

Glossary

"I learned very early the difference between knowing the name of something and knowing something."

- Richard Feynman

Active control – A controller that expends energy to accomplish a control task. For example, an automobile cruise-controller will actively control the fuel and brakes to regulate forward velocity.

Adaptive control – A controller that modifies its action to optimize performance or account for varying system parameters or externally varying conditions.

Actuator – A device that modifies the system according to the control input. The actuation effect is typically modeled by the structure of the **B** matrix in a control system.

Crossover – A genetic operation where two individuals exchange a portion of their expression, thereby increasing diversity of the future generation. Crossover tends to exploit successful patterns in the parent individuals to produce more fit offspring in future generations.

Closed-loop control – The process of controlling actuators based on sensor measurements.

Clustering – Identifying groups of similar data. If the data are labeled, this is called *supervised*, and if the data is not labeled, it is *unsupervised*.

Coherent structures – A structure in a dynamical system that remains coherent, or spatially correlated, for some time; here spatial correlation typically refers to

the state of the dynamical system. In fluids, coherent structures often refer to persistent vortical structures that stay intact despite turbulent fluctuations.

Control theory – The theory of processes which modify a system for an engineering goal, often with actuators and sensors.

Cost function – A function that quantifies the cost or penalty of a given control law or estimator.

Disturbance – An external perturbation to the system that passes through the dynamics, also known as *process noise*. Disturbances are typically seen as unwanted perturbations that degrade performance, such as unreliable or unpredictable environmental conditions.

Dynamical system – A model for how a state evolves in time, possibly in response to an actuation signal and external disturbances. The dynamical system may have an *output equation* that consists of a set of measurements of the state and actuation signal. A dynamical system may either be *nonlinear* or *linear*, and they are often represented as a system of ordinary differential equations.

Elitism – A genetic operation whereby the best individual(s) from a generation are automatically copied to the next generation without probabilistic selection based on fitness.

Estimator – A dynamical system that estimates the state of another dynamical system from a limited set of measurements. See *Kalman filter*.

Evolutionary algorithm – An algorithm that adapts over time (generations) according to a fitness or cost function.

Exploitation – The process in an evolutionary algorithm whereby successful patterns in individuals of a given generation are *exploited* to produce more fit individuals in the next generation. Crossover is a genetic operation that promotes exploitation.

Exploration – The process in an evolutionary algorithm whereby new, unexplored patterns are sought out for individuals in future generations. Mutation is a genetic operation that promotes exploration.

Expression tree – A function or expression that may be expressed as a tree, where each node represents a unary or binary mathematical operation, such as $+$, $-$, \times , $/$, \sin , \cos , etc. Function trees may be quickly evaluated using recursion.

- Feedback control** – A closed-loop control architecture, whereby a downstream sensor measurement is fed back to an upstream actuator.
- Feedforward control** – A control architecture, whereby an upstream sensor measurement is fed forward to a downstream actuator. Often feedforward control is used to measure an incoming disturbance and apply preventative control downstream; this is known as *disturbance feedforward control*.
- Fitness function** – A function that measures the success of an individual expression in achieving some goal. Often inversely related to the *cost function*. In genetic algorithms and genetic programming, the fitness function determines the probability that an individual will be selected for the next generation.
- Flow control** – The process of modifying a fluid system to achieve some engineering goal. This is often accomplished by *active* control, whereby energy is expended to actuate the flow. High-level goals often include lift increase, drag reduction, mixing enhancement, and these goals may be achieved by physical mechanisms such as relaminarizing a boundary layer or stabilizing an unstable shear layer.
- Frequency crosstalk** – A phenomena in nonlinear dynamics where a signal or behavior at one frequency can effect or modify a signal or behavior at another frequency. In a linear system, input forcing at a single fixed frequency will result in an output response with the same frequency and a new magnitude and phase. However, in a nonlinear system, forcing a system at a single fixed frequency may result in an output response where multiple frequencies are modified through nonlinear coupling mechanisms.
- Generation** – A collection of individuals to be tested in a genetic algorithm or in genetic programming. The performance of these individuals are evaluated, and each individual's *fitness function* determines the probability of advancing to the next generation via the *genetic operations*.
- Genetic algorithm** – An evolutionary algorithm to optimize the parameters of an expression with a pre-specified structure.
- Genetic operation** – A set of operations to advance individuals from one generation to the next. These operations include *elitism*, *replication*, *crossover*, and *mutation*. Individuals are selected for these operations depending on their *fitness function*.
- Genetic programming** – An evolutionary algorithm to optimize both the structure and parameters of an expression or a function; often referred to as *semantic regression*.

