

Random Variable

- A variable that has a single numerical value, determined by chance, for each outcome of a procedure
 - The number of eggs a hen lays in a day
 - The amount of milk a cow produces in a day

Probability Distribution

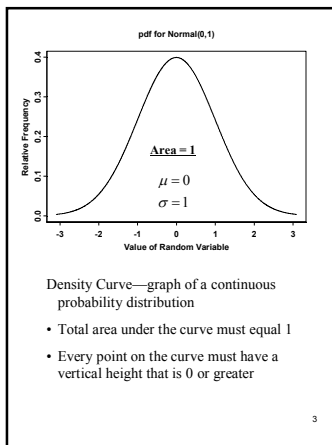
- A description that gives the probability for each value of the random variable
- Usually expressed as a graph, table, or formula

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Requirements for a Probability Distribution

1. $\sum_{\text{all } x} P(x) = 1$
2. For every individual value of x
 $0 \leq P(X \leq x) \leq 1$

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Statistical Inference

- Will be making statements about means or proportions
- Will take into account variability among samples
 - The value of a statistic depends on the particular values in the sample. Values generally vary from sample to sample
 - Variability of a statistic is called **sampling variability**

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Central Limit Theorem

If

- The random variable has a distribution (any distribution) with mean μ and standard deviation σ
- Simple random samples all of the same size n are selected from the population

Then

- The distribution of sample means will approach a normal distribution
- The mean of all sample means is the population mean μ
- The standard deviation of all sample means is σ/\sqrt{n}

Can be extended to proportions

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Confidence Intervals

Point Estimator —is a single value or point used to approximate a population

Confidence Interval (CI) —is a range of values used to estimate the true value of a population parameter

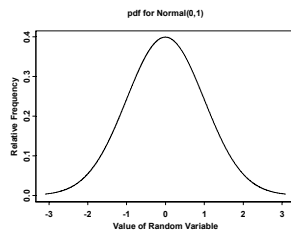
Confidence Level —represents the proportion of times that the confidence interval actually does contain the population parameter assuming that the estimation process is repeated a large number of times

Common choices for confidence levels are 90%, 95%, and 99%

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Form of a Confidence Interval

$$\text{point estimator} \pm (\text{critical value} \times \text{SE}_{\text{point estimator}})$$



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Interpreting a CI

Correct:

We are 95% confident that the interval actually does contain the true value of the population parameter. This means that if we collected many different samples of size n and constructed the corresponding CIs, 95% of them would actually contain the value of the population parameter.

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Interpreting a CI

Wrong:

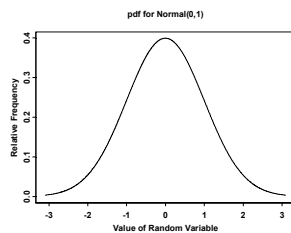
There is a 95% chance (probability) that the true population parameter will fall between (lower bound, upper bound)—at any specific point in time a population has a fixed and constant value of the population parameter and a confidence interval constructed from a sample either includes the parameter value or does not.

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Increasing Confidence

- Choose a higher confidence level—for a fixed sample size, this will effectively increase the width of the interval
- Increase the sample size—for a fixed confidence level, a larger sample will produce a narrower interval

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