

# Robust Biologically Guided Radiation Therapy (BGRT)

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**Location:** Hotel Grand Chancellor, 65 Hindley Street, Adelaide, South Australia

**Website:** <http://www.rah.sa.gov.au/cancer/mot.php>

# Learning Objectives

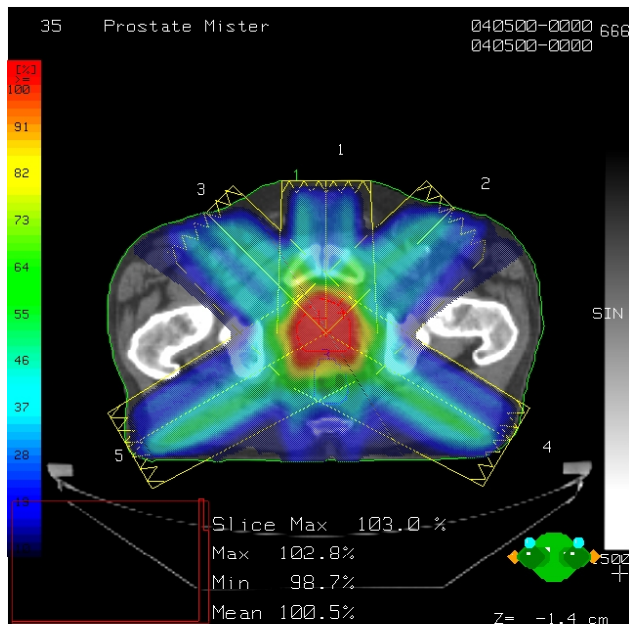
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- **Rationale for BGRT**
- **Are existing biological models “good enough” for clinical applications?**
  - Some of the challenges
  - Limitations and applicability of BED and EUD concepts with a focus on intra- and inter-patient heterogeneity
- **Examples**
  - Equivalent prescriptions
  - Plan ranking and comparison with EUD
- **This Presentation and Supplemental Slides**
  - <http://faculty.washington.edu/trawets/>

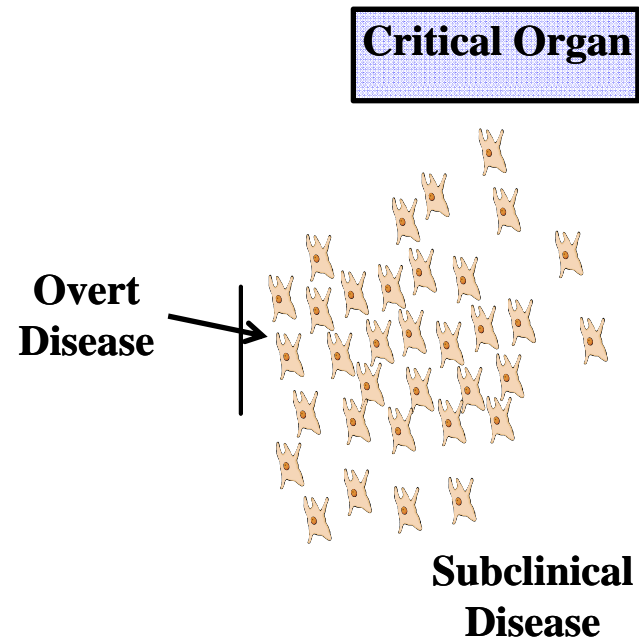
**Presenter has no conflicts of interest to disclose**

# Why isn't EBRT more successful?

- **Uncertainty in boundary of primary tumor**
- **Inability to delivery a tumoricidal dose**
- **Migration of diseased cells to other body parts**



**Dose escalation not always possible**



# Motivation for BGRT

How do we get the most bang for our buck (*dose*)?

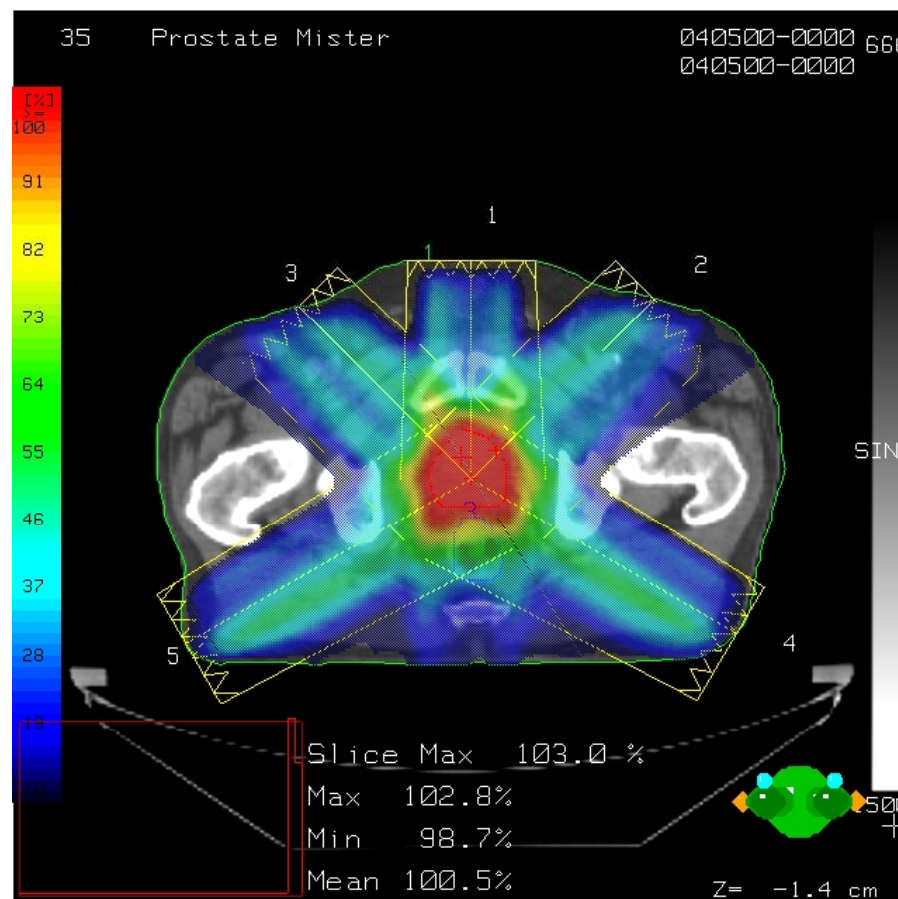


**Outcome Prediction**

**or**

***“Biological Metrics”***

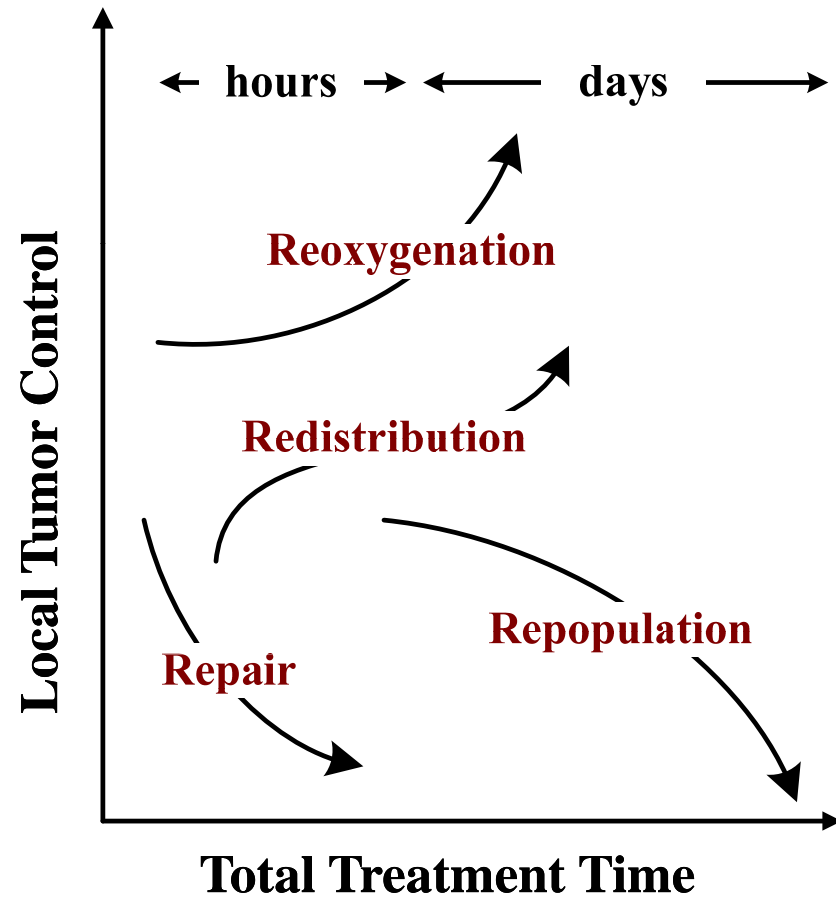
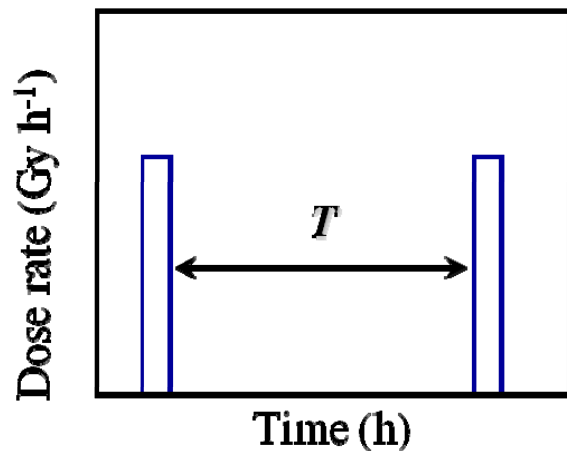
A way to rank the *relative* efficacy of alternate and competing treatments