Genetic programming control – The process of discovering an effective control law by using genetic programming to construct functions relating sensor measurements to an actuation signal.

Individual – A candidate expression in a genetic algorithm or genetic programming. Each individual is tested, resulting in a fitness function that determines its probability of propagating to the next generation.

Kalman filter – A dynamical system that estimates the full-state of another dynamical system from measurements of the sensor outputs and actuation inputs. The Kalman filter is an optimal state estimator for a linear system with additive Gaussian process and measurement noise.

Linear system – A dynamical system where superposition holds for solutions. This implies that doubling the initial condition and the control input signal will result in exactly twice the output. Often, the system will be a *linear time invariant* (LTI) system, so that the dynamics may be characterized entirely by linear operators (matrices).

Linear quadratic Gaussian (LQG) – An optimal sensor-based feedback control law that consists of a linear quadratic regular feedback law applied to the full-state estimate from a Kalman filter. The LQG controller is optimal for a linear system with the same quadratic cost function as in LQR and additive Gaussian white process and measurement noise of known magnitude.

Linear quadratic regulator (LQR) – An optimal full-state feedback control law to stabilize the state of a linear system while not expending too much actuation energy. LQR is optimal with respect to a quadratic cost function that balances deviation of the state and control expenditure.

Linearization – The process of approximating a nonlinear dynamical system by a linear dynamical system near a fixed point or periodic orbit by truncating a Taylor series of the dynamics at first order. Linearization is valid for small state perturbations in a small neighborhood of the fixed point or periodic orbit.

Machine learning – A set of techniques to automatically generate models from data that may be generalized and improve with more data. Machine learning is often applied to high-dimensional data where it is difficult to identify patterns and relationships in the data. Common techniques include classification and regression tasks, and these may be either supervised by expert input or unsupervised algorithms.

Machine learning control – The process of determining effective control laws through the use of machine learning methods. Controllers are *learned* through a guided process that is informed by measured performance data as opposed to

being derived from first principles or optimization routines.

Mean-field model – In fluid mechanics, a mean-field model is a low-order Galerkin model linking base-flow changes with fluctuations. In the most simple case, a mean-field model describes the soft onset of an oscillation via a supercritical Hopf bifurcation. This is also referred to as *Watson-Stuart model* or *weakly nonlinear theory* and implies the famous *Landau equation* for a supercritical Hopf bifurcation. Generalized models may incorporate several frequencies and do not require the closeness of a bifurcation.

Measurement noise – Noise that is added to the output equation of a dynamical system, thus not being affected by the dynamics. Often simply referred to as *noise*.

Model – A mathematical expression that describes a system. Often, a model is derived from first-principles by physical arguments, such as conservation of mass, momentum and energy. Alternatively, a model may be derived from observational data about the system, as in statistics, system identification, and machine learning. Dynamic models are often represented as a coupled system of differential equations relating the various quantities under observation.

Model reduction – The process of approximating a high-fidelity model with a smaller, more computationally efficient model in terms of fewer states. Model reduction is an important step when controlling high-dimensional systems, since determining and evaluating control laws based on high-fidelity models is often computationally prohibitive. Moreover, control performance may be limited by the latency of a control decision, so faster decisions resulting from reduced-order models are often beneficial.

Mutation – A genetic operation where a portion of an individual in the current generation is randomly altered to produce a new individual in the next generation. Mutation tends to promote exploration in the search space of possible individuals.

Open-loop control – A method of control that specifies a pre-determined input sequence without correction or adaptation via sensors. A common method of open-loop control is periodic forcing.

Neural network – A network representation of an input–output function that attempts to mimic the computational flexibility observed in biological networks of neurons. A neural network consists of a group of individual computational components, or neurons, that are connected in a network or graph structure to perform some computation. Neural networks are typically characterized by their *adaptability* and *trainability* to new stimulus.

