A General Test of Association for Quantitative Traits in Nuclear Families

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Summary

High-resolution mapping is an important step in the identification of complex disease genes. In outbred populations, linkage disequilibrium is expected to operate over short distances and could provide a powerful fine-mapping tool. Here we build on recently developed methods for linkage-disequilibrium mapping of quantitative traits to construct a general approach that can accommodate nuclear families of any size, with or without parental information. Variance components are used to construct a test that utilizes information from all available offspring but that is not biased in the presence of linkage or familiality. A permutation test is described for situations in which maximum-likelihood estimates of the variance components are biased. Simulation studies are used to investigate power and error rates of this approach and to highlight situations in which violations of multivariate normality assumptions warrant the permutation test. The relationship between power and the level of linkage disequilibrium for this test suggests that the method is well suited to the analysis of dense maps. The relationship between power and family structure is investigated, and these results are applicable to study design in complex disease, especially for late-onset conditions for which parents are usually not available. When parental genotypes are available, power does not depend greatly on the number of offspring in each family. Power decreases when parental genotypes are not available, but the loss in power is negligible when four or more offspring per family are genotyped. Finally, it is shown that, when siblings are available, the total number of genotypes required in order to achieve comparable power is smaller if parents are not genotyped.

Introduction

Increasingly large numbers of single-nucleotide polymorphisms are available in public and private databases (Collins et al. 1997). The emergence of high-throughput methods for their analysis holds promise for saturation mapping of human complex-disease loci (Risch and Merikangas 1996; Chakravarti 1998; Lander 1999). Whereas allele-sharing methods of linkage analysis can localize disease genes to broad chromosomal regions, in complex diseases their resolution is often poor. Accordingly, the effort spent in generating an increasingly fine map provides rapidly diminishing returns when these conventional methods of linkage analysis are used (Kruglyak 1997).

In outbred samples, allelic association due to linkage disequilibrium is expected to operate over very short distances. Appropriately designed tests of association that use family-based controls to account for population substructure can provide direct tests of linkage disequilibrium and efficient fine-mapping tools. These tests should have much greater power when a fine map is available, and their high resolution should be well suited to identification of candidate genes.

The most popular of these family-based tests of association is the transmission/disequilibrium test (TDT), which was introduced by Spielman et al. (1993) as a test of linkage in the presence of allelic association. When either a single affected child is tested in each family or, with appropriate adjustments (Martin et al. 1997), multiple children are tested, it is often used as a test of linkage disequilibrium (i.e., a test of the joint hypothesis of linkage and association). The TDT was designed for the analysis of dichotomous traits, and a number of refinements have been proposed to allow, for example, the use of siblings as controls (Curtis 1997) and increased power in the presence of imprinting or dominance (Weinberg et al. 1998).

It has been shown that tests of transmission disequilibrium require a larger number of families in order to achieve comparable power when siblings, rather than parents, are used to construct controls (Curtis 1997). However, it is not always practical to collect parents, and attempting to deduce parental genotypes is fraught with pitfalls (Curtis and Sham 1995). Ideally, TDT-like tests should use parental genotypes when available and

sibling genotypes otherwise, to consider all available information in the most efficient manner possible.

For many complex diseases, quantitative phenotype scores contain more information than is provided by dichotomous traits. Quantitative traits can provide effective descriptions of conditions as varied as asthma, type II diabetes, learning difficulties, and osteoporosis. The use of quantitative traits is well established in linkage studies, and these traits should be equally effective in family-based tests of association. Allison (1997) and Rabinowitz (1997) introduced family-based linkage tests, for quantitative traits; like the TDT, these tests use parental genotypes to construct well-matched controls and that are tests of linkage disequilibrium in simplex families. Fulker et al. (1999) described an analogous test for sib-pair data that does not use parental genotypes.

Here we present a general linkage-disequilibrium test that is applicable to the analysis of quantitative traits in nuclear families of any size and that optionally uses parental genotypes. The method builds on the recent approach of Fulker et al. (1999), in that association effects are partitioned into between- and within-family components. The model also makes use of the powerful and flexible variance-components framework, to construct tests of linkage, linkage disequilibrium, and population admixture that use information from all available offspring. In addition to extending this model to accommodate nuclear families of any size, we derive the expectations of the model parameters and show that a test of the within-family component is indeed free of confounding population-substructure effects, regardless of the composition of nuclear families. We also show that admixture impacts the between-family–component estimate when samples from a number of population strata are combined. This general model encompasses the specific test and study design of Fulker et al. (1999), as well as that of Rabinowitz (1997). The properties of the model in terms of power and error rates are explored in a number of situations, including moderate sample sizes and violation of the multivariate normality assumption underlying variance-components methods. Power and optimal study designs in terms of parental information and family size are also examined.

Maximum-Likelihood Tests of Association

Consider a candidate diallelic marker, M, with alleles arbitrarily designated as "1" (with frequency p) and "2" (with frequency $q = 1 - p$) and an additive genetic value a. Note that our usage of the additive genetic value refers to the observed marker, not the trait locus, and that $a \neq 0$ only when the marker locus is either the trait locus or in disequilibrium with it. Also, as long as the phase of the association is the same in all subpopulations,

$a = 0$ only when there is no linkage disequilibrium. Given a set of $i = 1 \ldots K$ nuclear families, each with n_i children so that the total number of offspring is $N = \Sigma_i n_i$, define the marker phenotype m_{ij} and the genotype score g_{ij} for the jth offspring ($j = 1 \ldots n_i$) in the ith family as m_{ij} = number of "1" alleles at locus M, and $g_{ij} = m_{ij} - 1$. If both parental genotypes are known, label their analogous genotype scores g_{iM} and g_{iF} for the male and female parent, respectively.

Following the usual biometric model (Falconer 1989), we assume that the phenotype scores for the trait of interest are defined by a major-gene effect, familial effects (which include the effects of shared environment and half the additive polygenic variance), and a residual environmental component. The expected mean of the residual resemblance and unique environmental effects are assumed to be 0, so that

$$E(y_{ij}) = E(\mu + g_{ij}a) = \mu + (p - q)a , \qquad (1)$$

and, for the offspring in each family, the $n_i \times n_i$ variance-covariance matrix, Ω_i, has elements

$$\Omega_{ijk} = \begin{cases} \sigma_a^2 + \sigma_s^2 + \sigma_e^2 & \text{if } j = k \\ \pi_{ijk}\sigma_a^2 + \sigma_s^2 & \text{if } j \neq k \end{cases}, \qquad (2)$$

where π_{ijk} denotes the proportion of alleles shared identical by descent (IBD) between siblings j and k in family i, σ_a^2 is the additive genetic variance of the major gene, σ_s^2 is the residual sibling resemblance, and σ_e^2 is the residual environmental variance component. Note that these expectations do not include any dominance variance, although the general method can easily accommodate such effects (Fulker et al. 1999; also discussed below).