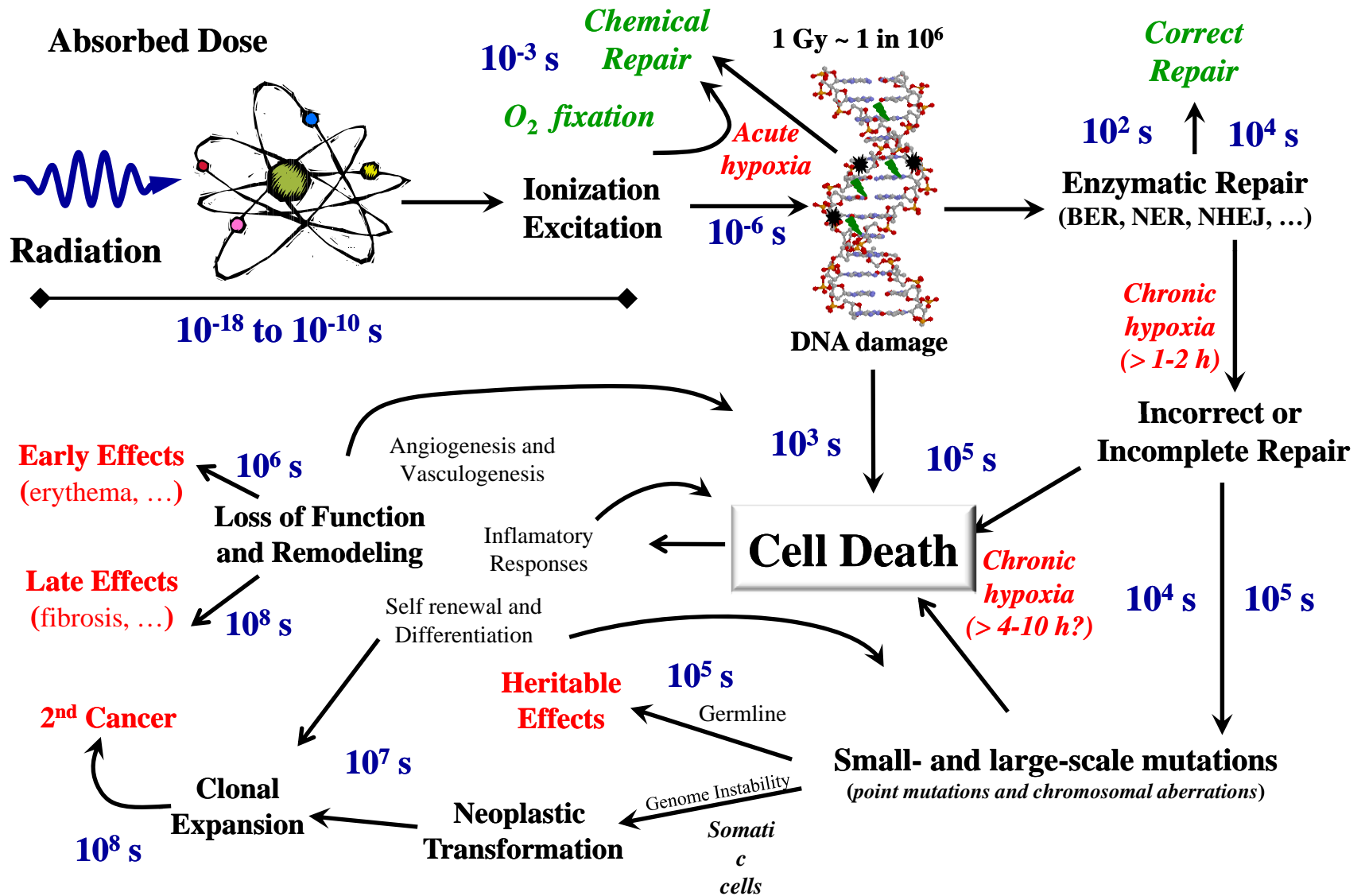
When local control cannot be achieved through dose escalation, only RT option is to move the dose around in space and/or time.

# Four R's of Radiobiology (*conventional wisdom*)

- **R**epair (↓)
- **R**epopulation (↓)
- **R**edistribution (↑)
- **R**eoxygenation (↑)



# Physics → Chemistry → Biology → Clinic



# The LQ in Radiation Therapy

Inaccurate and too simplistic (*compared to known biology*)

$$S(D) = \exp(-\alpha D - \beta G D^2)$$

one-hit damage  $\rightarrow$   $\alpha D$        $\beta G D^2$   $\leftarrow$  inter-track damage interaction  
 Dose-rate and dose-fractionation effects (“dose protraction factor”)

Parameters (e.g.,  $\alpha$  and  $\beta$ ) derived from analysis of clinical outcomes are uncertain and averaged over a heterogeneous tumor and patient population

JF Fowler, R Chappell, M Ritter,  
IJROBP **50**, 1021-1031 (2001)

$$\alpha = 0.039 \text{ Gy}^{-1}$$

$$\alpha/\beta = 1.49 \text{ Gy}$$

$$S = 1.159 \times 10^{-3} (37 \times 2 \text{ Gy})$$

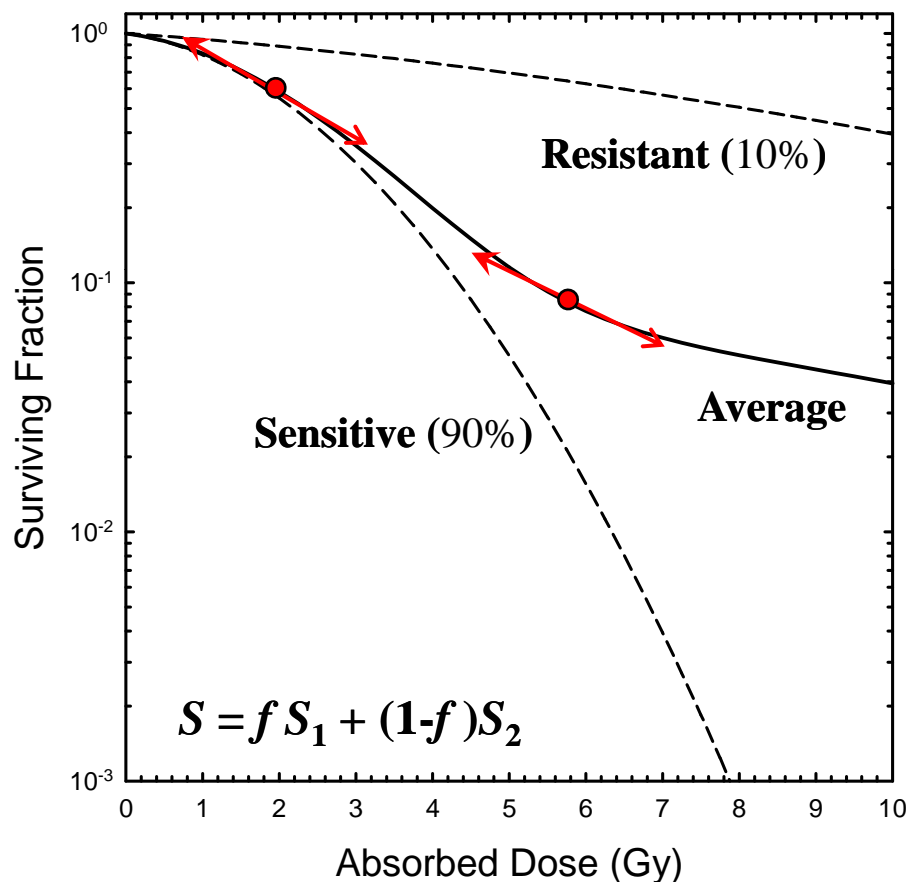
JZ Wang, M Guerrero, XA Li,  
IJROBP **55**, 194-203 (2003)

$$\alpha = 0.15 \text{ Gy}^{-1} \quad (4X \text{ higher})$$

$$\alpha/\beta = 3.1 \text{ Gy} \quad (2X \text{ higher})$$

$$S = 2.677 \times 10^{-8} \quad (10^4 \text{ smaller})$$

# SF for a Heterogeneous Cell Population

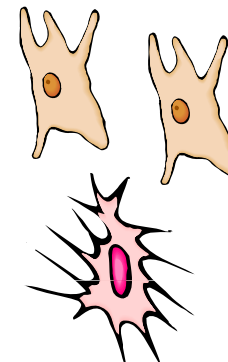


Can't use a single (*average*) set of LQ radiation sensitivity parameters ( $\alpha, \alpha/\beta$ ) to predict overall shape of dose-response curve

$$S \neq \exp(-\alpha D - \beta G D^2)$$

Five Reasons (*many others possible*)

- Genomic Instability
- Repair
- Repopulation
- Reassortment
- Reoxygenation



**But may be reasonable to extrapolate from a known point?**



# Poisson Tumor control probability (TCP)

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Most widely used model assumes that the distribution of the number of tumor cells surviving a treatment is adequately described by a Poisson distribution

$$\text{TCP} = \exp\{-\rho VS(D)\}$$

Chance no tumor cells survive a treatment that delivers total dose  $D$

$\rho$  = number of tumor cells per unit volume ( $< 10^9$  cells  $\text{cm}^{-3}$ )