- Noise** – A quantity that varies randomly in time and is added to some variable in a dynamical system. If added to the state equation, it is also known as a *disturbance* or *process noise*, and if added to the output equation, it is also known as *measurement noise*. Noise is often assumed to follow a Gaussian white noise process, although it may also be correlated or *colored*.
- Nonlinear system** – A system of equations or a dynamical system that is characterized by nonlinear dynamics. As opposed to a linear system, a nonlinear system does not satisfy superposition of solutions, resulting in complex behavior, including frequency crosstalk and chaos.
- Passive control** – A controller that modifies a system without energy expenditure. Examples include vortex generators on wings that passively delays flow separation over a wing.
- Plant** – In control theory, the plant refers to the model system being controlled along with the actuator.
- Process noise** – Noise that is added to the state equation of a dynamical system, thereby passing through the dynamics. Also called a *disturbance*.
- Real-time control** – A control law that modifies the system on a time scale that is fast compared with the natural time scale. Also referred to as *in-time* control.
- Reduced-order model** – An approximate model with fewer states than the full high-fidelity system. Reduced-order models are often desirable in the control of high-dimensional systems, such as fluids, to reduce computational overhead, leading to faster, lower-latency control decisions.
- Regression** – A statistical model that relates multiple variables from measurement data. The method of least squares is a simple *linear* regression that determines a best-fit line relating data. Least-squares regression may be generalized to higher dimensions in what is known as the principal components analysis (PCA). More generally, nonlinear regression, dynamic regression, and functional or semantic regression are used to determine complex and possibly time-varying relationships between variables. Regression is commonly used in both *system identification*, *model reduction*, and *machine learning*.
- Regulator** – A control law that maintains a set-point in the state variable. See *linear quadratic regulator*.
- Replication** – A genetic operation where individuals are copied directly from one generation to the next. These individuals are selected probabilistically based on their fitness, so that the most fit individuals are more likely to advance.

- Reynolds number** – A dimensionless quantity that measures the ratio of inertial and viscous forces in a fluid. The Reynolds number may also be thought of as a rough measure of the ratio of the size of the largest vortices and the smallest vortices in a flow. Thus, a volcanic eruption will constitute an extremely high Reynolds number flow, as there are both very large and very small eddies.
- Robust control** – The field of control theory where controllers are designed to be inherently robust to model uncertainty, unmodeled dynamics, and disturbances. Often referred to as \mathcal{H}_∞ *optimal control*.
- Selection** – The process of selecting individuals from one generation for the next generation via a genetic operation. The individuals are selected randomly but with a bias for individuals with a higher fitness, and these individuals are advanced using one of the *genetic operations*.
- Sensor** – A device that measures the system, producing an output. The sensor effect is typically modeled by the structure of the **C** matrix in a control system.
- Stability** – A property of a system, referring to how it behaves for long times or when it is perturbed. For example, a fixed point of a dynamical system is *stable* if small perturbations around this fixed point result in trajectories that stay near the fixed point and do not leave a neighborhood of the fixed point. A fixed point of a linear system is unstable if some initial conditions near the fixed point result in trajectories that grow and leave the neighborhood.
- State-space system** – A model consisting of a coupled system of ordinary differential equations in terms of a collection of variables known as the *state variable*. The state variable represents the state of the system, and it is an element of a vector space or manifold, known as the *state space*.
- System identification** – The process of determining a model for a physical process based on measurement data. Typically, system identification involves measuring the sensor output of a system in response to certain actuation inputs, and a model for the underlying state dynamics (i.e., hidden variables) is constructed. Most methods of system identification may be viewed as a form of dynamic regression of data onto models.
- Turbulence** – A fluid phenomena characterized by multi-scale coherent vorticity in space and time and strongly nonlinear, chaotic dynamics. Turbulence is often a characteristic of real-world or industrial flows at high *Reynolds number*.