Variance-components approaches allow simultaneous modeling of the means and variances, so that all the information in a set of related individuals can be used to construct a test of association. For a particular means model, such as

$$\hat{y}_{ij} = \mu + \beta_a g_{ij} , \qquad (3)$$

and for estimates of all of the variances in Ω_i, the likelihood of the data for the complete set of parameters, $\theta = [\mu, \beta_a, \sigma_a^2, \sigma_s^2, \sigma_e^2]$, is

$$L = \Pi_i(2\pi)^{-n_i/2}|\hat{\Omega}_i|^{-1/2}e^{-1/2[(y_i-\hat{y}_i)'\hat{\Omega}_i^{-1}(y_i-\hat{y}_i)]} . \qquad (4)$$

Evidence for association can be evaluated by maximization of L with the constraint $\beta_a = 0$ (null-hypothesis likelihood, L_0) and without constraints on the parameters (alternative-hypothesis likelihood, L_1). Asymptotically, the quantity $2[\ln (L_1) - \ln (L_0)]$ is distributed as χ^2,

with df equal to the difference in number of parameters estimated. Similar likelihood-ratio tests have been proposed as tests of association between marker and phenotype (e.g., see George and Elston 1987), and, in the absence of population admixture, they are valid tests of linkage disequilibrium, because $E(\beta_a) = a$. For families with exactly two siblings, this model is the same as the general model of Fulker et al. (1999).

Population Admixture

We allow for the most extreme form of population admixture, in which each family is drawn from a different stratum. Define μ_i, p_i, and q_i, the phenotypic mean and allele frequencies for the stratum from which family i was drawn. Assume that within each subpopulation there is random mating and random transmission of parental alleles to offspring and that the total sample of N individuals is centered on mean 0; that is, $\mu = \Sigma_i n_i \mu_i = 0$.

In this situation, the expectation given in equation (1) can be expressed as $E(y_{ij}) = E(\mu_i + g_{ij}a) = \mu_i + (p_i - q_i)a$, and the alternative hypothesis of no linkage disequilibrium is no longer encompassed in a test of $\beta_a \neq 0$. As shown in Appendix A, in this case, $E(\beta_a) = \Sigma_i n_i(p_i - q_i)\mu_i/(NV_g) + a$, where V_g is the variance of the genotypic scores. The numerator of the first term in this expression represents "spurious" association, at the population level, that is independent of linkage.

Orthogonal Decomposition of the Genotype Scores

Fulker et al. (1999) proposed that, for sib-pair data, the genotype score could be decomposed into orthogonal between-family (b) and within-family (w) components, in which only the former is sensitive to population structure and in which the latter is significant only in the presence of linkage disequilibrium. The means model under this specification is

$$\hat{y}_{ij} = \mu + \beta_b b_i + \beta_w w_{ij} , \qquad (5)$$

where b_i and w_{ij} are orthogonal between- and within-family components of g_{ij}. We extend this model to accommodate any number of offspring, with or without parental genotypes, as

$$b_i = \begin{cases} \dfrac{\sum\limits_j g_{ij}}{n_i} & \text{if parental genotypes are unknown} \\[2ex] \dfrac{g_{iF} + g_{iM}}{2} & \text{if parental genotypes are available} \end{cases},$$

$$w_{ij} = g_{ij} - b_i , \qquad (6)$$

so that b_i is the expectation of each g_{ij} conditional on family data and w_{ij} is the deviation from this expectation for offspring j. Note that, when $b_i = (\Sigma_j g_{ij})/n_i$, all possible siblings are considered and parental data are ignored, whereas, when $b_i = (g_{iF} + g_{iM})/2$, only parental data are used (for an example of how b_i and w_{ij} are scored, with and without parental data, see table 1). Positive values of w_{ij} indicate that a child inherits more copies of allele "1" than would be expected, whereas negative values refer to inheritance of an excess of allele "2." For sib-pair data for which parental genotypes are not available, which is the situation described by Fulker et al. (1999), $w_{i1} = -w_{i2}$ for any i, so that different alleles are tested in each member of a sib pair and the distribution of β_w is unaffected by linkage in the absence of association.

Fulker et al. (1999) suggested that the β_w regression coefficient, when estimated in the context of a variance-components model and in the absence of population admixture, provides a direct estimate of the additive genetic value a. Allowing for population admixture and extending the model to allow both for sibships of any size and for the inclusion of parental genotype data, we derive the expectation of β_b and β_w for each of these two alternative definitions and show that all the "spurious" association between genotype score and phenotype is

Table 1

Example Scoring of b_i and w_{ij} in a Sib Pair

OFFSPRING			PARENTAL INFORMATION			SIBS ONLY		
g_{i1}	g_{i2}	$P(g)$	b_i	w_{i1}	w_{i2}	b_i	w_{i1}	w_{i2}
One Heterozygous Parent $(g_{iF}, g_{iM}) = (1, 0)$								
0	0	p^3q	$\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{1}{2}$	0	0	0
0	1	$2p^3q$	$\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$
1	1	p^3q	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0	0
Two Parents Heterozygous $(g_{iF}, g_{iM}) = (0, 0)$								
−1	−1	$\frac{1}{4}p^2q^2$	0	−1	−1	−1	0	0
1	1	$\frac{1}{4}p^2q^2$	0	1	1	1	0	0
0	0	p^2q^2	0	0	0	0	0	0
−1	0	p^2q^2	0	−1	0	$-\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$
0	1	p^2q^2	0	0	1	$\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$
−1	1	$\frac{1}{2}p^2q^2$	0	−1	1	0	−1	1

NOTE.—For the unordered pairs of parental genotype scores $(g_{iF}, g_{iM}) = (1, 0)$ and $(g_{iF}, g_{iM}) = (0, 0)$, the table lists possible offspring genotype scores, and their frequency at the population level. The scoring of b_i and w_{ij} is illustrated for these cases by use of either parental genotypes or sibling genotypes only. Note that the frequency of these mating types is $4p^3q$ and $4p^2q^2$, respectively.

accounted for by β_b and that the β_w regression coefficient remains a direct estimate of the additive genetic value a (at the marker).