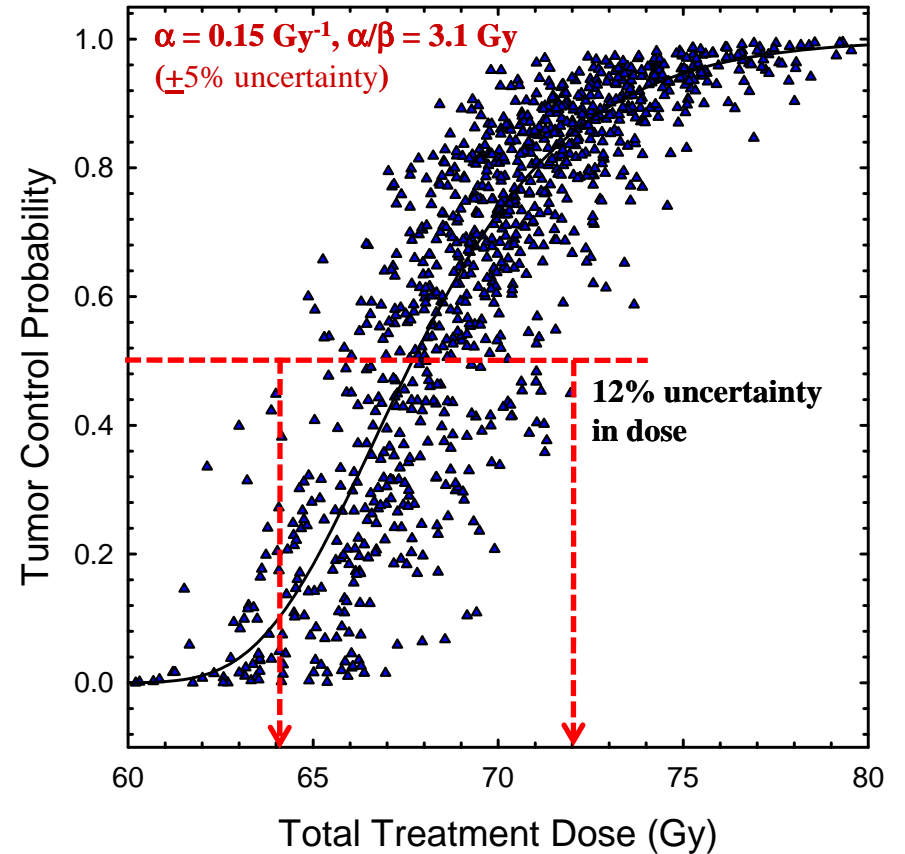
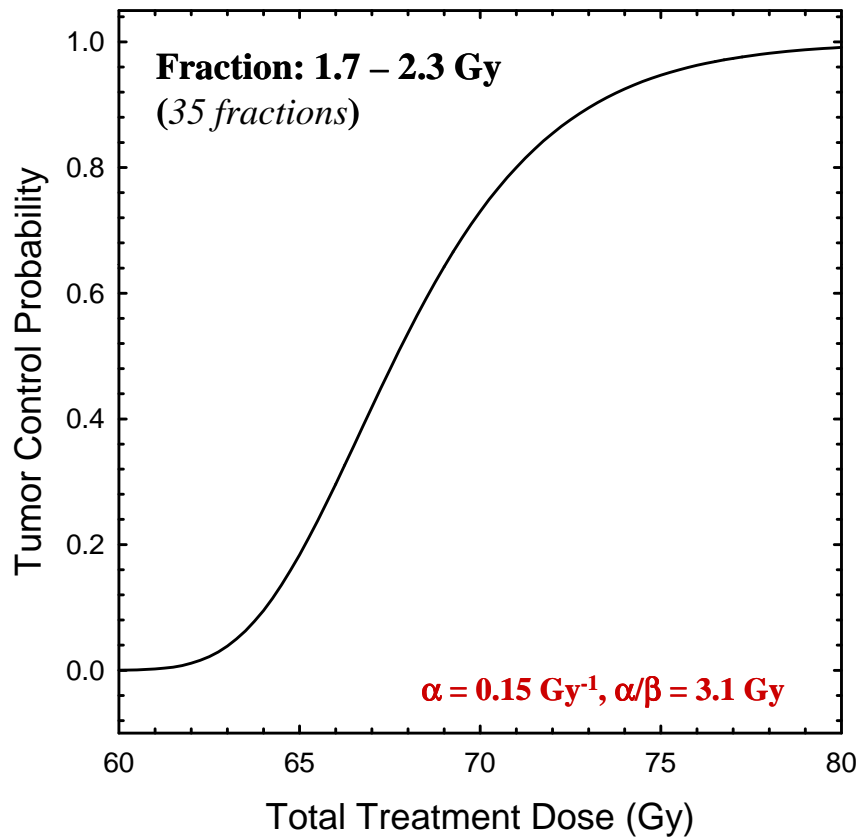
$V$  = tumor volume (GTV? CTV? PTV?)

product  $\rho V$  = pre-treatment number of tumor cells

Typical uncertainty? **Factors as large as  $10^3$  to  $10^6$ !**

**Eradication of some cells, such as cancer stem cells, may be far more important than the eradication of others (effective  $\rho \ll 10^9$  cells  $\text{cm}^{-3}$ ?)**

# Prediction of Local Tumor Control



**Even small levels of uncertainty in the biological parameters ( $\alpha$  and  $\alpha/\beta$ ) have a big impact on our ability to predict the chance we achieve tumor control**

# Outcomes for a Patient Population?



<http://www.cartoonaday.com/images/cartoons/2010/03/Crowd-of-Cartoon-Sports-FansA-598x429.jpg>

## Equivalent Prescriptions (*tumor*)

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What dose should be delivered to achieve the same level of biological damage as another treatment?

*Reference Treatment*      *Alternate Treatment*

$$TCP(D_R) = TCP(D)$$

$$\exp(-\rho VS(D_R)) = \exp(-\rho VS(D)) \quad \text{Poisson TCP model}$$

$$\rho = \text{cell density (\# cm}^{-3}\text{)} \quad V = \text{tumor volume (cm}^3\text{)}$$

When comparing or ranking plans in the *same patient*,  $\rho$  and  $V$  may be considered *modality and plan independent constants* (same number of diseased cells regardless of modality and plan).

$$S(D_R) = S(D) \quad \text{Two biological parameters (\rho and V) eliminated from modeling process (uncertainty in } \rho V \text{ doesn't matter!)}$$

**For individual patients, iso-TCP = iso-survival**

# Equivalent dose derived from the LQ

*Reference Treatment = Alternate Treatment*

$$S(D_R) = S(D)$$

$\alpha$  and  $\beta$  (or  $\alpha/\beta$ ) characterize  
*intrinsic radiation sensitivity*

$$\exp(-\alpha D_R - \beta G D_R^2) = \exp(-\alpha D - \beta G D^2) \quad G \text{ is the dose protraction factor}$$

↓ Take logarithm, apply quadratic formula  
and rearrange terms

$$D = \frac{\alpha / \beta}{2G} \left\{ -1 + \sqrt{1 - \frac{4G \ln S(D_R)}{\alpha(\alpha / \beta)}} \right\} = \frac{\alpha / \beta}{2G} \left\{ -1 + \sqrt{1 + \frac{4G D_R}{(\alpha / \beta)} \left( 1 + \frac{G_R D_R}{\alpha / \beta} \right)} \right\}$$

$D$  is the total treatment dose needed to achieve same biological effect as a reference treatment that delivers total dose  $D_R$

Determined by the value of  $\alpha/\beta$  and the dose protraction factor for the reference and alternate treatments ( $G_R$  and  $G$ )

# Equivalent Treatment Schedules

$$D = \frac{\alpha / \beta}{2G} \left\{ -1 + \sqrt{1 + \frac{4GD_R}{(\alpha / \beta)} \left( 1 + \frac{G_R D_R}{\alpha / \beta} \right)} \right\} \quad \begin{array}{l} G \cong 1/n \\ G \cong 1/n_R \end{array}$$

Determine biologically equivalent dose  $D$  by adjusting the physical parameter  $n$

$$D = \frac{n}{2} (\alpha / \beta) \left\{ -1 + \sqrt{1 + \frac{4D_R}{n(\alpha / \beta)} \left( 1 + \frac{D_R}{n_R(\alpha / \beta)} \right)} \right\}$$

**Reference Treatment**  
 (“clinical experience”)

$D_R$  = total dose (Gy)

$n_R$  = number fractions

$d_R = D_R/n_r$  (fraction size)

***New (alternate) Treatment***

$n$  = desired number fractions

Uncertainty in  $D$  mainly arises from uncertainties associated with  $\alpha/\beta$ .