Symbols

\mathbf{A} ; \mathbf{A}_d ; $\tilde{\mathbf{A}}$	State matrix (continuous time ; discrete time ; reduced).
\mathbf{a} ; \mathbf{a}_k ; a_m ; a	State (vector, continuous time ; vector, discrete time k^{th} step ; m^{th} component ; scalar).
$\hat{\mathbf{a}}$; $\hat{\mathbf{a}}_k$	Full state estimate (continuous ; discrete time).
\mathbf{B} ; \mathbf{B}_d ; $\tilde{\mathbf{B}}$	Input matrix (continuous ; discrete time ; reduced).
B	Amplitude of periodic forcing.
\mathbf{b} ; \mathbf{b}_k ; b_m ; b	Actuation command (vector, continuous time ; vector, discrete time k^{th} step ; m^{th} component ; scalar).
\mathcal{B}	Matrix of control inputs.
\mathbf{C} ; \mathbf{C}_d ; $\tilde{\mathbf{C}}$	Output matrix (continuous ; discrete time ; reduced).
c_μ	Momentum coefficient.
\mathcal{C} ; \mathcal{C}_d	Controllability matrix (continuous ; discrete time).
\mathbf{D} ; \mathbf{D}_d ; $\tilde{\mathbf{D}}$	Feedthrough matrix (continuous ; discrete time, reduced).
D	Characteristic distance.
d_c	Duty cycle.
$\mathbf{e}_x, \mathbf{e}_y, \mathbf{e}_z$	Unity vectors associated with directions x , y and z .
\mathbb{E}	Expectation operator.
\mathbf{F}	Dynamics.
F_D	Drag force.
\mathbf{G}	Measurement function.
g	Gain of control command in a generalized mean-field model.
\mathbf{H}	Hankel matrix.
H	Heavyside function.
H_{section}	Height of the test section.
$h_i(t)$; $h_{i,u}$; $h_{i,\text{max}}$	hot-wire or hot-film signal number i (raw signal ; average value of the unactuated measurement ; average measurement under constant maximal actuation).
h_{step} ; h_{ramp}	Height (of the step ; of the ramp).

I	Identity matrix.
i	Index of individual (or other counter).
$J ; J_i^j$	Cost function value ; of individual i in generation j .
J_a	Cost on states.
J_b	Cost on actuation.
j	Index of generation.
K	Control function.
\mathbf{K}_f	Kalman filter gain.
\mathbf{K}_r	Regulator gain, full-state control matrix.
L	Length of the experimental test section.
L_{sep}	Separation length.
l	Width of the experimental test section.
ℓ	Ramp length.
N_a	Number of states.
N_b	Number of actuation commands.
N_e	Number of individuals concerned by elitism.
N_g	Number of generations.
N_i	Number of individuals.
N_p	Tournament size.
N_s	Number of sensors.
$\mathcal{O} ; \mathcal{O}_d$	Observability matrix (continuous time ; discrete time).
P_c	Probability of crossover.
P_m	Probability of mutation.
P_r	Probability of replication.
p	Pressure.
$p(\mathbf{a})$	Probability density of states.
Q	State cost weight matrix for LQR.
$\dot{Q} ; Q_u$	Flow rate to actuator jets (instantaneous ; average value under constant blowing).
R	Actuation cost weight matrix for LQR.
r_\bullet, r_\circ	Amplitude of oscillators of a generalized mean-field model (Tab. 5.1).
Re	Reynolds number.
$S_a(t) ; S_{a,u}$	Area of backflow (instantaneous ; unactuated average value).
S_b	Actuator cross section.
S_j	Jet cross section.
S_{ref}	Ramp reference surface.
$\mathbf{s} ; \mathbf{s}_k ; s_m ; s$	Sensor signal (vector, continuous time ; vector, discrete time k^{th} step ; m^{th} component ; scalar).
$\hat{\mathbf{s}} ; \hat{\mathbf{a}}_k$	Expected sensor value (continuous time ; discrete time).
$\mathcal{S} ; \bar{\mathcal{S}}$	Markov parameters ; of the augmented system.
T	Evaluation time.
T_{rms}	Time period used to compute RMS of hot-wire signal fluctuations.
t, t_0	Time, initial time.

