

MATERIAL / PACE

- Please classify your perspective on material covered in today's class (46 respondents):
- 1-mostly review, 5-equal new/review, 10-mostly new
- Average 6.70 (↑ previous 5.73)
- Please rate the pace of today's class:
- 1-slow, 5-just right, 10-fast
- Average 5.24 (↑ previous 4.80)

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FEEDBACK FROM 5/1

How do we guarantee in "test and set" that the set value is different from the original value?

```
11 void lock(lock_t *lock) {
12    while (TestAndSet(&lock->flag, 1) == 1)
13    ;    // spin-wait
14 }
```

- Atomic TestAndSet() is called within lock()
- The output from TestAndSet is inspected
- Only if the returned 'old' value from TestAndSet() is ZERO, do we acquire the lock

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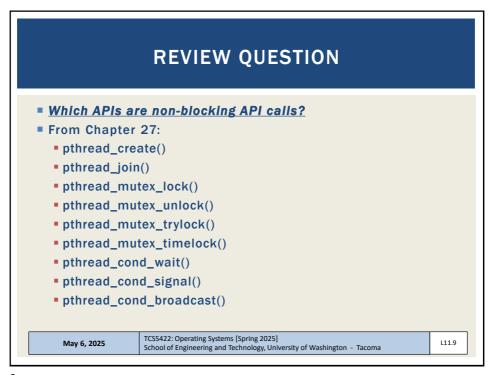
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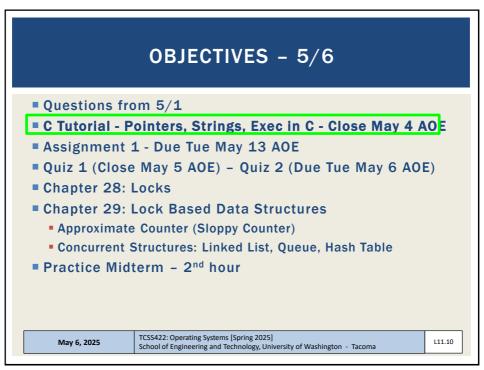
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TEST AND SET C pseudo code int TestAndSet(int *ptr, int new) { int old = *ptr; // fetch old value at ptr *ptr = new; // store 'new' into ptr return old; // return the old value 3 4 Chat GPT can provide the assembly code for x86 "TestAndSet" mov eax. 1 lock xchg eax, [lock_var] ; Atomically set [lock_var] to 1, get old value in eax 1 is loaded into eax register 'lock' forces the xchg instruction to be atomic ■ xchg swaps the values eax ← → [lock_var] Old lock_var is in eax, can be checked TCSS422: Operating Systems [Spring 2025] May 6, 2025 School of Engineering and Technology, University of Washington - Tacoma

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X86 ASSEMBLY LOCK Chat GPT can provide the assembly spinlock using xchg acquire lock: ; Value to set mov eax, 1 .spin: lock xchg eax, [lock_var] ; Atomically swap eax and lock_var test eax, eax ; Was the previous value 0? jnz .spin ; If not, spin (someone else has the lock) ret Notice the use of a 'goto' =) • jnz is a conditional jump (or goto) TCSS422: Operating Systems [Spring 2025] May 6, 2025 1118 School of Engineering and Technology, University of Washington - Tacoma





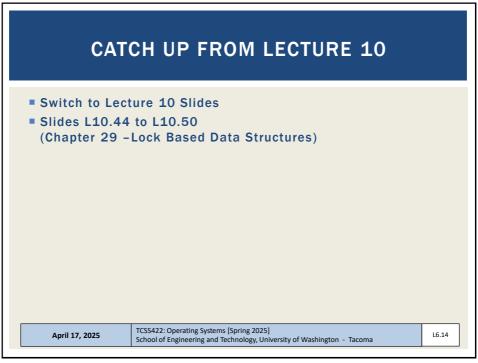
OBJECTIVES - 5/6 Questions from 5/1 C Tutorial - Pointers, Strings, Exec in C - Close May 4 AOE Assignment 1 - Due Tue May 13 AOE Quiz 1 (Close May 5 AOE) - Quiz 2 (Due Tue May 6 AOE) Chapter 28: Locks Chapter 29: Lock Based Data Structures Approximate Counter (Sloppy Counter) Concurrent Structures: Linked List, Queue, Hash Table Practice Midterm - 2nd hour