By use of the normal equations, equation (5) can be expressed as $\mathbf{y} = \mathbf{Xb} + \mathbf{e}$, so that $\hat{\mathbf{b}} = (\mathbf{X'X})^{-1} \mathbf{Xy}$, where $\mathbf{X}$ is the design matrix and $\hat{\mathbf{b}} = (\beta_b, \beta_w)$. $\mathbf{X'X}$ and $\mathbf{Xy}$ are asymptotically the covariance matrices between the independent and dependent variables, respectively. To solve these equations, only the expectations for the variances, V_b and V_w, and covariances, $C_{b,y}$ and $C_{w,y}$, are required, since b_i and w_{ij} are orthogonal by design. These quantities are derived in Appendices B and C.

Parental Genotypes Available

As shown in Appendix B,

$$
\begin{bmatrix} V_b & C_{b,w} \\ \\ C_{b,w} & V_w \end{bmatrix} =
$$

$$
\begin{bmatrix} \dfrac{\sum_i n_i(p_i^2 + q_i^2 - p_iq_i)}{N} - \dfrac{\left[\sum_i n_i(p_i - q_i)\right]^2}{N^2} & 0 \\ \\ 0 & \dfrac{\sum_i n_i p_i q_i}{N} \end{bmatrix},
$$

and

$$
\begin{bmatrix} C_{b,y} \\ \\ C_{w,y} \end{bmatrix} = \begin{bmatrix} \dfrac{\sum_i n_i(p_i - q_i)\mu_i}{N} + V_b a \\ \\ \dfrac{\sum_i n_i p_i q_i}{N} a \end{bmatrix},
$$

so that

$$
\begin{bmatrix} \beta_b \\ \\ \beta_w \end{bmatrix} = \begin{bmatrix} \dfrac{\sum_i n_i(p_i - q_i)\mu_i}{NV_b} + a \\ \\ a \end{bmatrix}.
$$

Note that all the population-substructure effects in the means, μ_i, that are apparent in the general specification of $E(\beta_a)$ are included in the expectation of β_b exclusively. Whereas β_b provides a direct estimate of a only if there is no "spurious" association between g and y (e.g., when all μ_i are 0 or, since $\Sigma_i n_i \mu_i = 0$, when p and q are constant), β_w is independent of any "spurious" effects and remains a valid estimate of a even when there is admixture.

Parental Genotypes Unobserved or Unused

As shown in Appendix C,

$$
\begin{bmatrix} V_b & C_{b,w} \\ \\ C_{b,w} & V_w \end{bmatrix} =
$$

$$
\begin{bmatrix} \dfrac{\sum_i n_i[p_i^2 + q_i^2 - p_iq_i(\frac{n_i-1}{n_i})]}{N} - \dfrac{\left[\sum_i n_i(p_i - q_i)\right]^2}{N^2} & 0 \\ \\ 0 & \dfrac{\sum_i p_i q_i(n_i - 1)}{N} \end{bmatrix},
$$

and

$$
\begin{bmatrix} C_{b,y} \\ \\ C_{w,y} \end{bmatrix} = \begin{bmatrix} \dfrac{\sum_i n_i(p_i - q_i)\mu_i}{N} + V_b a \\ \\ \dfrac{\sum_i p_i q_i(n_i - 1)}{N} a \end{bmatrix},
$$

so that, as $[(n_i - 1)/n_i] \to 1$, the contribution of each family to V_b, V_w, $C_{b,y}$, and $C_{w,y}$ approximates that of the case in which parents are available (given in the previous section). On solution of the normal equations,

$$
\begin{bmatrix} \beta_b \\ \\ \beta_w \end{bmatrix} = \begin{bmatrix} \dfrac{\sum_i n_i(p_i - q_i)\mu_i}{NV_b} + a \\ \\ a \end{bmatrix},
$$

so that β_w remains a direct estimate of a, independent of population admixture and the number of offspring observed in each family. In contrast, β_b is again a direct estimate of a only when there is no "spurious" association between genotype scores, g, and phenotype, y. These expectations show that the admixture test of $\beta_b = \beta_w$ proposed by Fulker et al. (1999) is valid even when parental genotypes are included in analysis and when sibships of size >2 are evaluated.

Simulations

A number of simulation studies were conducted to explore the properties of this orthogonal decomposition of genotype scores as a test of linkage disequilibrium. Data were simulated in nuclear families each having one to eight offspring. Trait values were constructed as the sum of a major-gene effect (with variance σ_a^2) generated by an additive quantitative-trait locus (QTL), Q, having two equifrequent alleles, a residual sibling correlation (σ_s^2), and an environmental effect (σ_e^2), each assigned independently from a normal distribution with mean 0.

Except where noted, a diallelic marker locus M, with allele frequencies $p = q = \frac{1}{2}$, was simulated with a recombination fraction (θ) of 0. For convenience, the total trait variance $\sigma^2 = \sigma_a^2 + \sigma_s^2 + \sigma_e^2$ was fixed at 100 in all simulations.

Linkage disequilibrium between the trait and marker locus was introduced in the parental chromosomes. When appropriate, disequilibrium was modeled in the usual fashion as $D = p_{M_1 Q_1} - p_{M_1} p_{Q_1}$ ($p_{M_1 Q_1}$ is the frequency of the haplotype with alleles M_1 and Q_1, and p_{M_1} and p_{Q_1} are the frequencies of alleles M_1 and Q_1; Lewontin and Kojima 1960), so that $D_{max} = \min(p_{M_1}, p_{Q_1}) - p_{M_1} p_{Q_1}$, and the standardized disequilibrium coefficient is D/D_{max}.

Where noted, population admixture was generated by the mixing of families drawn from one of two populations (A and B) with different phenotypic means (μ_A and μ_B) and marker allele frequencies ($p_A = .7$ and $p_B = .3$) in equal sampling proportions. μ_A and μ_B were selected such that admixture accounted for 20% of the total phenotypic variance in the combined population; that is, $[(\mu_A - \mu_B)^2/4\sigma^2] = .20$

Except where noted, parental genotypes were used to estimate π by use of information available from the single-marker locus (Haseman and Elston 1972). By use of the variance-components model (eq. [2]) and the orthogonal model for the means (eq. [5]), the likelihood was maximized under the null ($\beta_w = 0$) and alternative hypotheses, to calculate L_0 and L_1, respectively (eq. [4]). As suggested by Searle et al. (1992), the variance-component estimates were constrained to be positive. To examine the benefits of parental information, each simulated data set was examined under the two alternative definitions of b_i and w_{ij} (see eq. [6]). Only families having at least one heterozygous parent (when parental genotypes were used) or at least two different types of offspring (when parental genotypes were ignored) were included in the likelihood calculations, since other families do not contribute to estimates of β_w. For the purpose of our simulations, power and error rates were defined as the proportion of simulations exceeding nominal significance levels for the χ^2 distribution under the likelihood-ratio criteria.

