

## Fregean Semantics: Denotation (reference)

All linguistic expressions (proper names, predicates, sentences) denote **objects**.

- The denotation of a proper name is an **individual**.
- The denotation of a predicate is a **function** (which maps one object as *argument* to another object as *value*).
- The denotation of a sentence is a **truth-value**.
- A **concept** is a function whose values are truth-values.

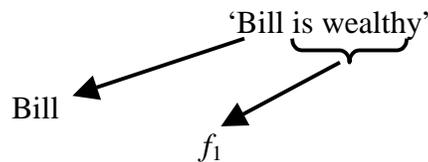
Example: 'Bill is wealthy'

'Bill' denotes Bill.

'is wealthy' denotes a function,  $f_1$ .

$\text{Bill} = \mathbf{D}(\text{'Bill'})$

$f_1 = \mathbf{D}(\text{'is wealthy'})$



$f_1$  maps individuals onto truth-values:  
That is,  $f_1$  maps Bill onto The True.

$f_1(\text{Bill}) = \text{The True}$

$\mathbf{D}(\text{'Bill is wealthy'})$  is a function of  $\mathbf{D}(\text{'Bill'})$  and  $\mathbf{D}(\text{'is wealthy'})$ .

$\mathbf{D}(\text{'Bill is wealthy'}) = \text{The True}$

The denotation of the entire sentence is a function of the denotations of its parts.

Example: 'Bill loves Melinda'

'Bill' denotes Bill.

'Melinda' denotes Melinda.

'loves' denotes a function,  $f_2$ .

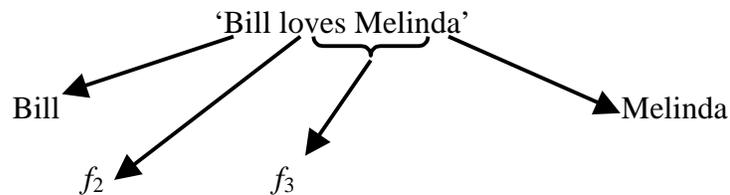
'loves Melinda' denotes a function,  $f_3$ .

$\text{Bill} = \mathbf{D}(\text{'Bill'})$

$\text{Melinda} = \mathbf{D}(\text{'Melinda'})$

$f_2 = \mathbf{D}(\text{'loves'})$

$f_3 = \mathbf{D}(\text{'loves Melinda'})$



$f_2$  maps individuals onto functions:  
That is,  $f_2$  maps Melinda onto  $f_3$ .

$f_2(\text{Melinda}) = f_3$

$f_3$  maps individuals onto truth-values:  
That is,  $f_3$  maps Bill onto The True.

$f_3(\text{Bill}) = \text{The True}$

$\mathbf{D}(\text{'Bill loves Melinda'})$  is a function of  $\mathbf{D}(\text{'Bill'})$ ,  $\mathbf{D}(\text{'Melinda'})$ , and  $\mathbf{D}(\text{'loves'})$ .

$\mathbf{D}(\text{'Bill loves Melinda'}) = \text{The True}$

Again, the denotation of the entire sentence is a function of the denotations of its parts.

## Fregean Semantics: Sense

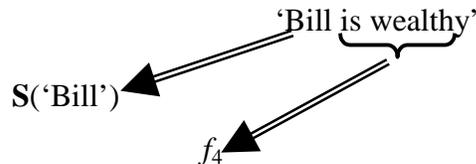
All linguistic expressions (proper names, predicates, sentences) express **senses**.

- The sense of a predicate is a **function** from a sense to a sense.
- The sense of a sentence is a **thought** (i.e., a proposition).

Example: ‘Bill is wealthy’

‘Bill’ expresses  $S(\text{‘Bill’})$ .

‘is wealthy’ expresses a function,  $f_4$ .       $f_4 = S(\text{‘is wealthy’})$



$f_4$  maps senses onto thoughts:       $f_4(S(\text{‘Bill’})) = S(\text{‘Bill is wealthy’})$

That is,  $f_4$  maps  $S(\text{‘Bill’})$  onto the sense of ‘Bill is wealthy’.

$S(\text{‘Bill is wealthy’})$  is the *thought*, or proposition, that Bill is wealthy.

$S(\text{‘Bill is wealthy’})$  is a function of  $S(\text{‘Bill’})$  and  $S(\text{‘is wealthy’})$ .

That is, the sense of the entire sentence is a function of the senses of its parts.

Example: ‘Bill loves Melinda’

‘Bill’ expresses  $S(\text{‘Bill’})$ .

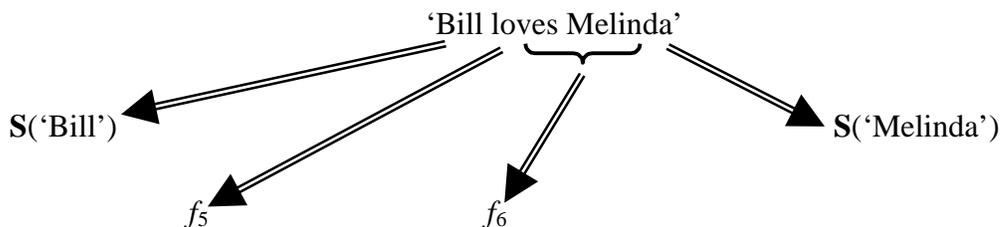
‘Melinda’ expresses  $S(\text{‘Melinda’})$ .

‘loves’ expresses a function,  $f_5$ .

‘loves Melinda’ expresses a function,  $f_6$ .

$f_5 = S(\text{‘loves’})$

$f_6 = S(\text{‘loves Melinda’})$



$f_5$  maps senses onto functions:       $f_5(S(\text{‘Melinda’})) = f_6$ .

That is,  $f_5$  maps  $S(\text{‘Melinda’})$  onto  $f_6$ , the function that is the sense of ‘loves Melinda’.

$f_6$  maps senses onto thoughts:       $f_6(S(\text{‘Bill’})) = S(\text{‘Bill loves Melinda’})$

That is,  $f_6$  maps  $S(\text{‘Bill’})$  onto the thought that Bill loves Melinda.

$S(\text{‘Bill loves Melinda’})$  is a function of  $S(\text{‘Bill’})$ ,  $S(\text{‘Melinda’})$ , and  $S(\text{‘loves’})$ .

That is, the sense of the entire sentence is a function of the senses of its parts.