$\mathbf{U}; \mathbf{U}_r$	Left singular vectors of SVD (complete ; reduced) .
U	Characteristic velocity.
$\mathbf{u}; \mathbf{u}_s, \mathbf{u}_\Delta, \mathbf{u}_\bullet, \mathbf{u}_\circ$	Velocity (vector field ; steady solution ; deviation due to Reynolds stresses ; contribution of frequency ω_\bullet ; contribution of frequency ω_\circ).
$\bar{\mathbf{u}}$	Slow varying mean flow.
\mathbf{u}'	Flow fluctuations.
u	Streamwise velocity component.
$\mathbf{V}; \mathbf{V}_r$	Right singular vectors of SVD (complete ; reduced).
\mathbf{V}_d	Disturbance variance.
\mathbf{V}_n	Noise variance.
V_{Jet}	Characteristic velocity of jets.
\mathbf{v}	Velocity vector initial condition.
v	Transverse velocity component.
\mathbf{W}_ϵ^d	Discrete time controllability Gramian.
\mathbf{W}_θ^d	Discrete time observability Gramian.
W	mixing layer width.
\mathbf{w}	Disturbance array.
\mathbf{w}_r	External reference signal.
\mathbf{w}_d	External disturbance, process noise.
\mathbf{w}_n	Measurement noise.
w	Spanwise velocity component.
\mathbf{X}	Solution to the Riccati equation for LQR.
\mathbf{x}	Space vector.
x	Streamwise coordinate.
\mathbf{Y}	Solution to the Riccati equation for Kalman filter.
y	Transverse coordinate.
\mathbf{z}	System output.
z	Spanwise coordinate.
$\beta_{\bullet\bullet}, \beta_{\bullet\circ}, \beta_{\circ\bullet}, \beta_{\circ\circ}$	Parameter for growth-rate change in oscillators of a generalized mean-field model (Tab. 5.1).
γ	Penalization coefficient.
$\gamma_{\bullet\bullet}, \gamma_{\bullet\circ}, \gamma_{\circ\bullet}, \gamma_{\circ\circ}$	Parameter for frequency change in oscillators for a generalized mean-field model (Tab. 5.1).
$\delta(\cdot)$	Dirac delta function.
ϵ	Nonlinearity strength coefficient or state stabilisation error.
κ	Gain of the generalized mean-field model.

ν	Kinematic viscosity.
ρ	Fluid density.
$\Sigma ; \Sigma_r$	Singular values matrix of SVD, (complete ; reduced) .
σ	Oscillator growth rate.
$\sigma_{\bullet} ; \sigma_{\bullet\star} ; \sigma_{\circ} ; \sigma_{\circ\star}$	Growth rate of oscillators of a generalized mean-field model (Tab. 5.1).
$\tau ; \tau_a ; \tau_u$	Period of time (with actuated system ; with unactuated system).
$\phi_{\bullet}, \phi_{\circ}$	Phase of oscillators in a generalized mean-field model (Tab. 5.1).
χ	Back-flow coefficient.
Ω	Space domain.
ω	Oscillator pulsation.
$\omega_{\bullet} ; \omega_{\bullet\star} ; \omega_{\circ} ; \omega_{\circ\star}$	Frequency of oscillators in a generalized mean-field model (Tab. 5.1).

Abbreviations

ANN...	Artificial Neural Network
ARMA(X)...	Auto-Regressive Moving Average (with eXogenous input)
AVERT...	Aerodynamic Validation of Emission Reducing Technologies
BPOD...	Balanced Proper Orthogonal Decomposition
CROM...	Cluster-based Reduced Order Modeling
DEIM...	Discrete Empirical Interpolation Method
DMD...	Dynamic Mode Decomposition
EC...	Evolutionary Computing
EP...	Evolutionary Programming
ERA...	Eigensystem Realization Algorithm
GA...	Genetic Algorithm
GMFM...	Generalized Mean-Field Model
GP...	Genetic Programming
LQE...	Linear Quadratic Estimation
LQG...	Linear Quadratic Gaussian
LQR...	Linear Quadratic Regulator
LML...	Laboratoire de Mécanique de Lille, Université de Lille 1 Cité Scientifique, Bâtiment M3 - 59655 Villeneuve d'Ascq Cedex, France
LPV...	Linear Parameter Varying
MIMO...	Multiple Input Multiple Output
MISO...	Multiple Input Single Output
ML...	Machine Learning
MLC...	Machine Learning Control
NLSA...	Nonlinear Laplacian Spectral Analysis
OKID...	Observer Kalman filter IDentification
PCA...	Principal Component Analysis

PID...	Proportional Integral Derivative
PIV...	Particle Image Velocimetry
PMMH...	Physique et Mecanique des Millieux Hétérogènes Laboratory, 10 rue Vauquelin - 75231 Paris Cedex, France
POD...	Proper Orthogonal Decomposition
PPRIME...	Institute Pôle Poitevin de Recherche pour l'Ingénieur en Mécanique, Matériaux et Énergétique, 11 Boulevard Marie et Pierre Curie BP 30179 - 86962 Futuroscope Chasseneuil Cedex, France
PRISME...	Laboratoire Pluridisciplinaire de Recherche, Ingénierie des Systèmes, Mécanique, Énergétique. Université d'Orléans 8 Rue Léonard de Vinci - 45072 Orléans, France.
ROM...	Reduced Order Model
RT...	Real-Time
SIMO...	Single Input Multiple Output
SISO...	Single Input Single Output
SSA...	Singular Spectrum Analysis
SVM...	Support Vector Machine
TUCOROM...	TURbulence COntrol using Reduced Order Models, ANR Chair of Excellence (ANR-10-CEXC-0015), Poitiers, France.
UVG...	Unsteady Vortex Generator

Matlab[®] Code: OpenMLC

This appendix describes OpenMLC, the employed implementation of MLC in Matlab[®]. All examples in the book have been performed with this software.