It is well known that segregation of a major locus violates the multivariate normality assumption and that maximum-likelihood estimates of the variance components can be biased in small samples (Amos et al. 1996). To characterize the effect that that bias has on the present test, error rates of β_w were examined for a range of sample sizes (i.e., 120–1,920 offspring) and family structures (1–8 children), in the following situations: (1) no sibling correlation or major-gene effect ($\sigma_s^2 = \sigma_a^2 = 0$) in homogeneous and admixed populations, (2) a large major-gene effect ($\sigma_a^2 = 30$) or a large residual sibling correlation ($\sigma_s^2 = 50$), and (3) both residual sibling corre-

lation and major-gene effect ($\sigma_a^2 = 20$, $\sigma_s^2 = 30$). Five thousand simulated data sets were examined in each test case. No disequilibrium was modeled in any of these simulations.

The effects that family structure and linkage disequilibrium have on power were examined in a sample of 480 total offspring when $\sigma_a^2 = 10$ and $\sigma_s^2 = 30$, by varying D between 0 and D_{max} and varying, from one to eight, the number of offspring in each family. In these assessments, the total number of offspring sampled was fixed, so that the number of families varied according to sibship size. Finally, the sensitivity of the test to linkage disequilibrium was estimated for a variety of sample sizes and family structures. Sensitivity was defined as the most stringent significance level that could be obtained with 80% power in simulated data sets in which the trait and marker loci were identical. When power and test sensitivity were examined, 1,000 simulated data sets were analyzed in each case.

Permutation Test

For each family, the vector $\mathbf{w}_i$ denotes the observed pattern of allelic transmission. In the absence of linkage disequilibrium, the vectors $\mathbf{w}_i$ and $-\mathbf{w}_i$ are equally likely, as long as there is no segregation distortion. Construct a random permutation of any set of K families by replacing each $\mathbf{w}_i$ with either itself or $-\mathbf{w}_i$, with equal probability, so that, for any given data set, there are 2^K different permutations of the data. The distribution of the maximum likelihood of the data, L_1, under the hypothesis of no linkage disequilibrium is the distribution of the maximum likelihoods of these 2^K permuted data sets. When the distribution of $2[\ln(L_1) - \ln(L_0)]$ is not well approximated by the χ^2 distribution, the distribution of L_1 can be estimated by a sampling of a large number of permutations and their respective likelihoods. These empirical P values and the likelihood-ratio criterion were compared in a small sample (120 total offspring) in which the major-gene effect was introduced by simulation of a dominant QTL with equally frequent alleles. In this situation, empirical significance levels should be desirable because both dominance (which both induces nonnormality into the trait distribution and makes the variances model [eq. {2}] incomplete) and the small sample size are expected to reduce the accuracy of asymptotic significance levels. For dichotomous traits, the increased error rates of likelihood-ratio tests in small samples, as well as their spurious effect on power, have been described by Whittaker and Thompson (1999). The rationale for permutation tests in linkage studies has been discussed by Wan et al. (1997).

Table 2

Error Rates When Parents Are Available

Offspring per Family and Test Case[a]	Error Rate[b] When Total No. of Offspring Is				
	120	240	480	960	1,920
1:					
Overall	5.5	5.3	5.4	5.1	5.1
2:					
Null	5.4	5.0	5.3	4.8	5.0
Admixture	5.6	5.4	5.4	4.6	5.7
Sibling resemblance	4.8	5.0	4.7	4.4	5.2
Linkage	7.0	5.4	5.7	5.0	5.3
Composite	5.6	4.8	4.9	5.4	5.1
4:					
Null	5.1	5.1	4.9	4.5	4.2
Admixture	5.0	4.9	4.5	5.2	4.7
Sibling resemblance	4.8	5.0	4.7	4.4	4.8
Linkage	7.0	5.4	5.7	5.0	5.2
Composite	5.6	4.8	4.9	5.4	5.3
8:					
Null	4.9	5.3	5.7	4.8	5.5
Admixture	4.5	4.4	4.9	4.2	5.2
Sibling resemblance	4.4	4.0	4.5	4.7	4.8
Linkage	6.5	6.2	5.9	5.8	6.1
Composite	5.2	5.3	5.0	5.2	4.7

  [a] Null = no sibling resemblance, or major-gene effect ($s^2 = h^2 = 0$); Admixture = no sibling resemblance, or major-gene effect ($s^2 = h^2 = 0$, with population admixture); Sibling resemblance = large sibling resemblance ($s^2 = .5$); Linkage = linked major gene of large effect ($h^2 = .3$, $\theta = 0$); Composite = composite test case ($s^2 = .3$ and $h^2 = .2$, $\theta = 0$). There was no linkage disequilibrium between QTL and marker locus ($D = 0$). For single-child families, only the overall error rate is reported. Each estimate is based on 5,000 replicates.

  [b] Shown as the proportion of simulations exceeding the nominal significance level, .05.

Type 1–Error Rates

Error rates in estimates of the β_w parameter in various test cases are presented in tables 2 and 3. Additional family structures were examined, but the results were intermediate between those tabulated and are not shown. A large major gene and sibling resemblance were selected for description of error rates, to make any possible biases obvious. When one child from each family was considered, error rates were not influenced by population admixture or by the effects of the linked major locus or additional sibling resemblance, so that only a summary error rate over all test cases is reported.

The error rates for the rows labeled "Null" in tables 2 and 3 should be considered as baseline error rates for the other test cases. Not surprisingly, error rates were closer to nominal significance levels in larger samples, where the likelihood-ratio criterion is more accurate. For very large samples, the asymptotic criteria seem to be appropriate regardless of model or sibship size (tables 2

and 3). In smaller samples, error rates are slightly high for the linkage test case and are slightly low for the admixture and sibling-resemblance test cases, an effect that is more pronounced for larger sibships. When only a small number of observations are considered, estimates of the variance components may be biased (see Hopper and Mathews 1982; Amos et al. 1996), so that these error rates are not a specific feature of the present model but may reflect violations of multivariate normality.

As the sample size increases, bias in the maximum-likelihood estimates of variance components should be reduced, and the error rate of asymptotic significance tests should approach its nominal level (Amos et al. 1996). These small-sample biases decrease for more-realistic values of σ_a^2 and σ_s^2. It is interesting to note that, although some bias remains when the variance components are estimated by maximum likelihood, these biases are much larger if only σ_e^2 is considered: for example, if the linkage information is ignored and a traditional least-squares regression framework is adopted, modeling only σ_e^2 and the association parameters, the error rates exceed 11% at the nominal .05 significance level, for all sample sizes examined in the eight-sib linkage-test case in tables 2 and 3.