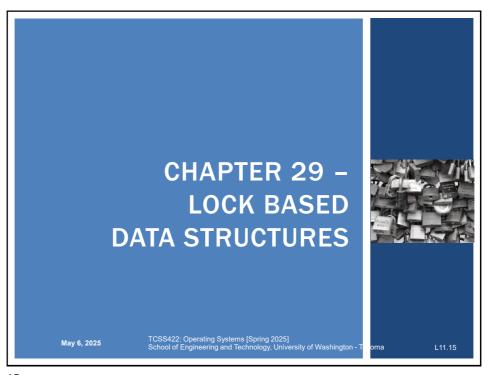
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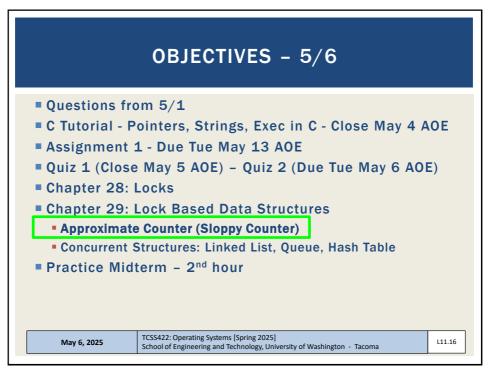
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QUIZ 2 Canvas Quiz - Practice CPU Scheduling Problems Posted in Canvas Unlimited attempts permitted Provides CPU scheduling practice problems FIFO, SJF, STCF, RR, MLFQ (Ch. 7 & 8) Multiple choice and fill-in the blank Quiz automatically scored by Canvas Please report any grading problems Please report any grading problems Due Tuesday May 6th AOE Link: https://canvas.uw.edu/courses/1809484/assignments/10329061

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APPROXIMATE (SLOPPY) COUNTER

- Provides single logical shared counter
 - Implemented using local counters for each ~CPU core
 - 4 CPU cores = 4 local counters & 1 global counter
 - Local counters are synchronized via local locks
 - Global counter is updated periodically
 - Global counter has lock to protect global counter value
 - Update threshold (S) referred to as sloppiness threshold: How often to push local values to global counter
 - Small (S): more updates, more overhead
 - Large (S): fewer updates, more performant, less synchronized
- Why this implementation?

Why do we want counters local to each CPU Core?

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L11.17

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APPROXIMATE COUNTER - MAIN POINTS

- Idea of the Approximate Counter is to <u>RELAX</u> the synchronization requirement for counting
 - Instead of synchronizing global count variable each time: counter=counter+1
 - Synchronization occurs only every so often:
 e.g. every 1000 counts
- Relaxing the synchronization requirement <u>drastically</u> reduces locking API overhead by trading-off split-second accuracy of the counter
- Approximate counter: trade-off accuracy for speed
 - It's approximate because it's not so accurate (until the end)

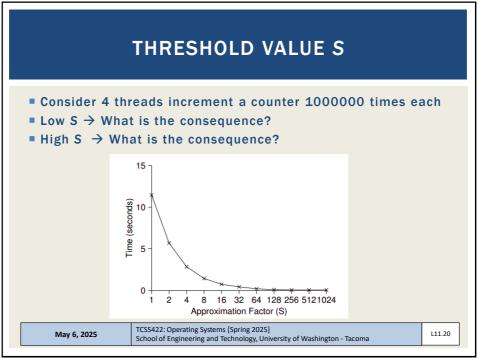
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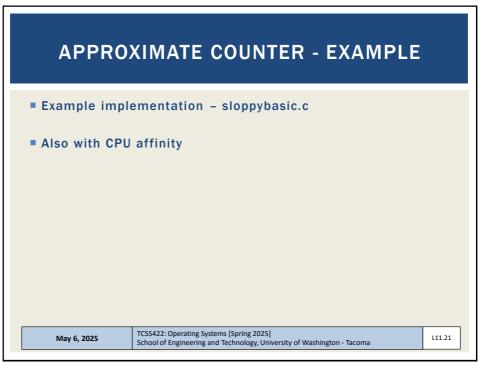
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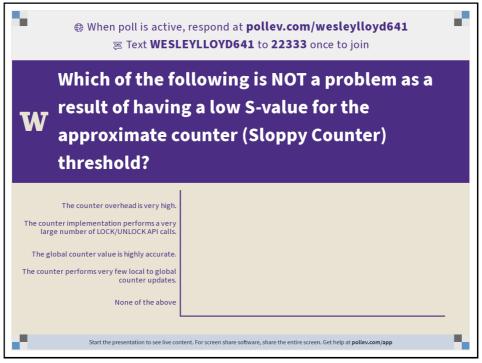
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APPROXIMATE COUNTER - 2 ■ Update threshold (S) = 5 Synchronized across four CPU cores ■ Threads update local CPU counters Time $\mathbf{L_1}$ L_3 G L_4 $5 \rightarrow 0$ 5 (from L_1) $5 \rightarrow 0$ 10 (from L_4) TCSS422: Operating Systems [Spring 2025] May 6, 2025 School of Engineering and Technology, University of Washington - Tacoma