Installation

OpenMLC is a Matlab[®] toolbox. It can be added to Matlab[®] by downloading the toolbox from [94] or duplicate the master branch. The root directory of the toolbox, **OpenMLC**, needs to be added to the path with subdirectories. Detailed or alternative instructions will be available from the Github repository [94] as the software is updated.

Content

OpenMLC contains a class defined by the file `MLC.m` in the folder `@MLC`. This class implements all methods discussed in the book. Additionally, a folder **MLCtools** is provided. It provides the `MLCparameters` class description files which implements all parameters. Also functions such as expression-tree interpreter, derivation function, common function overloading for protection are provided in this folder. Finally this folder also contains the **Examples** subfolder that contains all configuration files, evaluation function, and typical results discussed in this book.

The reader is referred to the documentation of the software:

```
help MLC           % class description and first steps. Also
                  % list all properties of the MLC class and
                  % its methods.
help MLC/parameters % will list all configuration parameters
                  % and available options
```

for a quick starting guide. Contextual help is available for each method by typing:

```
help MLC/METHOD % will provide help for METHOD
```

A full package documentation is available on the Github repository [94]. Any bug report, feature request or participation can be brought to our attention through the Github repository.

Bibliography

1. Nobel Media AB. Nobel peace prize. http://www.nobelprize.org/nobel_prizes/peace/laureates/2007/, 2007.
2. Y. S. Abu-Mostafa, M. Magdon-Ismail, and H.-T. Lin. *Learning from Data. A Short Course*. AMLBook, 2012.
3. International Energy Agency. Key world energy statistics. <http://www.iea.org/publications/freepublications/publication/keyworld2014.pdf>, 2014.
4. S. R. Ahmed, G. Ramm, and G. Faltin. Some salient features of the time averaged ground vehicle wake. *Society of Automotive Engineers, SAE Inc*, 840300, 1984.
5. J.-L. Aider, 2014. Private communication.
6. K. Aleksic, D. M. Luchtenburg, R. King, B. R. Noack, and J. Pfeiffer. Robust nonlinear control versus linear model predictive control of a bluff body wake. In *5th AIAA Flow Control Conference*, pages 1–18, Chicago, USA, 2010. AIAA Paper 2010-4833.
7. M. R. Allen and L. A Smith. Monte Carlo SSA: Detecting irregular oscillations in the presence of colored noise. *J. Climate*, 9(12):3373–3404, 1996.
8. M. Amitay and A. Glezer. Role of actuation frequency in controlled flow reattachment over a stalled airfoil. *AIAA Journal*, 40(2):209–216, 2002.
9. B. F. Armaly, F. Durst, J. C. F. Pereira, and B. Schönung. Experimental and theoretical investigation of backward-facing step flow. *J. Fluid Mech.*, 127:473–496, 1983.
10. S. Aubrun, J. McNally, F. Alvi, and A. Kourta. Separation flow control on a generic ground vehicle using steady microjet arrays. *Exp. Fluids*, 51(5):1177–1187, 2011.
11. S. Bagheri, L. Brandt, and D.S. Henningson. Input-output analysis, model reduction and control of the flat-plate boundary layer. *J. Fluid Mechanics*, 620:263–298, 2009.
12. S. Bagheri and D. S. Henningson. Transition delay using control theory. *Phil. Trans. R. Soc. A*, 369(1940):1365–1381, 2011.
13. S. Bagheri, J. Hoepffner, P. J. Schmid, and D. S. Henningson. Input-output analysis and control design applied to a linear model of spatially developing flows. *Appl. Mech. Rev.*, 62(2):020803–1..27, 2009.
14. Z. Bai, S. L. Brunton, B. W. Brunton, J. N. Kutz, E. Kaiser, A. Spohn, and B. R. Noack. Data-driven methods in fluid dynamics: Sparse classification from experimental data. In A. Polard, editor, *Whither Turbulence and Big Data in the 21st Century*. To appear in Springer, 2016.
15. C. J. Baker. Ground vehicles in high cross winds. Part I: Steady aerodynamic forces. *J. Fluid Struct.*, 5(1):69–90, 1991.
16. B. Bamieh and L. Giarré. Identification of linear parameter varying models. *Int. J. Rob. Nonl. Cont.*, 12:841–853, 2002.