When parental genotypes are not available for analysis (table 3), it may appear counterintuitive that, although the biases follow the general trends described above, they

Table 3

Error Rates When Parents Are Unavailable or Unused

Offspring per Family and Test Case[a]	Error Rate[b] When Total No. of Offspring Is				
	120	240	480	960	1,920
2:					
Null	6.5	6.1	5.7	5.3	5.1
Admixture	6.6	6.0	4.6	4.2	4.8
Sibling resemblance	5.4	5.5	5.5	4.7	5.1
Linkage	7.1	5.7	6.0	5.7	5.3
Composite	5.7	5.2	5.2	5.2	4.9
4:					
Null	5.3	5.4	4.5	4.6	4.8
Admixture	5.1	4.1	4.4	4.7	4.6
Sibling resemblance	4.3	4.4	4.6	4.6	4.7
Linkage	6.2	6.1	5.7	5.7	5.3
Composite	5.5	6.1	5.5	5.2	4.8
8:					
Null	5.2	4.9	5.4	4.8	5.2
Admixture	4.2	4.2	4.6	4.2	5.0
Sibling resemblance	3.5	4.3	4.8	3.9	4.8
Linkage	7.7	6.9	5.9	5.6	5.5
Composite	6.1	5.7	5.2	5.2	5.4

Note.— The simulated data sets are the same as those used in table 1, but parental genotypes were not considered during the analysis.

  [a] Test cases are as defined in table 2.

  [b] Shown as the proportion of simulations exceeding the nominal significance level, .05.

appear to be greater in the two-sib case. The reason for this increased bias is that $\mathbf{w}_i$ is not $\mathbf{0}$ (and therefore informative) in only a small proportion of sib pairs when parental genotypes are not available for analysis, so that the effective sample size is much less than that actually genotyped.

Power Estimates

Results of the power calculations are presented in table 4 and figure 1. When parental genotypes are available, power depends mostly on the amount of disequilibrium between the trait and marker loci and is largely independent of the number of offspring in each family (table 4). In contrast, when parental genotypes are not available, power depends both on family size and on the level of disequilibrium: larger sibships allow a greater proportion of segregating alleles to be identified (and scored to be not 0 in the respective w_{ij}), and, thus, power increases with the number of siblings in each family. As might be expected, for any family size, power is always greater when parental genotypes are available for analysis, since all pairs of segregating alleles are evident in this situation. However, for larger sibships (four or more offspring), it appears that $\leqslant 5\%$ power is lost when parental genotypes are unavailable.

When $D/D_{\mathrm{max}} > 50\%$, it is possible to achieve consid-

erable power for loci accounting for 10% of the phenotypic variance, and estimates of β_w are unbiased and essentially exact when there is complete disequilibrium (table 4). The relationship between the apparent additive genetic value of the marker locus, β_w, the disequilibrium coefficient, D, and additive genetic effect at the QTL is very close to $a_{\mathrm{marker}} = a_{\mathrm{QTL}}D/p_{\mathrm{QTL}}q_{\mathrm{QTL}}$ (Falconer 1989; Fulker et al. 1999). This implies that the proportion of variance explained by the association parameter is a function of the squared disequilibrium coefficient D^2 and the additive genetic variance of the trait locus, so that it is not surprising that power is very sensitive to D. When $D = D_{\mathrm{max}}$ and the QTL and marker-allele frequencies are the same, all of the genetic variance attributable to the QTL will be encompassed in the allelic-association parameter, and estimates of the residual additive genetic variance (σ_a^2) will equal 0.

Figure 1 shows the most stringent significance level, α, that can be applied when 80% power is achieved, as a function of both the total number of offspring sampled and the additive genetic variance of the QTL, when the trait locus is observed. As noted previously, when parental genotypes are available, power does not depend greatly on the number of offspring in each family, so that only the sib-pair case has been plotted. When parents are unavailable, it is clear that achievable significance levels rapidly approach that of the case in which

Table 4

Effects of Family Structure and Linkage Disequilibrium on Power

D/D_{max}[a] (%)	ONE SIB PER FAMILY	TWO SIBS PER FAMILY	THREE SIBS PER FAMILY	FOUR SIBS PER FAMILY	FIVE SIBS PER FAMILY	SIX SIBS PER FAMILY	EIGHT SIBS PER FAMILY	$\hat{\beta}_w$
	No. of Families When Total No. of Sibs Is 480							
	480	240	160	120	96	80	60	
	Power When Parental Genotypes Are Included in Analysis, for $E(N_w) = 360$[b]							
0	.2	.0	.1	.1	.2	.1	.0	.01
25	2.1	1.8	2.0	2.6	3.0	2.1	2.1	1.11
50	19.5	22.9	24.8	26.7	26.7	27.2	23.9	2.24
75	69.3	72.6	74.2	76.9	76.0	76.5	75.4	3.35
100	97.4	97.7	98.3	98.4	98.2	98.4	98.5	4.46
	Power When Parental Genotypes Are Not Included in Analysis, for $E(N_w) =$[b]							
	...	195	281	322	341	350	358	
0	...	.1	.1	.2	.2	.0	.0	.02
25	...	1.2	2.3	2.7	2.3	1.6	1.8	1.11
50	...	12.8	18.7	22.6	23.5	25.2	23.1	2.25
75	...	44.3	64.1	69.5	71.5	73.5	73.9	3.34
100	...	83.3	94.6	97.3	97.7	98.0	98.3	4.45

NOTE.— Each simulated data set consisted of 480 total offspring, so that the total number of families decreased with increasing sibship size.

[a] Between QTL and marker locus ($\theta = 0$). The total trait variance was set at 100, so that the true additive genetic value at the QTL was 4.47.