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CONCURRENT LINKED LIST - 1 Simplification - only basic list operations shown Structs and initialization: // basic node structure typedef struct __node_t { int key; 3 struct __node_t *next; } node_t; // basic list struct typedef struct __list_t { node_t *head; red mutex t : // basic list structure (one used per list) 8 9 10 pthread_mutex_t lock; } list_t; 12 13 void List Init(list t *L) { L->head = NULL; 14 pthread_mutex_init(&L->lock, NULL); 15 16 } 17 (Cont.) TCSS422: Operating Systems [Spring 2025] May 6, 2025 L11.24 School of Engineering and Technology, University of Washington - Tacoma

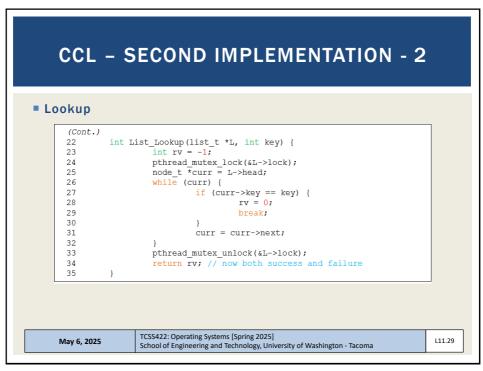


CONCURRENT LINKED LIST - 3 Lookup - checks list for existence of item with key Once again everything is critical Note - there are also two unlocks (Cont.) 32 int List_Lookup(list_t *L, int key) { 32 33 pthread_mutex_lock(&L->lock); 34 node_t *curr = L->head; while (curr) { 35 36 if (curr->key == key) { 37 pthread mutex unlock(&L->lock); 38 return 0; // success 39 40 curr = curr->next; 41 42 pthread_mutex_unlock(&L->lock); 43 return -1; // failure 44 TCSS422: Operating Systems [Spring 2025] May 6, 2025 L11.26 School of Engineering and Technology, University of Washington - Tacoma

CONCURRENT LINKED LIST First Implementation: Lock everything inside Insert() and Lookup() If malloc() fails lock must be released Research has shown "exception-based control flow" to be error prone 40% of Linux OS bugs occur in rarely taken code paths Unlocking in an exception handler is considered a poor coding practice There is nothing specifically wrong with this example however Second Implementation ... May 6, 2025 TCSS422: Operating Systems [Spring 2025] School of Engineering and Technology, University of Washington - Tacoma

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CCL - SECOND IMPLEMENTATION Init and Insert void List_Init(list_t *L) { L->head = NULL; pthread_mutex_init(&L->lock, NULL); void List_Insert(list_t *L, int key) { node_t *new = malloc(sizeof(node_t)); if (new == NULL) { 10 perror("malloc"); 11 return; 12 new->key = key; 13 14 15 // just lock critical section 16 pthread_mutex_lock(&L->lock); new->next = L->head; 18 L->head = new; 19 pthread_mutex_unlock(&L->lock); 20 21 TCSS422: Operating Systems [Spring 2025] May 6, 2025 L11.28 School of Engineering and Technology, University of Washington - Tacoma

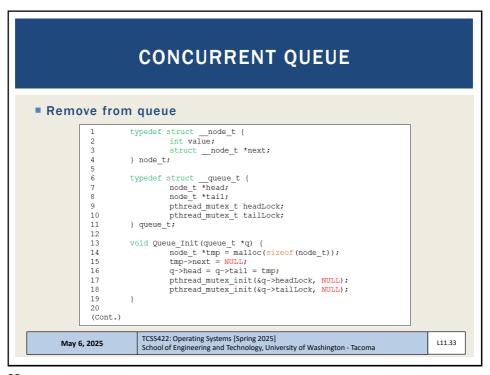


CONCURRENT LINKED LIST PERFORMANCE Using a single lock for entire list is not very performant Users must "wait" in line for a single lock to access/modify any item Hand-over-hand-locking (lock coupling) Introduce a lock for each node of a list Traversal involves handing over previous node's lock, acquiring the next node's lock... Improves lock granularity Degrades traversal performance Consider hybrid approach Fewer locks, but more than 1 Best lock-to-node distribution? TCSS422: Operating Systems [Spring 2025] School of Engineering and Technology, University of Washington - Tacoma May 6, 2025 111 30

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| Improvement beyond a single master lock for a queue (FIFO) | Two locks: | One for the head of the queue | One for the tall | Synchronize enqueue and dequeue operations | Add a dummy node | Allocated in the queue initialization routine | Supports separation of head and tail operations | Items can be added and removed by separate threads at the same time | May 6, 2025 | TCSS422: Operating Systems [Spring 2025] | School of Engineering and Technology, University of Washington - Tacoma | 111.32 | 111.32 |

