	1 ms ~1GB/sec SSD, 4X memory
Read 1 MB sequentially from disk	20,000,000 ns	20,000 μs	20 ms 80x memory, 20X SSD

- Latency numbers every programmer should know
- From: https://gist.github.com/jboner/2841832#file-latency-txt

SWAP SPACE

- Disk space for storing memory pages
- “Swap” them in and out of memory to disk as needed



Physical Memory and Swap Space

PAGE LOCATION

- Page table pages are:
  - Stored in memory
  - Swapped to disk
- Present bit
  - In the page table entry (PTE) indicates if page is present
- Page fault
  - Memory page is accessed, but has been swapped to disk

PAGE FAULT

- OS steps in to handle the page fault
- Loading page from disk requires a free memory page
- Page-Fault Algorithm

```
PFN = FindFreePhysicalPage()
if (PFN == -1)                   // no free page found
        PFN = EvictPage()        // run replacement algorithm
DiskRead(PTE.DiskAddr, pfn)      // sleep (waiting for I/O)
PTE.present = True               // set PTE bit to present
PTE.PFN = PFN                    // reference new loaded page
RetryInstruction()               // retry instruction
```

PAGE REPLACEMENTS

- Page daemon
  - Background threads which monitors swapped pages
- Low watermark (LW)
  - Threshold for when to swap pages to disk
  - Daemon checks: free pages < LW
  - Begin swapping to disk until reaching the highwater mark
- High watermark (HW)
  - Target threshold of free memory pages
  - Daemon free until: free pages >= HW

REPLACEMENT POLICIES

CACHE MANAGEMENT

- Replacement policies apply to "any" cache
- Goal is to minimize the number of misses
- Average memory access time can be estimated:

$$AMAT = (P_{Hit} * T_M) + (P_{Miss} * T_D)$$

Argument	Meaning
T_M	The cost of accessing memory (time)
T_D	The cost of accessing disk (time)
P_{Hit}	The probability of finding the data item in the cache(a hit)
P_{Miss}	The probability of not finding the data in the cache(a miss)

- Consider T_M = 100 ns, T_D = 10ms
- Consider P_{hit} = .9 (90%), P_{miss} = .1
- Consider P_{hit} = .999 (99.9%), P_{miss} = .001

OPTIMAL REPLACEMENT POLICY

- What if:
  - We could predict the future (... with a magical oracle)
  - All future page accesses are known
  - Always replace the page in the cache used farthest in the future
- Used for a comparison
- Provides a "best case" replacement policy
- Consider a 3-element empty cache with the following page accesses:

0 1 2 0 1 3 0 3 1 2 1

What is the hit/miss ratio?

6 hits

FIFO REPLACEMENT

- Queue based
- Always replace the oldest element at the back of cache
- Simple to implement
- Doesn't consider importance… just arrival ordering
- Consider a 3-element empty cache with the following page accesses:

0 1 2 0 1 3 0 3 1 2 1

- What is the hit/miss ratio?
- How is FIFO different than LRU?

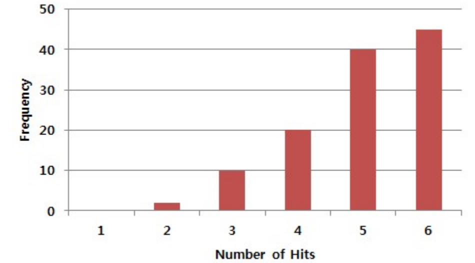
4 hits

LRU incorporates history

RANDOM REPLACEMENT

- Pick a page at random to replace
- Simple and fast implementation
- Performance depends on luck of random choices

0 1 2 0 1 3 0 3 1 2 1



Random Performance over 10,000 Trials

HISTORY-BASED POLICIES

- LRU: Least recently used
- Always replace page with oldest access time (front)
- Always move end of cache when element is read again
- Considers temporal locality (*when pg was last accessed*)

0 1 2 0 1 3 0 3 1 2 1

What is the hit/miss ratio?

6 hits

- LFU: Least frequently used
- Always replace page with fewest accesses (front)
- Consider frequency of page accesses

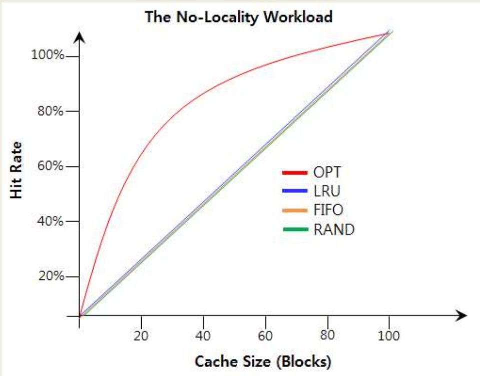
0 1 2 0 1 3 0 3 1 2 1

Hit/miss ratio is=

6 hits

WORKLOAD EXAMPLES: NO-LOCALITY

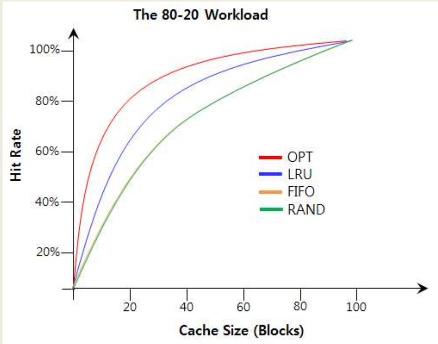
- No-Locality (Random Access) Workload
  - Perform 10,000 random page accesses
  - Across set of 100 memory pages