17. W. Banzhaf, P. Nordin, R. E. Keller, and R. D. Francone. *Genetic Programming: An Introduction*. Morgan Kaufmann, San Francisco, 1998.
18. R. G. Baraniuk. Compressive sensing. *IEEE Signal Processing Magazine*, 24(4):118–120, 2007.
19. D. Barros. *Wake and drag manipulation of a bluff body using fluidic forcing*. PhD thesis, École Nationale Supérieure de Mécanique et d’Aérotechnique, Poitiers, France, 2015.
20. D. Barros, J. Borée, B. R. Noack, A. Spohn, and T. Ruiz. Bluff body drag manipulation by unsteady shear layer forcing and Coanda blowing. *J. Fluid Mech.*, in revision, see arXiv:1507.02243 [physics.flu-dyn], 2016.
21. D. Barros, T. Ruiz, J. Borée, and B. R. Noack. Control of a three-dimensional blunt body wake using low and high frequency pulsed jets. *Int. J. Flow Control*, 6(1):61–76, 2014.
22. J-F. Beaudoin, O. Cadot, J-L. Aider, and J. E. Wesfreid. Three-dimensional stationary flow over a backwards-facing step. *Eur. J. Mech. B-Fluid*, 38:147–155, 2004.
23. N. Benard, J. Pons-Prats, J. Periaux, G. Bugeada, J. P. Bonnet, and E. Moreau. Multi-input genetic algorithm for experimental optimization of the reattachment downstream of a backwards-facing step with surface plasma actuator. In *46th AIAA Plasadynamics and Lasers Conference*, pages 1–23, Dallas, USA, 2015. AIAA Paper 2015-2957.
24. P. Benner, S. Gugercin, and K Willcox. A survey of projection-based model reduction methods for parametric dynamical systems. *SIAM Rev.*, 57(4):483–531, 2015.
25. E. Berger, M. Sastuba, D. Vogt, B. Jung, and H. B. Amor. Estimation of perturbations in robotic behavior using dynamic mode decomposition. *Journal of Advanced Robotics*, 29(5):331–343, 2015.
26. Z. P. Berger, M. G. Berry, P. R. Shea, B. R. Noack, S. Gogineni, and M. N. Glauser. Active flow control for high speed jets with large window PIV. *Flow, Turb., Combust.*, 94:97–123, 2014.
27. M. Bergmann, L. Cordier, and J.-P. Brancher. Optimal rotary control of the cylinder wake using proper orthogonal decomposition reduced order model. *Phys. Fluids*, 17:097101–1..21, 2005.
28. G. Berkooz, P. Holmes, and J.L. Lumley. The proper orthogonal decomposition in the analysis of turbulent flows. *Ann. Rev. Fluid Mech.*, 25:539–575, 1993.
29. T.R. Bewley and S. Liu. Optimal and robust control and estimation of linear paths to transition. *J. Fluid Mech.*, 365:305–349, 1998.
30. C. M. Bishop. *Pattern Recognition and Machine Learning*. Springer New York, 2006.
31. H. M. Blackburn and R. D. Henderson. A study of two-dimensional flow past an oscillating cylinder. *J. Fluid Mech.*, 385:255–286, 1999.
32. J. Bongard and H. Lipson. Automated reverse engineering of nonlinear dynamical systems. *Proc. Natl. Acad. Sci. USA*, 104(24):9943–9948, 2007.
33. L. Breiman. Random forests. *Machine Learning*, 45(1):5–32, 2001.
34. I. Bright, G. Lin, and J. N. Kutz. Compressive sensing and machine learning strategies for characterizing the flow around a cylinder with limited pressure measurements. *Phys. Fluids*, 25(12), 2013.
35. D. Bristow, M. Tharayil, and A. G. Alleyne. A survey of iterative learning control. *Control Syst. Mag.*, 3(26):96–114, 2006.
36. D. S. Broomhead and R. Jones. Time-series analysis. *Proc. Roy. Soc. Lond. A*, 423(1864):103–121, 1989.
37. D. S. Broomhead, R. Jones, and G. P. King. Topological dimension and local coordinates from time series data. *Journal of Physics A: Mathematical and General*, 20(9):L563, 1987.
38. D. S. Broomhead and G. P. King. Extracting qualitative dynamics from experimental data. *Phys. D*, 20(2-3):217–236, 1986.
39. B. W. Brunton, S. L. Brunton, J. L. Proctor, and J. N. Kutz. Optimal sensor placement and enhanced sparsity for classification. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, under review, see arXiv:1310.4217v1 [cs.CV], 2013.
40. B. W. Brunton, L. A. Johnson, J. G. Ojemann, and J. N. Kutz. Extracting spatial–temporal coherent patterns in large-scale neural recordings using dynamic mode decomposition. *Journal of Neuroscience Methods*, 258:1–15, 2016.