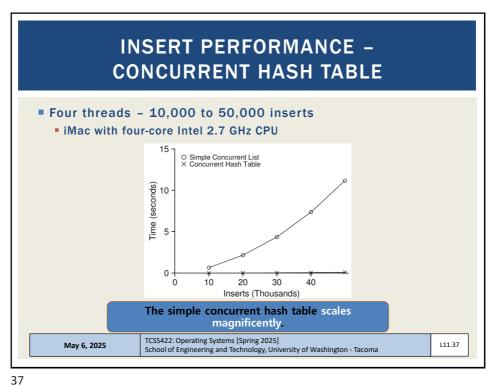


```
CONCURRENT QUEUE - 2
Add to queue
          (Cont.)
         21
                    void Queue_Enqueue(queue_t *q, int value) {
    node_t *tmp = malloc(sizeof(node_t));
         22
                              assert(tmp != NULL);
         23
         24
         25
                             tmp->value = value;
         26
                             tmp->next = NULL;
         27
         28
                             pthread mutex lock(&g->tailLock);
                             q->tail->next = tmp;
         30
                             q->tail = tmp;
         31
                             pthread_mutex_unlock(&q->tailLock);
          32
          (Cont.)
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                                                                                                L11.34
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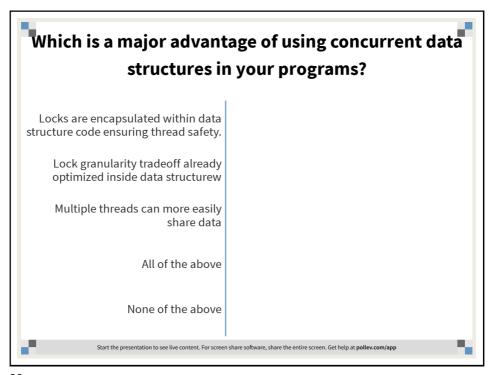
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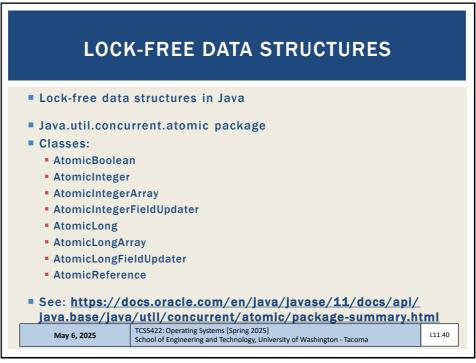
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CONCURRENT HASH TABLE Consider a simple hash table Fixed (static) size Hash maps to a bucket Bucket is implemented using a concurrent linked list One lock per hash (bucket) Hash bucket is a linked lists TCSS422: Operating Systems [Spring 2025] School of Engineering and Technology, University of Washington - Tacoma

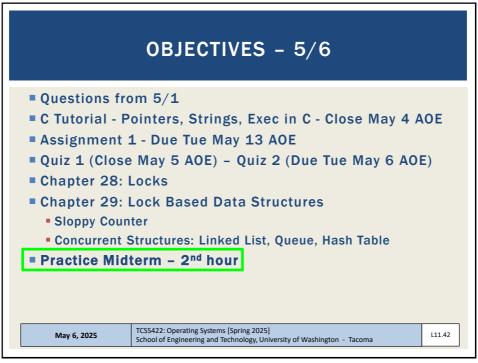