[b] Power is shown as the proportion of simulations exceeding the nominal significance level, .001. The simulation parameters specified a QTL locus with $h^2 = .1$ and a residual sibling correlation $s^2 = .3$. N_w = effective sample size, which corresponds to offspring in families in which allelic transmission could be scored.
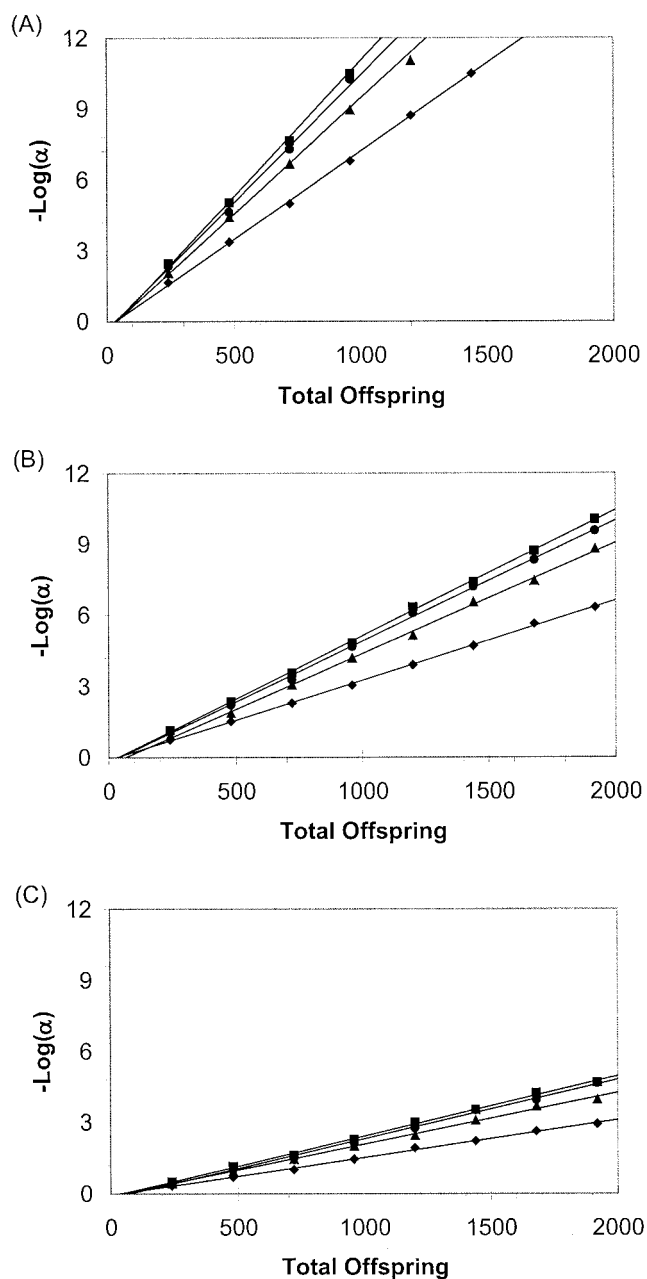
Figure 1 Sensitivity of the orthogonal test to association. Sensitivity is defined as $\log_{10} \alpha$, where α is the significance level exceeded by 80% of simulated data sets. The total number of offspring varied between 240 and 1,920 (in increments of 240 children). Results were plotted for sib-pair families in which parental genotypes were available for analysis (*squares*) and for sib-pair (*diamonds*), sib-triad (*triangles*), and sib-quad (*circles*) families in which parental genotypes were not available for analysis. The proportion of phenotypic variance attributable to residual sibling resemblance (s^2) was .30. The major-gene effect (h^2) was .10 in panel *A*, .05 in panel *B*, and .025 in panel *C*, Each plotted data point corresponds to 1,000 simulated data sets. For convenience, a least-squares straight line has been plotted through each set of data points.

parents are available, as the number of children in each family increases. When these plots are used, an arbitrary significance level may be selected for a given sample size and study design. Alternatively, for a desired number of independent tests and correspondingly adjusted significance level, an appropriate sample size and study design may be selected. For example, for the hypothetical genome screens proposed by Risch and Merikangas (1996), $\alpha = 5 \times 10^{-8}$ and $\log_{10}(\alpha) = 7.3$, so that, as can be seen in figure 1*A*, either ~350 sib pairs with parents (700 total offspring but 1,400 genotypes) or ~500 sib pairs without parental information (1,000 total offspring/genotypes) or ~260 sib trios without parents (800 total offspring/genotypes) are needed for 80% power and a locus that accounts for 10% of phenotypic variance. It is noteworthy that the total number of genotypes required is smaller when parental information is not used. In practice, the marker locus and trait locus will often not be identical, so these represent best-case estimates of power.

Evaluation of the Permutation Test

To assess the performance of the permutation test, a series of simulations was undertaken in which dominance variance was introduced to skew the phenotypic distribution and to violate multivariate normality. In an attempt to introduce further departures from asymptotic expectations, we omitted the appropriate dominance-variance parameter from the variance-components portion of the model. The results of these simulations are presented in table 5. The performance of the empirical permutation test was examined in 5,000 samples of 120 offspring (in families with 1 to 8 children) when a dominant major gene ($H^2 = .3$, $s^2 = .3$) was segregating ($\theta = 0$). When $D = 0$, the overall error rate at the .05 significance level was .06 when asymptotic expectations were used but was .05 when empirical significance levels were calculated from 1,000 permutations of each data set. When $D = D_{max}$, power at the .05 significance level was 56% for asymptotic significance levels but was 52% when empirical significance levels were calculated from 1,000 permutations of each data set. For larger samples in which the model is well specified, such as those in table 4, we find no significant advantages in this permutation test.

Discussion

The orthogonal model that we propose is a generalization of the one described by Fulker et al. (1999) for sib-pair data. It allows for the optional inclusion of parental data, which greatly increases power, and for the analysis of larger sibships, in which identification of segregating alleles is more efficient. For large sample

Table 5

Error Rates When the Variances Model for Ω_{ijk} Is Inappropriate

Offspring per Family	Error Rate when Total No. of Offspring Is[a]				
	120	240	480	960	1,920
When Parental Genotypes Are Available					
1	5.9	5.6	5.2	5.1	5.2
2	6.3	5.2	5.5	5.3	5.8
4	6.3	5.2	5.5	5.3	5.6
8	6.9	6.6	6.2	5.9	5.5
When Parental Genotypes Are Not Available					
2	7.0	5.7	5.8	5.2	5.7
4	6.5	6.6	6.1	6.3	6.2
8	8.6	7.0	6.2	6.1	5.5

[a] Proportion of simulations exceeding the nominal .05 significance level when there is a linked dominant major gene ($\theta = 0$, $h^2 = .3$) with equally frequent alleles. The model for variances in Ω_j did not include a dominance variance component, so that in larger families the error rate is high. This major gene also introduced skewness in the phenotype distribution, violating multivariate normality.

sizes or when empirical significance levels are calculated by the permutation method described, the test is robust to a variety of biases, including linkage, background familiality, and population stratification. Also, when parental data are used, the test of the within-family–association parameter β_w is asymptotically a test of $E(wy) = 0$ and is equivalent to that described by Rabinowitz (1997) without the benefit of the variance-components framework. Other linear models, such as that proposed by Allison (1997), could be used with the variance-components approach, but the orthogonal model is attractive because it both provides direct estimates of the additive genetic value of the marker alleles and can be used when parental genotypes are unavailable. It is important to emphasize that the present approach treats linkage and association separately. Consequently, in contrast to other methods, which provide tests of disequilibrium only in minimal family configurations (Spielman et al. 1993; Allison 1997; Rabinowitz 1997; Allison et al. 1999), the orthogonal method does not detect linkage in the absence of disequilibrium in nuclear families of any configuration.