When the cache is large enough to fit the entire workload, it doesn't matter which policy you use.

WORKLOAD EXAMPLES: 80/20

- 80/20 Workload
  - Perform 10,000 page accesses, against set of 100 pages
  - 80% of accesses are to 20% of pages (hot pages)
  - 20% of accesses are to 80% of pages (cold pages)

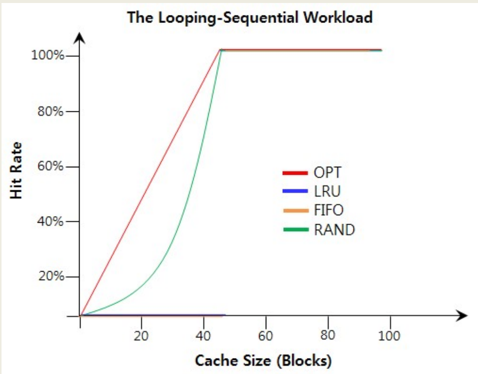


LRU is more likely to hold onto hot pages

(recalls history)

WORKLOAD EXAMPLES: SEQUENTIAL

- Looping sequential workload
  - Refer to 50 pages in sequence: 0, 1, …, 49
  - Repeat loop



Random performs better than FIFO and LRU for cache sizes < 50

Algorithms should provide "scan resistance"

IMPLEMENTING LRU

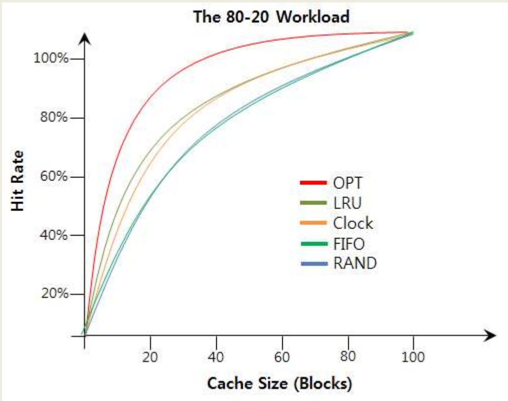
- Implementing last recently used (LRU) requires tracking access time for all system memory pages
- Times can be tracked with a list
- For cache eviction, we must scan an entire list
- Consider: 4GB memory system (2^{32}),
  with 4KB pages (2^{12})
- This requires 2^{20} comparisons !!!
- Simplification is needed
  - Consider how to approximate the oldest page access

IMPLEMENTING LRU - 2

- Harness the Page Table Entry (PTE) Use Bit
- HW sets to 1 when page is used
- OS sets to 0
- Clock algorithm (*approximate LRU*)
  - Refer to pages in a circular list
  - Clock hand points to current page
  - Loops around
    - IF USE_BIT=1 set to USE_BIT = 0
    - IF USE_BIT=0 replace page

CLOCK ALGORITHM

- Not as efficient as LRU, but better than other replacement algorithms that do not consider history



CLOCK ALGORITHM - 2

- Consider dirty pages in cache
- If DIRTY (modified) bit is FALSE
  - No cost to evict page from cache
- If DIRTY (modified) bit is TRUE
  - Cache eviction requires updating memory
  - Contents have changed
- Clock algorithm should favor no cost eviction

WHEN TO LOAD PAGES

- On demand → demand paging
- Prefetching
  - Preload pages based on anticipated demand
  - Prediction based on locality
  - Access page P, suggest page P+1 may be used
- What other techniques might help anticipate required memory pages?
  - Prediction models, historical analysis
  - In general: accuracy vs. effort tradeoff
  - High analysis techniques struggle to respond in real time

OTHER SWAPPING POLICIES

- Page swaps / writes
  - Group/cluster pages together
  - Collect pending writes, perform as batch
  - Grouping disk writes helps amortize latency costs
- Thrashing
  - Occurs when system runs many memory intensive processes and is low in memory
  - Everything is constantly swapped to-and-from disk

OTHER SWAPPING POLICIES - 2

- Working sets
  - Groups of related processes
  - When thrashing: prevent one or more working set(s) from running
  - Temporarily reduces memory burden
  - Allows some processes to run, reduces thrashing

QUESTIONS