```
CONCURRENT HASH TABLE
               #define BUCKETS (101)
               typedef struct __hash_t {
    list_t lists[BUCKETS];
   3
               } hash_t;
               void Hash_Init(hash_t *H) {
                          int i;
                          for (i = 0; i < BUCKETS; i++) {</pre>
                                     List_Init(&H->lists[i]);
   11
   12
               }
   13
               int Hash_Insert(hash_t *H, int key) {
    int bucket = key % BUCKETS;
   14
   15
   16
                         return List_Insert(&H->lists[bucket], key);
   17
   18
               int Hash_Lookup(hash_t *H, int key) {
    int bucket = key % BUCKETS;
   19
   20
    21
                          return List Lookup(&H->lists[bucket], key);
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                                                                                                 L11.38
```



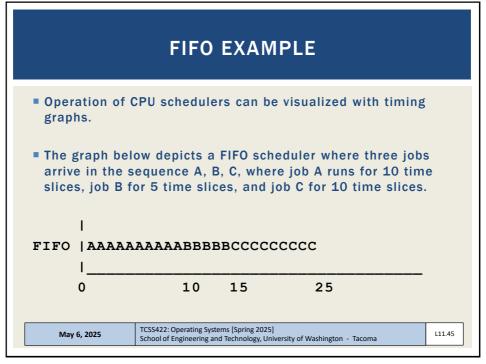


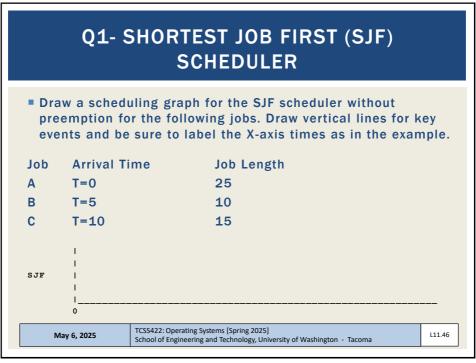






MIDTERM ■ Thursday May 8th ■ Meet in BHS 106 (2.0 hrs 3:40 - 5:40p) Test designed to take less than 2 hours ■ Three pages of notes, double-sided, any-size paper permitted No book, other notes, cell phones, or internet ■ Basic calculators OK ■ Individual work Coverage: up through Chapter 29 Preparation: Practice quiz: Quiz 2: CPU scheduling (posted) Auto grading w/ multiple attempts allowed as study aid Practice Midterm Questions - second hour of lecture Series of problems presented with some time to solve Will then work through solutions TCSS422: Operating Systems [Spring 2025] School of Engineering and Technology, University of Washington - Tacoma May 6, 2025 L11.44





	Q1 - SJF - 2
What is the resp jobs A, B, and C	onse time (RT) and turnaround time (TT) for ?
RT Job A:	TT Job A:
RT Job B:	TT Job B:
RT Job C:	TT Job C:
What is the aver	age response time for all jobs?
What is the aver	age turnaround time for all jobs?
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Q2 - SHORTEST TIME TO COMPLETION FIRST (STCF) SCHEDULER				
the fo Draw	ollowing job	es for key events and be sure to label the X-axis	r	
Job A B C		me Job Length 25 10 15		
CPU	 			
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Q2 - STCF - 2		
What is the response time (RT) and turnaround time (TT) for jobs A, B, and C?		
RT Job A: TT Job A:	•	
RT Job B: TT Job B:	•	
RT Job C: TT Job C:		
■ What is the average response time for all jobs?		
■ What is the average turnaround time for all jobs?		
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Q3 - OPERATING SYSTEM APIS		
1. Provide a def	inition for what is a blocking API call	
2. Provide a def	inition for a non-blocking API call	
	cample of a blocking API call. sed to manage processes and/or threads.	
 Provide an example of a non-blocking API call. Consider APIs used to manage processes and/or threads. 		
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Q4 - OPERATING SYSTEM APIs - II

- 1. When implementing memory synchronization for a multi-threaded program list one advantage of combining the use of a condition variable with a lock variable via the Linux C thread API calls: pthread_mutex_lock() and pthread_cond_wait()