Although, in our simulations, power depended mostly on the major-gene–effect size and on the total number of offspring available for analysis, in practice it is undesirable to rely on a small number of large families, because they might represent very few alleles. However, moderate-size families (i.e., three to four sibs) might be more attractive than sib pairs, because they provide much greater power when parents are not available and require less genotyping effort when parents are available.

The observation that, for multiplex families, the number of individuals that need to be genotyped in order to achieve comparable power is smaller when parental genotypes are not used is important in situations in which genotyping capacity is limited.

Obviously, power is very sensitive to disequilibrium, so that this test and other, related approaches are well suited for the analysis of dense maps. In practice, it may not be practical to use these dense maps for genome screens, but they can be used to follow up suggestive linkages that have been identified by allele-sharing methods on a more sparse map. When a dense marker map becomes available, it can be used to produce multipoint estimates of IBD. In the variance-components side of the model, better IBD estimates allow the fitted variance-covariance matrix to better approximate the true variances and covariances, improving the performance of the model, in terms of both power and error rates.

The model can be easily extended to allow for multiallelic markers with up to X alleles, by inclusion of a separate between- and within-family component for alleles 1 through $X - 1$, and, in this situation, no changes to the variance model should be required. In other situations, it might be appropriate to define either dominance genotype scores or, when imprinting is suspected, separate paternal and maternal genotype scores. These alternative genotype scores can be decomposed into orthogonal components by taking either the sibling average or its asymptotic expectation derived from the parental genotypes. However, these modifications require either changes to the variance model or calculation of empirical P values, by analogous permutation tests.

Hopper and Mathews (1982) have described a number of methods for verifying that multivariate normality assumptions are not grossly violated. The permutation test that we describe should allow this orthogonal model to be applied in situations in which multivariate normality is violated—for example, when the sample size is small or the trait distribution has been skewed by selection (e.g., see Allison 1997) or when the model for variances may be inappropriate. However, asymptotic significance levels are still appropriate in most situations examined here and can be a useful tool in prescreening, to conserve computing resources.

Acknowledgments

Appendix A

$E(\beta_a)$ with Allowance for Population Admixture

Consider population admixture by defining μ_i and p_i and q_i as the phenotypic mean and the marker-allele frequencies for the population from which family i was drawn (allowing for up to K different subpopulations). Assume that within each subpopulation there is random mating and random transmission of parental alleles to offspring and that the total sample of N individuals is centered on mean 0, so that $\mu = \Sigma n_i \mu_i = 0$. In this situation,

$$E(y) = \frac{\sum_i n_i u_i}{N} + \frac{\sum_i n_i(p_i - q_i)a}{N} = \frac{\sum_i n_i(p_i - q_i)a}{N} \ ,$$

$$E(g) = \frac{\sum_i n_i \sum_{l=-1}^{1} P(g = l|i)l}{N} = \frac{\sum_i n_i(p_i - q_i)}{N} \ ,$$

$$E(g^2) = \frac{\sum_i n_i \sum_{l=-1}^{1} P(g = l|i)l^2}{N} = \frac{\sum_i n_i(p_i^2 + q_i^2)}{N} \ ,$$

and

$$E(gy) = \frac{\sum_i n_i \sum_{l=-1}^{1} [P(g = l|i)l(\mu_i + la)]}{N} = \frac{\sum_i n_i(p_i - q_i)\mu_i}{N} + \frac{\sum_i n_i(p_i^2 + q_i^2)a}{N} \ ,$$

so that, for model (3), when the standard expectations $V_x = E(x^2) - E(x)^2$ and $C_{x,y} = E(xy) - E(x)E(y)$ are used, for any x and y,

$$E(\beta_a) = \frac{C_{g,y}}{V_g} = \frac{\sum_i n_i(p_i - q_i)\mu_i}{NV_g} + a \ ,$$

where

$$V_g = \frac{\sum_i n_i(p_i^2 + q_i^2)}{N} - \left[\frac{\sum_i n_i(p_i - q_i)}{N} \right]^2 \ .$$

These expectations extend those of Cardon (in press).

Appendix B

$E(\beta_b)$ and $E(\beta_w)$ with Use of Parental Genotypes

For the orthogonal model in equation (5), the expectations for V_b, V_w, $C_{b,y}$, and $C_{w,y}$ are required for solution of the normal equations and to obtain expectations for the regression parameters β_w and β_b.

Let Σ_z denote the sum over all possible mating types z and note that $E(y)$, $E(g)$, $E(g^2)$, and $E(gy)$ are as given in Appendix A. Then, when the mating type frequencies given by Haseman and Elston (1972) are used,

$$E(b) = \frac{\sum\limits_i n_i \sum\limits_z P(z|i)E(b|z)}{N} = \frac{\sum\limits_i n_i(p_i^4 - q_i^4 + 2p_i^3 q_i - 2p_i q_i^3)}{N} = \frac{\sum\limits_i n_i(p_i - q_i)}{N} \ ,$$

$$E(w) = E(g - b) = 0,$$

$$E(b^2) = \frac{\sum\limits_i n_i \sum\limits_z P(z|i)E(b^2|z)}{N} = \frac{\sum\limits_i n_i(p_i^4 + q_i^4 + p_i^3 q_i + p_i q_i^3)}{N} = \frac{\sum\limits_i n_i(p_i^2 + q_i^2 - p_i q_i)}{N} \ ,$$

$$E(w^2) = E[(g - b)^2] = \frac{\sum\limits_i n_i p_i q_i}{N} \ ,$$

$$E(by) = \frac{\sum\limits_i n_i \sum\limits_z P(z|i)E(by|z)}{N} = \frac{\sum\limits_i n_i \sum\limits_z P(z|i)E(b\mu_i|z)}{N} + \frac{\sum\limits_i n_i \sum\limits_z P(z|i)E(bga|z)}{N}$$

$$= \frac{\sum\limits_i n_i(p_i - q_i)\mu_i}{N} + \frac{\sum\limits_i n_i(p_i^4 + q_i^4 + p_i^3 q_i + p_i q_i^3)a}{N} = \frac{\sum\limits_i n_i(p_i - q_i)\mu_i}{N} + \frac{\sum\limits_i n_i(p_i^2 + q_i^2 - p_i q_i)a}{N} \ ,$$

and

$$E(wy) = E[(g - b)y] = E(gy - by) = \frac{\sum\limits_i n_i p_i q_i}{N} a \ .$$

These are all the quantities required in order to determine

$$\mathbf{X'X} = \begin{bmatrix} V_b & C_{b,w} \\ C_{b,w} & V_w \end{bmatrix} = \begin{bmatrix} \dfrac{\sum\limits_i n_i(p_i^2 + q_i^2 - p_i q_i)}{N} - \dfrac{\left[\sum\limits_i n_i(p_i - q_i)\right]^2}{N^2} & 0 \\ 0 & \dfrac{\sum\limits_i n_i p_i q_i}{N} \end{bmatrix}$$

and

$$\mathbf{Xy} = \begin{bmatrix} C_{b,y} \\ C_{w,y} \end{bmatrix} = \begin{bmatrix} \dfrac{\sum\limits_i n_i(p_i - q_i)\mu_i}{N} + V_b a \\ \dfrac{\sum\limits_i n_i p_i q_i}{N} a \end{bmatrix} \ .$$