# Biologically Effective Dose (BED)

How is an iso-effective physical dose related to BED?

$$D = \frac{\alpha / \beta}{2G} \left\{ -1 + \sqrt{1 - \frac{4G \ln S(D_R)}{\alpha(\alpha / \beta)}} \right\}$$

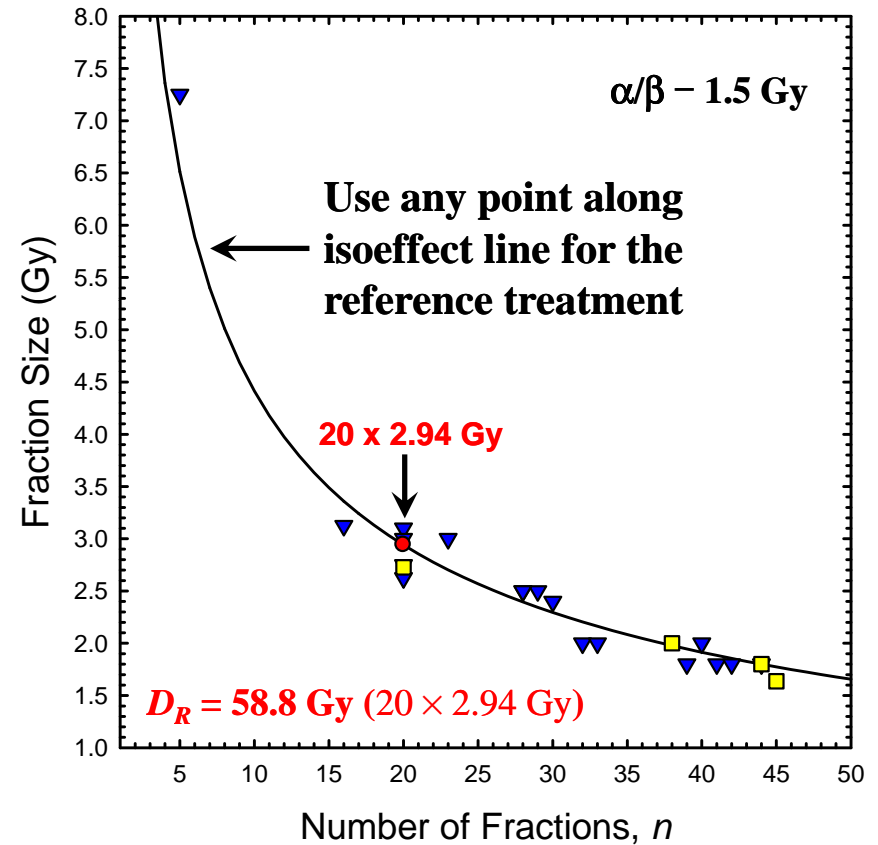
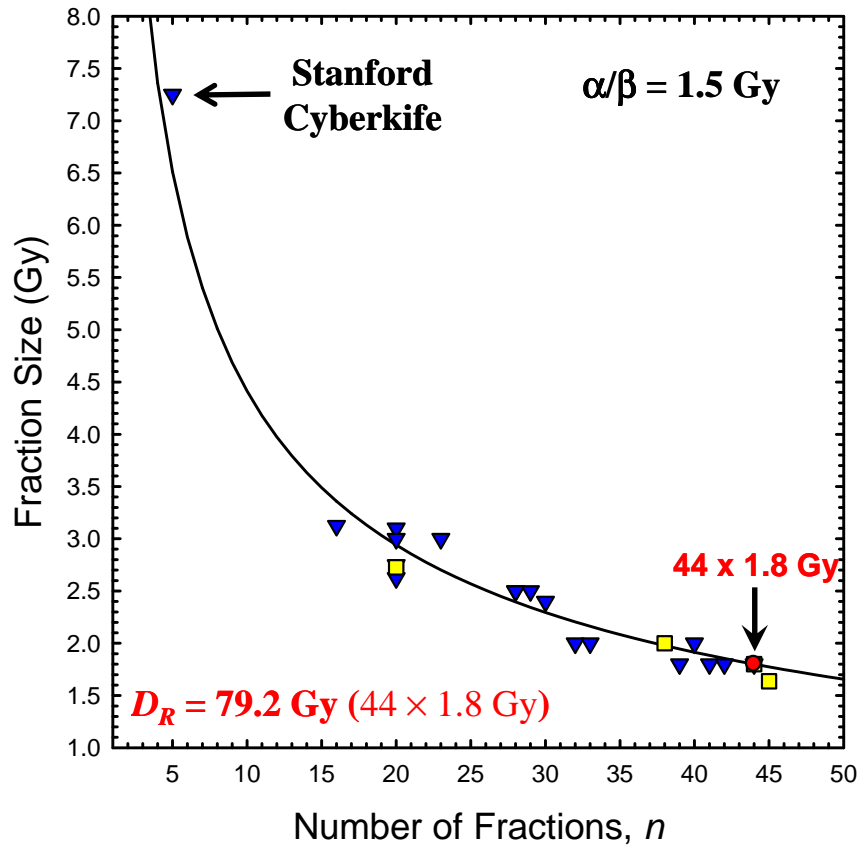
$$= \frac{\alpha / \beta}{2G} \left\{ -1 + \sqrt{1 + \frac{4G}{(\alpha / \beta)} D_R \left( 1 + \frac{d_R}{\alpha / \beta} \right)} \right\} \quad \text{No repopulation effects}$$

$$D = \frac{\alpha / \beta}{2G} \left\{ -1 + \sqrt{1 + \frac{4G}{\alpha / \beta} D_R \left[ 1 + \frac{d_R}{\alpha / \beta} - \frac{\gamma(T_R - T)}{\alpha D_R} \right]} \right\}$$

Correction for exponential repopulation without time lag



# Equivalent Treatments (*prostate cancer*)



$$D = \frac{n}{2} (\alpha / \beta) \left\{ -1 + \sqrt{1 + \frac{4D_R}{n(\alpha / \beta)} \left( 1 + \frac{D_R}{n_R(\alpha / \beta)} \right)} \right\}$$



# Inter-Patient Heterogeneity

$$D = \frac{n}{2}(\alpha / \beta) \left\{ -1 + \sqrt{1 + \frac{4D_R}{n(\alpha / \beta)} \left( 1 + \frac{D_R}{n_R(\alpha / \beta)} \right)} \right\}$$

When applied to a patient population, we are implicitly assuming that  $\alpha/\beta$  is the same for *all patients* for the reference *and* alternate treatment – an assumption that is *surely* incorrect!

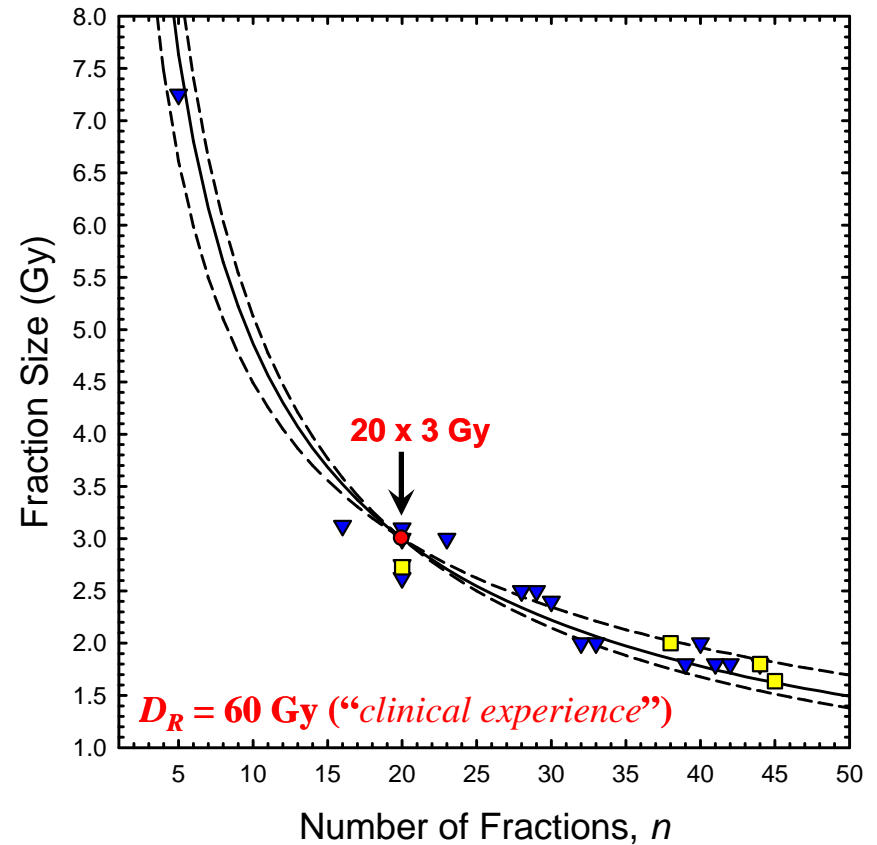
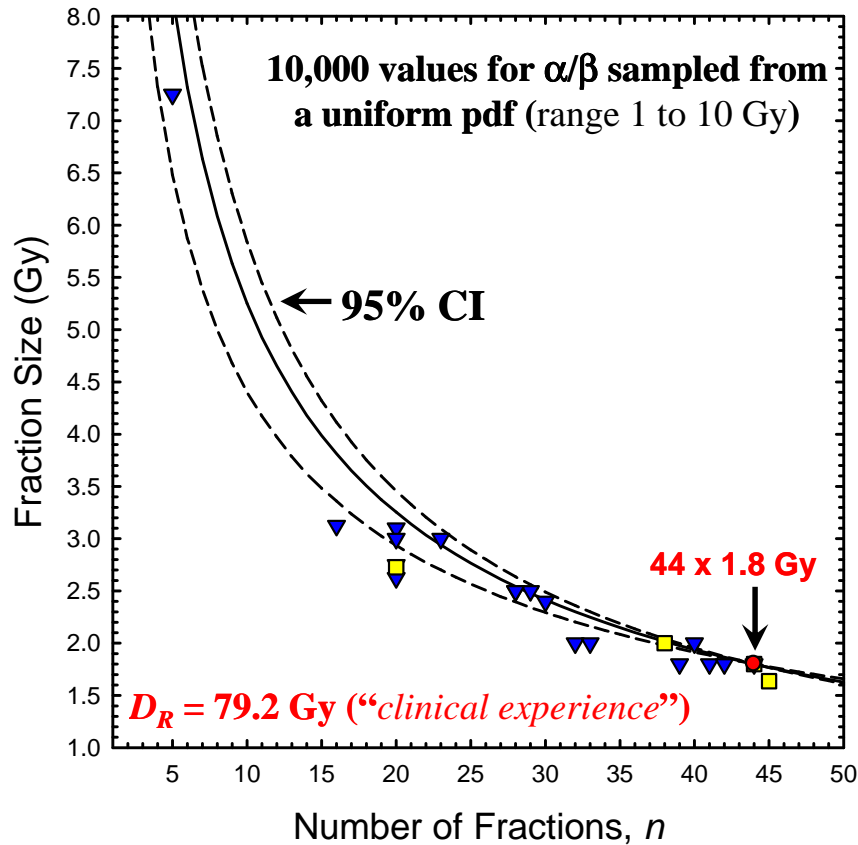
## *Inter-Patient Heterogeneity*

**Thought Experiment:** All patients (*tumors*) have a different effective  $\alpha/\beta$  (*unknown distribution*). BUT... same value of  $\alpha/\beta$  is appropriate (*as a first approximation*) in the same patient for competing plans and modalities

How does inter-patient heterogeneity influence our ability to determine equivalent prescription dose?