- 2. When implementing memory synchronization for a multi-threaded program using locks, list one disadvantage of using blocking thread API calls such as the Linux C thread API calls for: pthread_mutex_lock() and pthread_cond_wait()
- 3. List (2) factors that cause Linux blocking API calls to introduce **overhead** into programs:

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L11.51

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Q5 - PERFECT MULTITASKING OPERATING SYSTEM

In a perfect-multi-tasking operating system, every process of the same priority will always receive exactly $1/n^{th}$ of the available CPU time. Important CPU improvements for multi-tasking include: (1) fast context switching to enable jobs to be swapped in-and-out of the CPU very quickly, and (2) the use of a timer interrupt to preempt running jobs without the user voluntarily yielding the CPU. These innovations have enabled major improvements towards achieving a coveted "Perfect Multi-Tasking System".

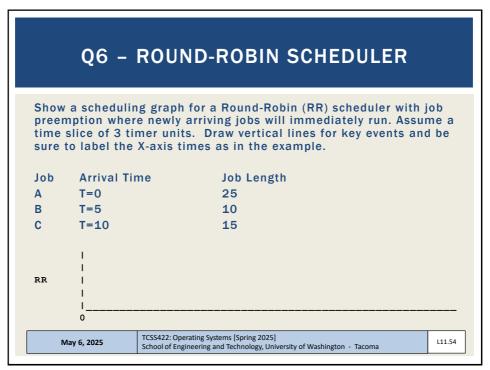
List and describe two challenges that remain complicating the full realization of a Perfect Multi-Tasking Operating System. In other words, what makes it very difficult for all jobs (for example, 10 jobs) of the same priority to receive **EXACTLY** the same runtime on the CPU? Your description must explain why the challenge is a problem for achieving perfect multi-tasking.

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L11.52





Q6 - RR SCHEDULER - 2

Using the graph, from time t=10 until all jobs complete at t=50, evaluate Jain's Fairness Index:

Jain's fairness index is expressed as:

$$\mathcal{J}(x_1,x_2,\ldots,x_n) = rac{(\sum_{i=1}^n x_i)^2}{n\cdot\sum_{i=1}^n x_i{}^2}$$

Where n is the number of jobs, and x_i is the time share of each process Jain's fairness index=1 for best case fairness, and 1/n for worst case fairness.

For the time window from t=10 to t=50, what percentage of the CPU time is allocated to each of the jobs A, B, and C?

Job A: _____ Job B: ____ Job C: ____

With these values, calculate Jain's fairness index from t=10 to t=50.

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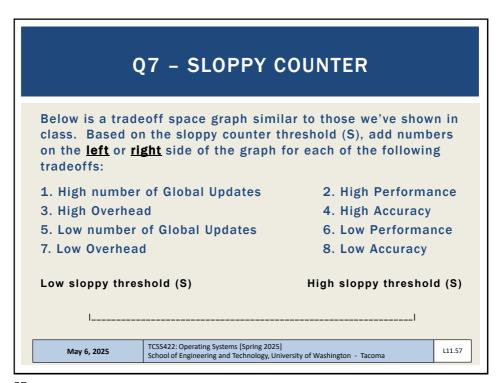
Q6 - II

$$\mathcal{J}(x_1, x_2, \dots, x_n) = rac{(\sum_{i=1}^n x_i)^2}{n \cdot \sum_{i=1}^n x_i{}^2}$$

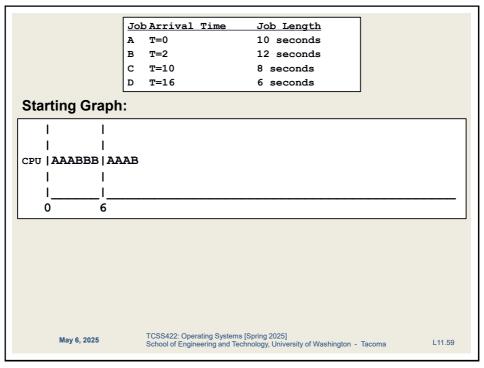
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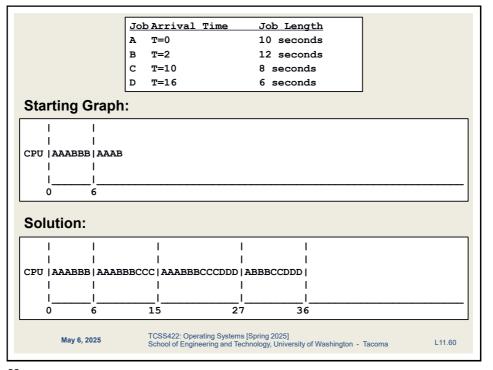
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Q8 - ROUND ROBIN SCHEDULER Consider a round-robin (RR) scheduler where upon new job arrival, the scheduler does not perform a context switch, but places the new job at the back of the RR queue. When the current job finishes its time quantum, a context switch is performed to execute the next job in the RR queue. ■ The RR-scheduler has a 3-sec time slice. Draw a scheduling graph for the following jobs. Job Arrival Time Job Length A T=0 10 seconds T=2 12 seconds T=10 8 seconds T=16 6 seconds TCSS422: Operating Systems [Spring 2025] May 6, 2025 111 58 School of Engineering and Technology, University of Washington - Tacoma