So, on inversion and multiplication,

$$\hat{b} = \begin{bmatrix} \beta_b \\ \beta_w \end{bmatrix} = \begin{bmatrix} \dfrac{\sum\limits_i n_i(p_i - q_i)\mu_i}{NV_b} + a \\ a \end{bmatrix} \ .$$

Appendix C

$E(\beta_b)$ and $E(\beta_w)$ with Use of Sibling Genotypes Only

When one parent is heterozygous, consider allelic transmission $t \sim$ binomial $(n_i, \frac{1}{2})$, so that $E(t^2) = (\frac{1}{4})(n_i^2 + n_i)$. When the heterozygous and homozygous parents transmit the same allele t times, $|b| = t/n_i$. Thus, for any family i,

$$E(b_i^2|C_1) = E(|b_i|^2|C_1) = \frac{E(t^2)}{n_i^2} = \frac{n_i + 1}{4n_i} \ ,$$

where C_1 denotes the condition that exactly one parent is heterozygous.

To calculate $E(by)$, it is convenient to separate y into its orthogonal-mean, μ, and major-gene, ga, components. Recall that $b_i = (1/n_i)\Sigma_j g_{ij}$, so that, when one parent is heterozygous, the major-gene component is

$$E(b_i g_i a|C_1) = E\left(\frac{b_i g_{i1} a + \cdots + b_i g_{in_i} a}{n_i} \,\bigg|\, C_1\right) = E\left(b_i \frac{\sum_j g_{ij}}{n_i} \,\bigg|\, C_1\right)a = E(b_i^2|C_1)a = \frac{E(t^2)a}{n_i^2} = \frac{n_i + 1}{4n_i}a \ .$$

When two parents are heterozygous, consider allelic transmission $t' \sim$ binomial $(2n_i, \frac{1}{2})$, so that $E(t') = n_i$ and $E(t'^2) = (\frac{1}{4})(4n_i^2 + 2n_i)$. When allele 1 (or 2) is transmitted t' times, $|b| = |t'/n_i - 1|$. So, for any family i,

$$E(b_i^2|C_2) = E(|b_i|^2|C_2) = E\left[\left(\frac{t'}{n_i} - 1\right)\right]^2 = \frac{4n_i + 2}{4n_i} - 1 = \frac{1}{2n_i} \ ,$$

and the major-gene component of $E(by)$ is

$$E(b_i g_i a|C_2) = E\left(\frac{b_i g_{i1} a + \cdots + b_i g_{in_i} a}{n_i} \,\bigg|\, C_2\right) = E(b_i^2|C_2)a = E\left[\left(\frac{t'}{n_i - 1}\right)^2\right]a = \frac{1}{2n_i}a \ ,$$

where C_2 denotes the condition that both parents are heterozygous.

When C_1 and C_2 are considered, together with $E(y)$, $E(g)$, $E(g^2)$, and $E(gy)$ given in Appendix A, and the mating-type frequencies

$$E(b^2) = \frac{\sum_i n_i \sum_z P(z|i)E(b^2|z)}{N} = \frac{\sum_i n_i[p_i^4 + q_i^4 + 4p_i q_i^3(\frac{n_i+1}{4n_i}) + 4p_i^3 q_i(\frac{n_i+1}{4n_i}) + 4p_i^2 q_i^2(\frac{1}{2n_i})]}{N} = \frac{\sum_i n_i[p_i^2 + q_i^2 - p_i q_i(\frac{n_i-1}{n_i})]}{N} \ ,$$

and

$$E(w^2) = E[(g - b)^2] = \frac{\sum_i n_i p_i q_i(\frac{n_i-1}{n_i})}{N} = \frac{\sum_i p_i q_i(n_i - 1)}{N} \ ,$$

and, when the component derivations of $E(by)$ are used,

$$E(by) = \frac{\sum_i n_i E[b(\mu + ga)|i]}{N} = \frac{\sum_i n_i E(b\mu|i)}{N} + \frac{\sum_i n_i E(bga|i)}{N} = \frac{\sum_i n_i(p_i - q_i)\mu_i}{N} + E(b^2)a \ ,$$

and

$$E(wy) = E[(g - b)y] = E(gy - by) = \frac{\sum\limits_i n_i[p_iq_i(\frac{n_i-1}{n_i})]a}{N} = \frac{\sum\limits_i p_iq_i(n_i - 1)a}{N} \ .$$

Thus,

$$\mathbf{X'X} = \begin{bmatrix} V_b & C_{b,w} \\ C_{b,w} & V_w \end{bmatrix} = \begin{bmatrix} \dfrac{\sum\limits_i n_i[p_i^2 + q_i^2 - p_iq_i(\frac{n_i-1}{n_i})]}{N} - \dfrac{\left[\sum\limits_i n_i(p_i - q_i)\right]^2}{N^2} & 0 \\ 0 & \dfrac{\sum\limits_i p_iq_i(n_i - 1)}{N} \end{bmatrix}$$

and

$$\mathbf{Xy} = \begin{bmatrix} C_{b,y} \\ C_{w,y} \end{bmatrix} = \begin{bmatrix} \dfrac{\sum\limits_i n_i(p_i - q_i)\mu_i}{N} + V_b a \\ \dfrac{\sum\limits_i p_iq_i(n_i - 1)}{N} a \end{bmatrix},$$

so that

$$\hat{b} = \begin{bmatrix} \beta_b \\ \beta_w \end{bmatrix} = \begin{bmatrix} \dfrac{\sum\limits_i n_i(p_i - q_i)\mu_i}{NV_b} + a \\ a \end{bmatrix} \ .$$

Electronic-Database Information

The URL for data in this article is as follows:

The Wellcome Trust Centre for Human Genetics, http://well.ox.ac.uk (for QTDT computer program)

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