How sensitive are estimates of  $D$  to uncertainties in  $\alpha/\beta$ ?

# Effects of Inter-Patient Heterogeneity



**Key Point #1:** Small changes from an accepted fractionation schedule quite reasonable – even for a *very* heterogeneous patient population

# Equivalent Uniform Dose (EUD)

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## Concept of an EUD introduced by A. Niemierko in 1997

**“It is intuitively logical that, for any inhomogeneous dose distribution delivered to a volume of interest (VOI) according to a certain fractionation scheme, there exists a unique uniform dose distribution delivered in the same number of fractions, over the same total time, which causes the same radiobiological effect.**

**The important feature of this equivalent dose distribution would be its uniformity, which allows one to use a *single number to describe the entire VOI dose distribution*. Of course, the equivalent dose depends on the considered effect.”**

**A. Niemierko, Reporting and analyzing dose distributions: a concept of equivalent uniform dose. *Med Phys.* 24(1), 103-110 (1997).**

## EUD for tumor control and cell survival

$$\exp(-\alpha EUD - \beta EUD^2) = \frac{1}{\rho V} \sum_{i=1}^N v_i \rho_i \exp(-\alpha_i D_i - \beta_i D_i^2)$$

To solve for EUD, take logarithm and apply quadratic formula

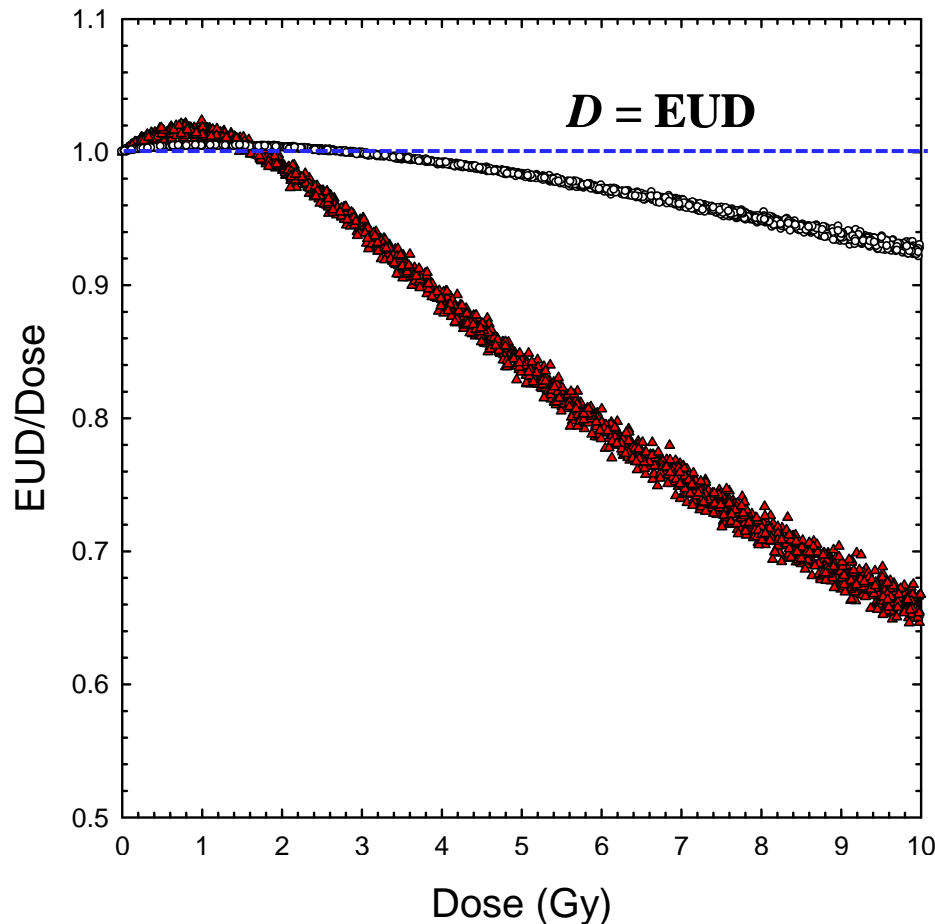


$$EUD = \frac{1}{2} \alpha / \beta \left( -1 + \sqrt{1 - \frac{4 \ln \bar{S}}{\alpha(\alpha / \beta)}} \right) = \frac{1}{2} \alpha / \beta \left( -1 + \sqrt{1 + \frac{4 BED_{het}}{(\alpha / \beta)}} \right)$$

$$\bar{S} \equiv \frac{1}{\rho V} \sum_{i=1}^N v_i \rho_i \exp(-\alpha_i D_i - \beta_i D_i^2)$$

Delivery of dose = EUD to all  $i$  regions will produce same surviving fraction and level of tumor control as heterogeneous dose distribution (array of  $D_i$  values)

# EUD for a heterogeneous cell population



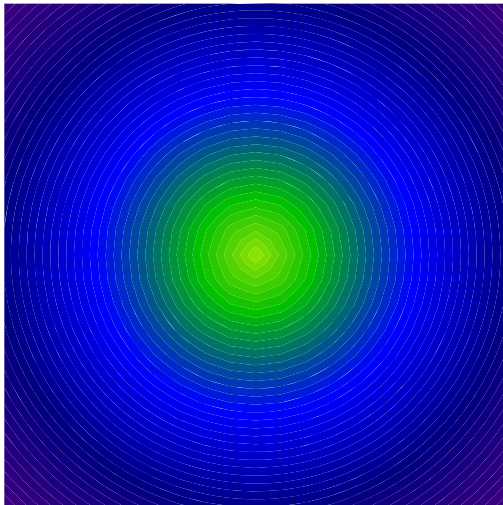
Individual filled symbols denote Monte Carlo sampling of the radiation response characteristics of 1000 cells given a uniform dose of radiation ( $x$ -axis).

Open circles:  $\alpha_i$  sampled from  $0.1 \text{ Gy}^{-1}$  to  $0.2 \text{ Gy}^{-1}$ ;  $(\alpha/\beta)_i$  sampled 2 to 4 Gy (population-average:  $\alpha = 0.15 \text{ Gy}^{-1}$ ,  $\alpha/\beta = 3 \text{ Gy}$ ).

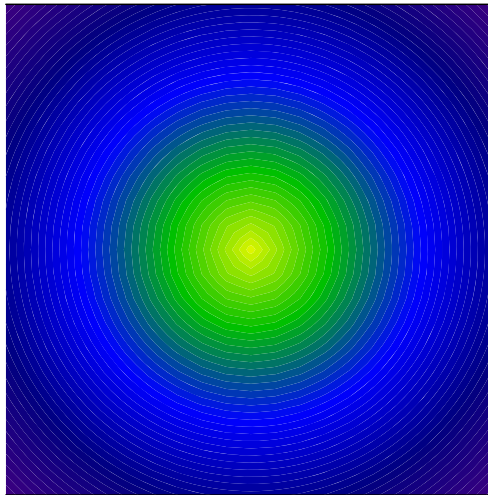
Filled Triangles:  $\alpha_i$  sampled from  $0.05 \text{ Gy}^{-1}$  to  $0.5 \text{ Gy}^{-1}$  and  $(\alpha/\beta)_i$  sampled from 1 to 10 Gy ( $\alpha = 0.275 \text{ Gy}^{-1}$ ,  $\alpha/\beta = 5.5 \text{ Gy}$ ).

# Effects of intra-tumor heterogeneity

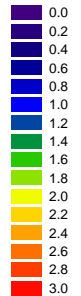
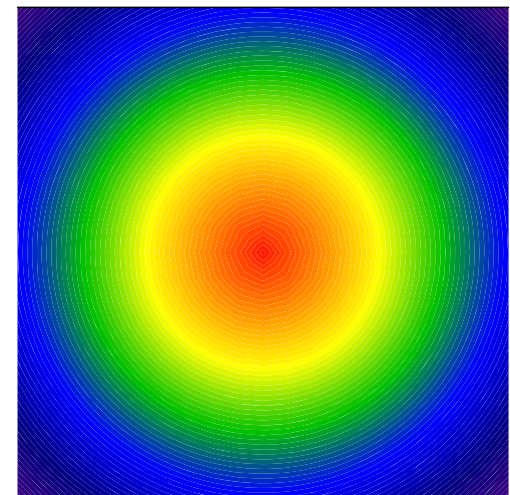
44 × 1.80 Gy (*original*)