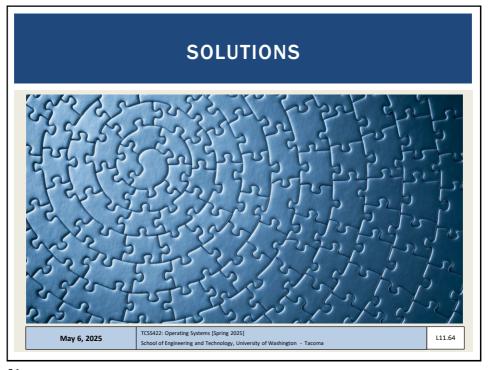


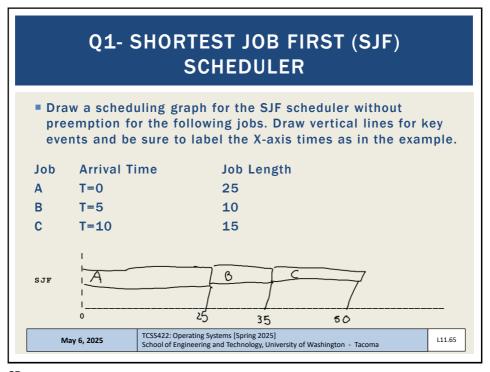
Q8 PART B - ROUND ROBIN SCHEDULER
Using the graph, calculate the turnaround time for each job, and the average turnaround time
■ TT Job A: AVG TT:
■ TT Job B:
■ TT Job C:
■ TT Job D:
Calculate the response time for each job, and the average response time
■ RT Job A: AVG RT:
■ RT Job B:
■ RT Job C:
■ RT Job D:
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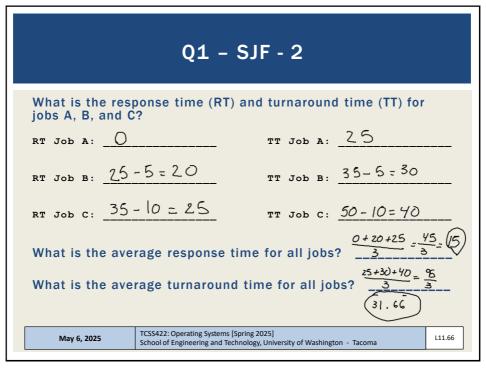
Q8 PART B - ROUND ROBIN SCHEDULER Using the graph, calculate the turnaround time for each job, and the average turnaround time ■ TT Job A: <u>28-0=28</u> AVG TT: <u>100/4=25</u>_ ■ TT Job B: <u>31-2=29</u> ■ TT Job C: <u>33-10=23</u> ■ TT Job D: <u>36-16=20</u> Calculate the response time for each job, and the average response time ■ RT Job A: ___0___ AVG RT: 11/3=3.66 ■ RT Job B: <u>3-2 = 1</u> ■ RT Job C: <u>12-10=2</u> ■ RT Job D: <u>24-16=8</u> TCSS422: Operating Systems [Spring 2025] School of Engineering and Technology, University of Washington - Tacoma May 6, 2025 L11.62

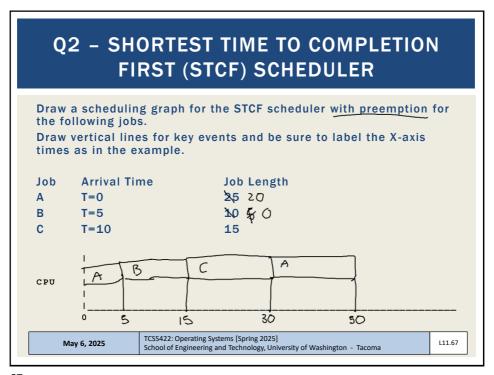
MULTI-LEVEL FEEDBACK QUEUE Review the bonus lecture for scheduling examples including several Multi-level-feedback-queue problems (MLFQ) Shortcut to Zoom recording of practice session: https://tinyurl.com/422s25-practice

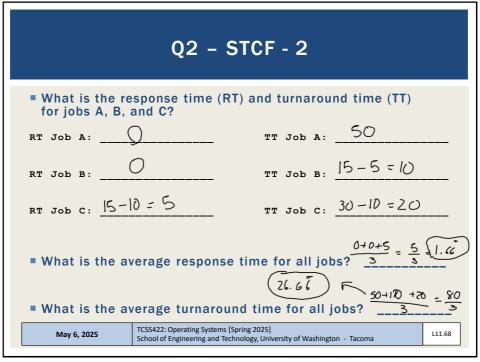
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03 - OPERATING SYSTEM APIS

- 1. Provide a definition for what is a blocking API call AN API call that suspends the calling thread to wait for a system interrupt to FIRE when an event occups. Calling thread foes to sleep. Furnish BLOCKED
- 2. Provide a definition for a non-blocking API call AN API CALL that DOES NOT SUSPEND the CALLING Thread, but returns quickly AND DOES NOT WAIT FOR AN INTERRUPT TO OCCUR POR EVENT
 - 3. Provide an example of a blocking API call. Consider APIs used to manage processes and/or threads. or thes? pthread_mutex_lock() wait () wait pol()
 - others (4. Provide an example of a non-blocking API call. Consider APIs used to manage processes and/or threads. pthread_mutex_try(ockc) fork()

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Q4 - OPERATING SYSTEM APIs - II

1. When implementing memory synchronization for a multi-threaded program list one advantage of combining the use of a condition variable with a lock variable via the Linux C

thread API calls: pthread_mutex_lock() and pthread_cond_wait() The combination ensures the order that blocked threads waiting for the lock will be 2. When implementing memory synchronization for a

- multi-threaded program using locks, list one disadvantage of using blocking thread API calls such as the Linux C thread API calls for: pthread_mutex_lock() and pthread_cond_wait()
- w/ pthread_mutex_loct the lock may never become available resulting in 3. List (2) factors that cause Linux blocking APP calls to

introduce overhead into programs: WITH FINC-GRAINED LOUTUNG, MANY CALLS TO CHULLA ANDRE LOUT APTS TO SYNCHRIPTE CRHICAL SECTIONS WILL INCREASE OVERHEAD - blockwas APTS MUST Trap + context switch andre and in Kermon Entropent more overhead

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Q5 - PERFECT MULTITASKING OPERATING SYSTEM

In a perfect-multi-tasking operating system, every process of the same priority will always receive exactly $1/n^{\text{th}}$ of the available CPU time. Important CPU improvements for multi-tasking include: (1) fast context switching to enable jobs to be swapped in-and-out of the CPU very quickly, and (2) the use of a timer interrupt to preempt running jobs without the user voluntarily yielding the CPU. These innovations have enabled major improvements towards achieving a coveted "Perfect Multi-Tasking System".

List and describe two challenges that remain complicating the full realization of a Perfect Multi-Tasking Operating System. In other words, what makes it very difficult for all jobs (for example, 10 jobs) of the same priority to receive **EXACTLY** the same runtime on the CPU? Your description must explain why the challenge is a problem for achieving perfect multi-tasking.

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L11.71

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2 challenges for Perfect MULTITASING

- JOBS ARRIVE AT DIFFORUTT TIMES AND RUN FOR DIFFORENT LENGTHS
MAKING IT MORE DIFFICULT TO PERFECTLY BALANCE RUNTIME FOR JOBS
IN the SAME PRIORITY RULLE

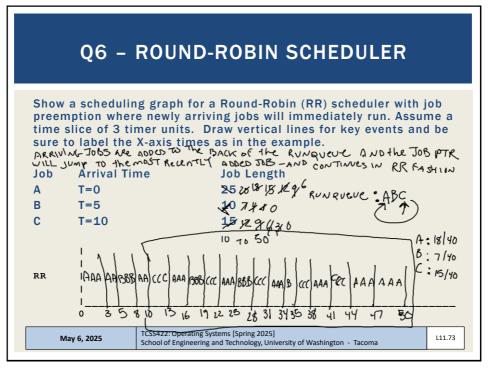
TOB ACCOUNTING (TRACKING TIME) INVOLVES OVER head - MEASUREMENTS MAY NOT be PRECISE (VRUNTIME)

over head of a c/s may Lead To Inconsistencies in JOB RUNTIME

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L11.72



Q6 - RR SCHEDULER - 2

Using the graph, from time t=10 until all jobs complete at t=50, evaluate Jain's Fairness Index:

Jain's fairness index is expressed as:

$$\mathcal{J}(x_1, x_2, \dots, x_n) = rac{(\sum_{i=1}^n x_i)^2}{n \cdot \sum_{i=1}^n x_i^2}$$

Where n is the number of jobs, and x_i is the time share of each process Jain's fairness index=1 for best case fairness, and 1/n for worst case fairness.

For the time window from t=10 to t=50, what percentage of the CPU time is allocated to each of the jobs A, B, and C?

Job A: $\frac{15}{40}$ Job B: $\frac{7}{40}$ Job C: $\frac{15}{40}$ 375

With these values, calculate Jain's fairness index from t=10 to t=50.

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$$Q6 - II$$

$$J(x_1, x_2, ..., x_n) = \frac{(\sum_{i=1}^n x_i)^2}{n \cdot \sum_{i=1}^n x_i^2} \quad \text{west} \quad \frac{1}{3} = .333$$

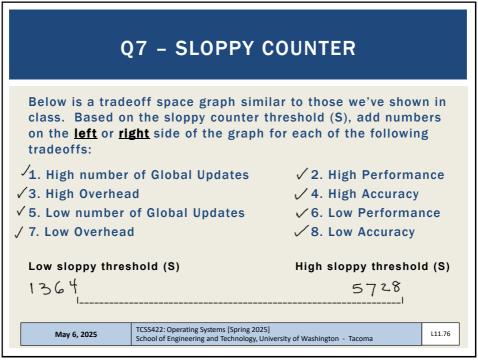
$$(.45 + .75 + .375) = (1)^2 = 1 \qquad \text{prefect} \quad 1$$

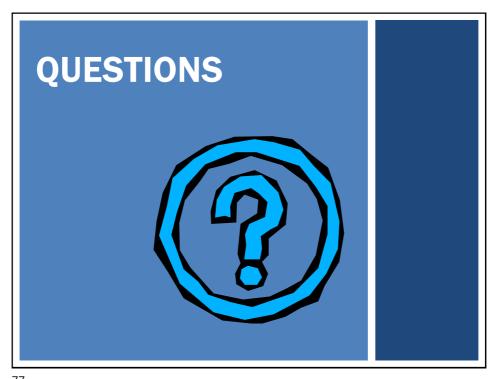
$$n \cdot \underbrace{\sum_{i=1}^n Y_i^2} \rightarrow 3 \cdot \left((.45)^2 + (.175)^2 + (.375)^2 \right)$$

$$3 \cdot \left(.2025 + .030625 + .140625 \right) \quad \frac{1}{1.12125}$$

$$3 \cdot \left(.37375 \right) \qquad \rightarrow .8418617$$

$$1.12125 \qquad \qquad 89.29$$
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