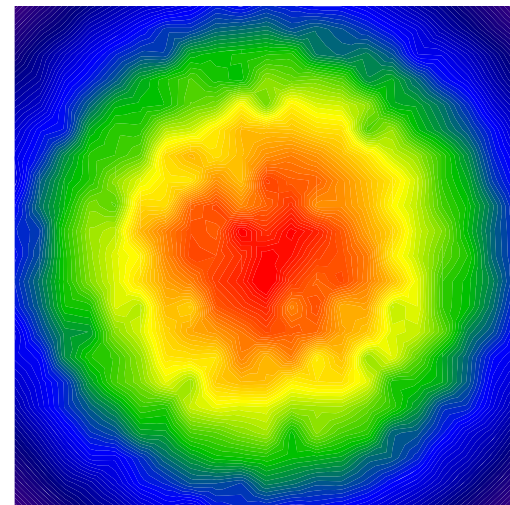
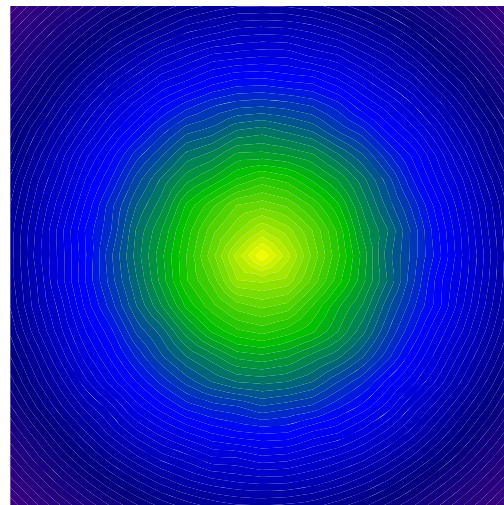
39 × 1.95 Gy ( $\alpha/\beta = 1.5$  Gy)



20 × 2.94 Gy ( $\alpha/\beta = 1.5$  Gy)



$\alpha/\beta$  sampled from a uniform pdf (1 to 10 Gy) on a voxel by voxel basis



## EUD for large dose per fraction

- So-called “generalized” gEUD neglects the  $\beta GD^2$  component of cell killing
  - Most of our knowledge of the effects of radiation on normal tissues comes from conventional (*low dose*) fractionation

**Step 1.** Convert 3D dose distribution for hypofractionated ( $n_R < 3-5$ ) treatment into equivalent conventional ( $n < 30-45$ ) 3D dose distribution

$$d = \frac{(\alpha / \beta)}{2} \left\{ -1 + \sqrt{1 + \frac{4d_R}{(\alpha / \beta)} \frac{n_R}{n} \left( 1 + \frac{d_R}{\alpha / \beta} \right)} \right\} \quad \text{Apply on voxel by voxel basis}$$

**Step 2.** Convert 3D dose distribution for conventional treatment into gEUD

$$gEUD = \left( \frac{1}{V} \sum_i v_i D_i^{1/a} \right)^a$$

$a = 1$  (*average dose*),  $a \rightarrow +\infty$  (*maximum dose*),  $a \rightarrow -\infty$  (*minimum dose*)

# Summary

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- **Absolute quantitative prediction of tumor control, complication rates and cell survival very sensitive to even small uncertainties in biological parameters**
  - Such models are (*and always will be*) a highly non-linear function of dose
- **For a heterogeneous patient (*or cell*) population, shapes of dose-response curve cannot be accurately modeled using the LQ and a single set of (*average*) radiosensitivity parameters**
  - Usefulness of alternate mathematical models usually offset by introduction of additional *ad hoc* biological parameters into modeling process
- **Direct use of TCP, NTCP models to compare and rank alternate plans and modalities may result in the selection of inappropriate or suboptimal treatments**
  - Also need to specify large number of biological inputs



## Robust BGRT – Key Points

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- **Many (all?) clinical questions can be usefully tackled using biological metrics (*doses*) derived from existing models**
  - Semi-quantitative *relative* plan ranking and comparison
- **Biological metrics derived by equating acceptable treatments to alternate ones**
  - Need to incorporate corrections for relevant biology into biological metrics (repopulation effects, LET effects, oxygen effects, low-dose hyper-radiation sensitivity, bystander effects, ...)
- **Isoeffect calculation are remarkably *insensitive* to uncertainties in biology parameters**
  - Assess the impact of uncertainties associated with biological parameters through Monte Carlo sampling (or other methods)
  - Uncertainties in biology offset by clinical judgment (i.e., the use of a “*reference treatment*”)

# Future of BGRT – Individualize and Adapt

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- **Patient imaging first part of treatment**
  - Estimate of *one or two* key biological parameters from patient imaging
- **Individualized isoeffect calculations**
  - Sample *other* biological parameters from probability distributions for an appropriate patient population
- **Individualize and adapt 2<sup>nd</sup> stage of treatment**
  - Compare and rank alternate plans and modalities for individual patients
    - ❖ Boost, alter modality (e.g., protons), re-size GTV or PTV, ...
  - Patient-specific cost-benefit analysis of adapted treatment
    - ❖ Is it worthwhile to alter the original plan?

## **Supplemental Slides**

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- **Repopulation Effects in External Beam Therapy**
- **Brachytherapy Isoeffect Calculations**
- **Derivation of EUD formula**

**This presentation along with the supplemental slides available at**

**<http://faculty.washington.edu/trawets/>**

# Equivalent dose – repair and repopulation

*Reference Treatment = Alternate Treatment*

$$S(D_R) = S(D)$$

$$\exp(-\alpha D_R - \beta G D_R^2 + \gamma T_R) = \exp(-\alpha D - \beta G D^2 + \gamma T)$$

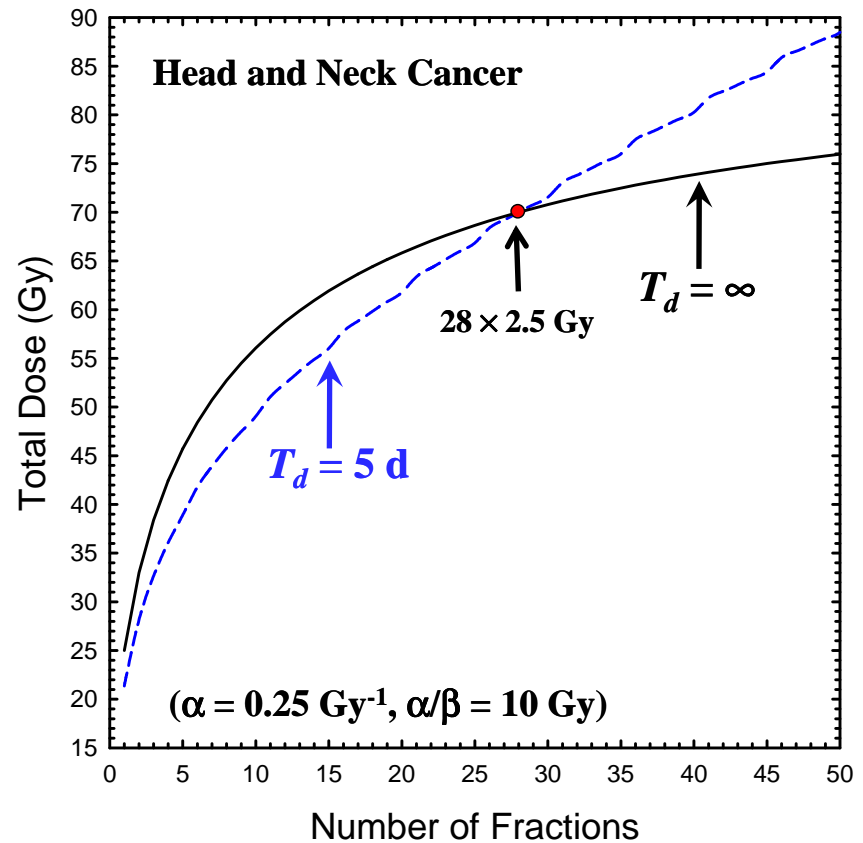
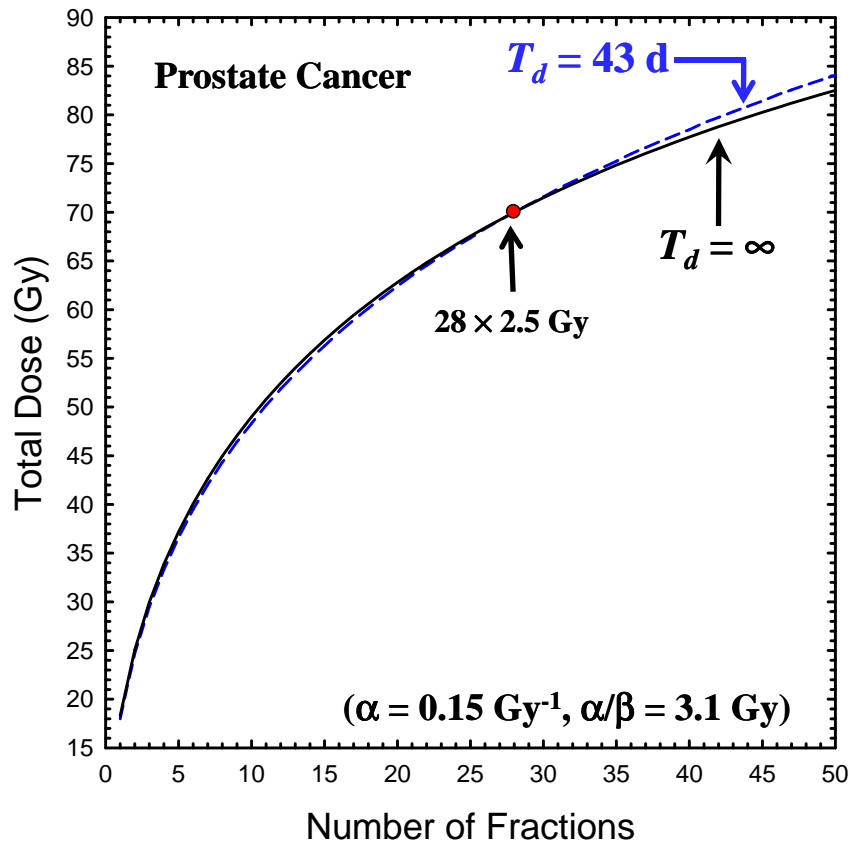
↓ Take logarithm, apply quadratic formula and rearrange terms

$$D = \frac{\alpha / \beta}{2G} \left\{ -1 + \sqrt{1 + \frac{4GD_R}{\alpha / \beta} \left[ 1 + \frac{G_R D_R}{\alpha / \beta} - \frac{\gamma(T_R - T)}{\alpha D_R} \right]} \right\}$$

**$D$**  is the total treatment dose needed to achieve same biological effect as a reference treatment that delivers total dose  **$D_R$**

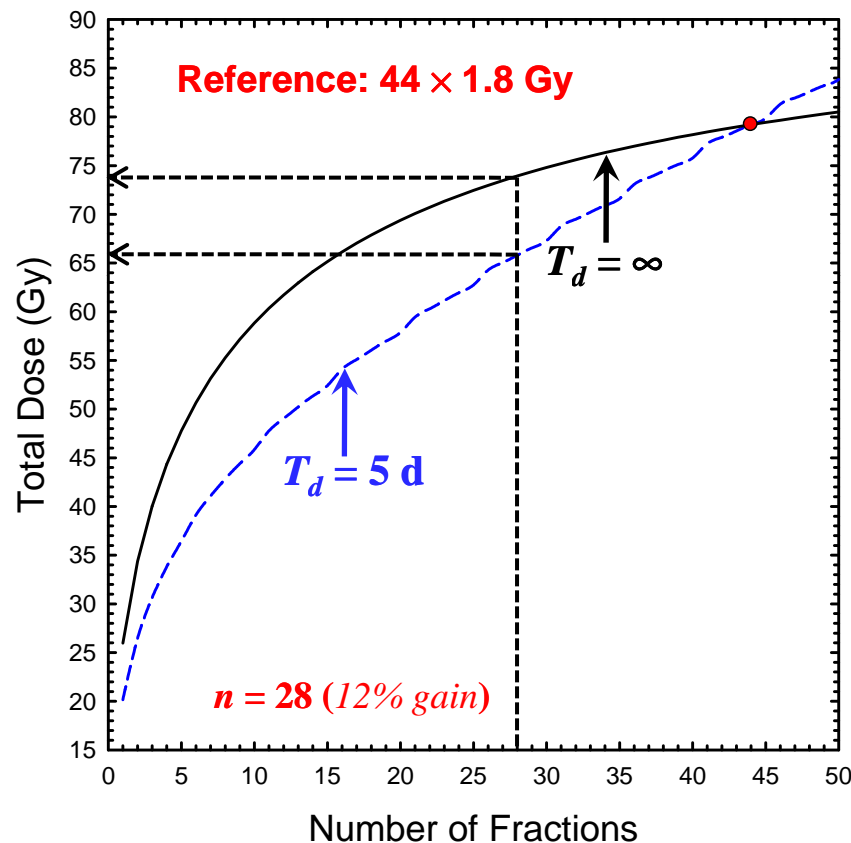
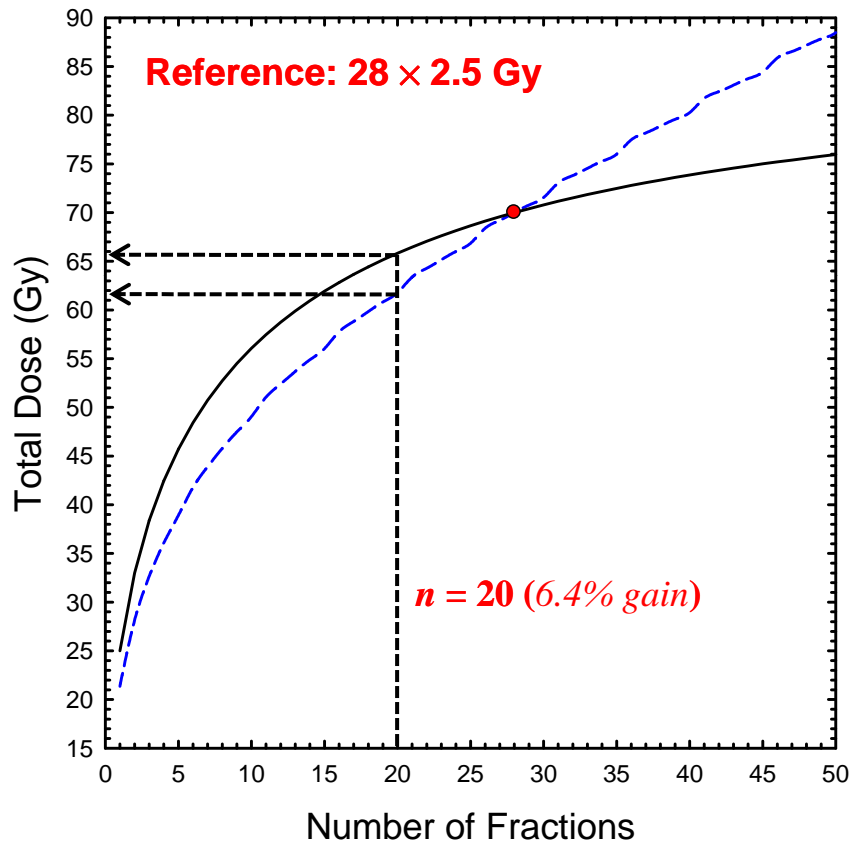
Determined by the value of  **$\alpha/\beta$**  (in Gy),  **$\gamma/\alpha$**  (in Gy/day) and the dose protraction factor for the reference and alternate treatments ( **$G$**  and  **$G_R$** )

# Repopulation Effects – Fast and Slow Growing Tumors



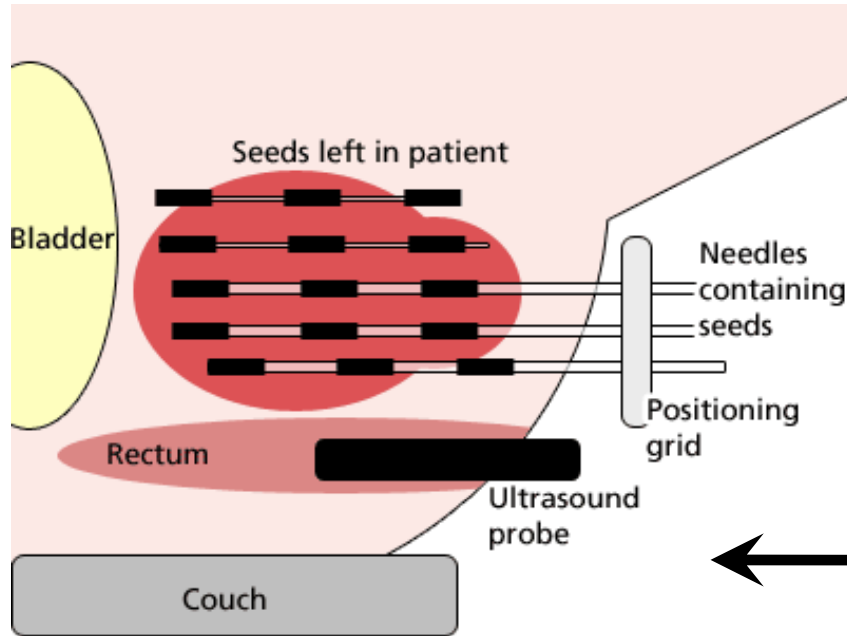
**Repopulation effects are negligible for slow growing tumors but potentially very significant for fast growing tumors**

# Are gains in tumor control significant?

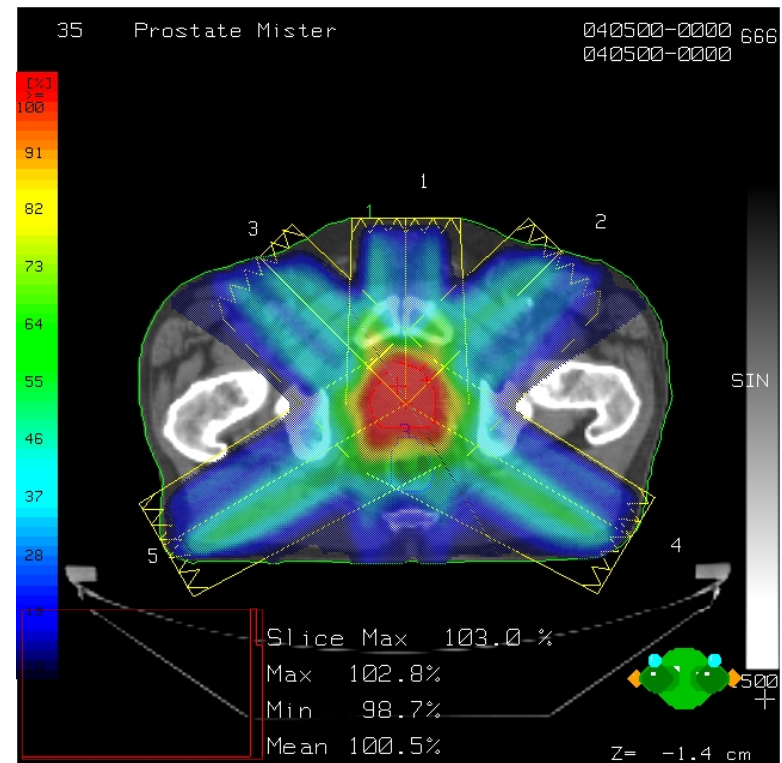


**Key Point #2:** Clinical significance of potential gains (or losses) are easily judged when expressed in terms of physical dose.

# Prescription dose for competing modalities?



**Temporary or permanent brachytherapy implants**



**Fractionated External Beam Radiation Therapy**

# Fractionated EBRT → Brachytherapy

Dose for a brachytherapy procedure (*again*) determined by

$$D = \frac{\alpha / \beta}{2G} \left\{ -1 + \sqrt{1 + \frac{4GD_R}{\alpha / \beta} \left[ 1 + \frac{G_R D_R}{\alpha / \beta} - \frac{\gamma(T_R - T)}{\alpha D_R} \right]} \right\}$$

**Reference Treatment**  
 (“clinical experience”)

$D_R$  = total dose (Gy)

$n_R$  = number fractions

$d_R = D_R/n_r$  (fraction size)

$T_R = (n_R - 1) + 2\text{int}[(n_R - 1)/5]$

**Brachytherapy Procedure**

$$G = G_\infty \left\{ \frac{(1+x)}{(1-x)} - \frac{yx^2}{(1-x)^2} \left[ 1 - e^{-(\lambda-\mu)T} \right] \right\}$$

$$G_\infty \equiv \mu / (\mu + \lambda) \quad x \equiv \exp(-\mu T)$$

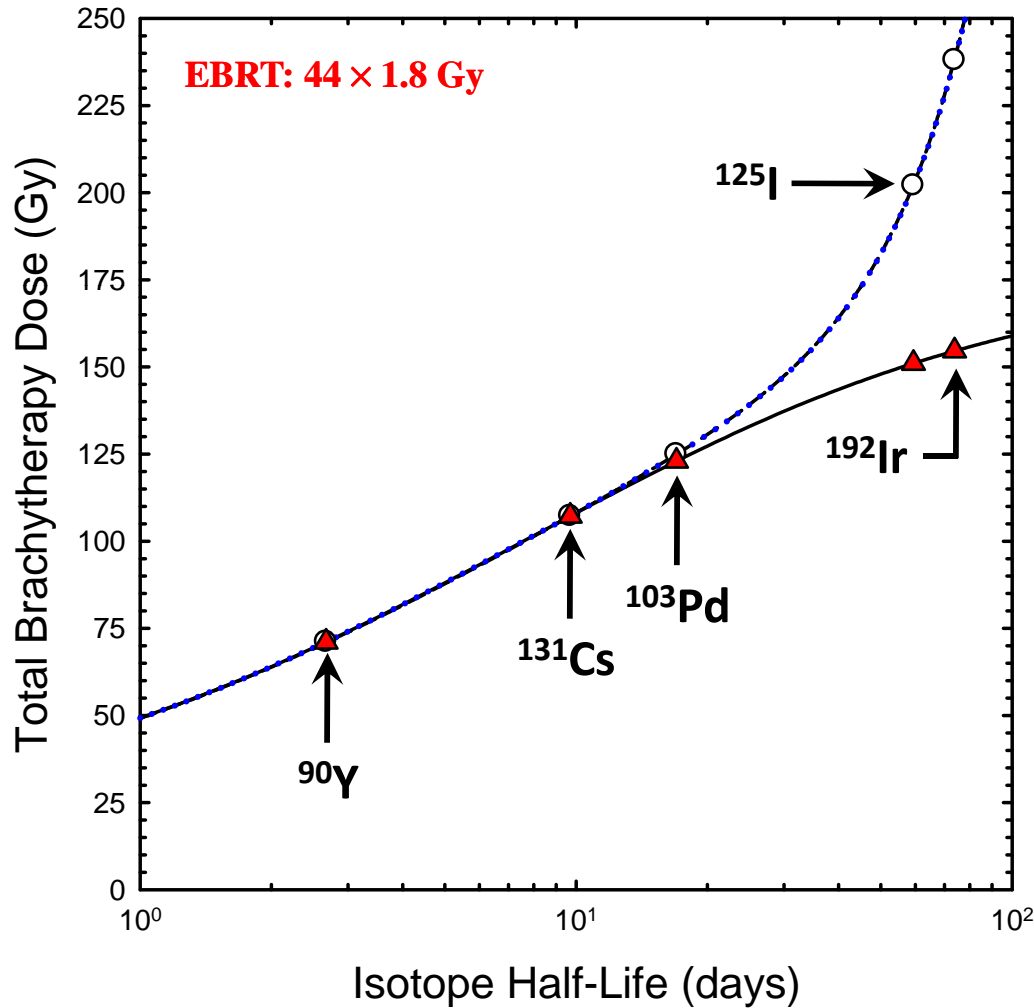
$$y \equiv 2\mu / (\lambda - \mu)$$

$\uparrow$  relates to  $\uparrow$   
**Isotope**      **Repair**  
**Half-life**    **Half-time**

$T$  = effective treatment time

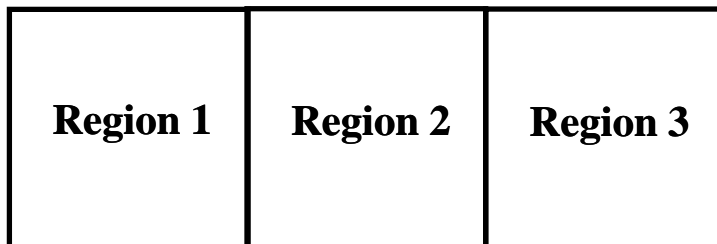


# Brachytherapy – Isotope Selection and Dose



**Brachytherapy dose equivalent to 44 × 1.8 Gy fractions EBRT**

# EUD Motivation – which is better?



*Distribution 1*

$$D_1 = 74 \text{ Gy}$$

$$D_2 = 78 \text{ Gy}$$

$$D_3 = 76 \text{ Gy}$$

$$D_{avg} = 76 \text{ Gy}$$

→ EUD<sub>1</sub>

*Distribution 2*

$$D_1 = 73 \text{ Gy}$$

$$D_2 = 75 \text{ Gy}$$

$$D_3 = 80 \text{ Gy}$$

$$D_{avg} = 76 \text{ Gy}$$

EUD<sub>2</sub> ←

**EUD = the dose applied to all three regions that would produce the same overall level of biological damage**

**In general, EUD ≠ D<sub>avg</sub> (because cell killing is a non-linear function of dose)**

**Biological damage increases with increasing EUD**

## EUD for tumor control (3)

$$\exp(-\alpha EUD - \beta EUD^2) = \frac{1}{\rho V} \sum_{i=1}^N v_i \rho_i \exp(-\alpha_i D_i - \beta_i D_i^2)$$

To solve for EUD, take logarithm and apply quadratic



$$EUD = \frac{1}{2} \alpha / \beta \left( -1 + \sqrt{1 - \frac{4 \ln \bar{S}}{\alpha(\alpha / \beta)}} \right) = \frac{1}{2} \alpha / \beta \left( -1 + \sqrt{1 + \frac{4BED}{(\alpha / \beta)}} \right)$$

$$\bar{S} \equiv \frac{1}{\rho V} \sum_{i=1}^N v_i \rho_i \exp(-\alpha_i D_i - \beta_i D_i^2)$$

**Delivery of dose = EUD to all  $i$  regions will produce same surviving fraction and level of tumor control as heterogeneous dose distribution (array of  $D_i$  values)**

## EUD for tumor control (1)

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$$TCP(EUD) = \prod_{i=1}^N TCP_i$$

$$\exp \left[ - \sum_{i=1}^N v_i \rho_i S(EUD) \right] = \exp \left[ - \sum_{i=1}^N v_i \rho_i S(D_i) \right]$$

**Neglect repopulation effects**



$$\sum_{i=1}^N v_i \rho_i \left[ \exp(-\alpha_i EUD - \beta_i EUD^2) \right] = \sum_{i=1}^N v_i \rho_i \exp(-\alpha_i D_i - \beta_i D_i^2)$$

## EUD for tumor control (2)

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$$\sum_{i=1}^N v_i \rho_i \left[ \exp(-\alpha_i EUD - \beta_i EUD^2) \right] = \sum_{i=1}^N v_i \rho_i \exp(-\alpha_i D_i - \beta_i D_i^2)$$

**Solve for EUD – in principle, formula applicable to *any* dose distribution**

**Assume ok to replace  $\alpha_i$  and  $\beta_i$  on the left-hand-side (LHS) with tumor-averaged parameters  $\alpha$  and  $\beta$**



$$\exp(-\alpha EUD - \beta EUD^2) = \frac{1}{\rho V} \sum_{i=1}^N v_i \rho_i \exp(-\alpha_i D_i - \beta_i D_i^2)$$

$$V \equiv \sum_{i=1}^N v_i \quad \text{and} \quad \rho \equiv \frac{1}{V} \sum_{i=1}^N v_i \rho_i$$

## EUD for tumor control (3)

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$$\exp(-\alpha EUD - \beta EUD^2) = \frac{1}{\rho V} \sum_{i=1}^N v_i \rho_i \exp(-\alpha_i D_i - \beta_i D_i^2)$$

**To solve for EUD, take logarithm and apply quadratic**



$$EUD = \frac{1}{2} \alpha / \beta \left( -1 + \sqrt{1 - \frac{4 \ln \bar{S}}{\alpha(\alpha / \beta)}} \right)$$

$$\bar{S} \equiv \frac{1}{\rho V} \sum_{i=1}^N v_i \rho_i \exp(-\alpha_i D_i - \beta_i D_i^2)$$

**Delivery of dose = EUD to all  $i$  regions will produce same surviving fraction and level of tumor control as heterogeneous dose distribution (array of  $D_i$  values)**