41. S. L. Brunton, B. W. Brunton, J. L. Proctor, and J. N. Kutz. Koopman observable subspaces and finite linear representations of nonlinear dynamical systems for control. *PLoS ONE*, 11(2):e0150171, 2016.
42. S. L. Brunton, X. Fu, and J. N. Kutz. Self-tuning fiber lasers. *IEEE Journal of Selected Topics in Quantum Electronics*, 20(5):464–471, 2014.
43. S. L. Brunton and B. R. Noack. Closed-loop turbulence control: Progress and challenges. *Appl. Mech. Rev.*, 67(5):050801:01–48, 2015.
44. S. L. Brunton, J. L. Proctor, and J. N. Kutz. Discovering governing equations from data: Sparse identification of nonlinear dynamical systems. *Proc. Natl. Acad. Sci. USA*, in print, 2016.
45. S. L. Brunton, J. L. Proctor, J. H. Tu, and J. N. Kutz. Compressive sampling and dynamic mode decomposition. *J. Comp. Dyn.*, in print, see arXiv:1312.5186, 2015.
46. S. L. Brunton, J. H. Tu, I. Bright, and J. N. Kutz. Compressive sensing and low-rank libraries for classification of bifurcation regimes in nonlinear dynamical systems. *SIAM Journal on Applied Dynamical Systems*, 13(4):1716–1732, 2014.
47. Marko Budišić and I. Mezić. Geometry of the ergodic quotient reveals coherent structures in flows. *Phys. D*, 241(15):1255–1269, 2012.
48. Statistisches Bundesamt. Straßenverkehrunfälle 1986 (transl: Road traffic accidents). Technical Report Fachserie 8, Reihe 7, Statistisches Bundesamt, 1987.
49. J. Burkardt, M.D. Gunzburger, and H.-C. Lee. Centroidal Voronoi Tessellation-Based Reduced-Order Modeling of Complex Systems. Technical report, Florida State University, 2004.
50. E. J. Candès. Compressive sensing. *Proceedings of the International Congress of Mathematics*, 2006.
51. E. J. Candès and T. Tao. Decoding by linear programming. *IEEE Transactions on Information Theory*, 51(12):4203–4215, 2005.
52. E. J. Candès and M. B. Wakin. An introduction to compressive sampling. *IEEE Signal Processing Magazine*, March:21–30, 2008.
53. J. Carberry, J. Sheridan, and D. Rockwell. Controlled oscillations of a cylinder: a new wake state. *J. Fluid Struct.*, 17(2):337–343, 2003.
54. L. Cattafesta and M. Shelpak. Actuators for active flow control. *Ann. Rev. Fluid Mech.*, 43:247–272, 2011.
55. L. Cattafesta, D. Williams, C. Rowley, and F. Alvi. Review of active control of flow-induced cavity resonance. In *33rd AIAA Fluid Dynamics Conference and Exhibit*, 2003. AIAA Paper 2003-3567.
56. L. N. Cattafesta III, D. Shukla, S. Garg, and J. A. Ross. Development of an adaptive weapons-bay suppression system. In *5th AIAA/CEAS Aeroacoustics Conference and Exhibit*, 1999. AIAA Paper 1999-1901.
57. L. N. Cattafesta III, Q. Song, D. R. Williams, C. W. Rowley, and F. S. Alvi. Active control of flow-induced cavity oscillations. *Progr. Aerosp. Sci.*, 44(7):479–502, 2008.
58. O. Cetiner and D. Rockwell. Streamwise oscillations of a cylinder in a steady current. Part 1: Locked-on states of vortex formation and loading. *J. Fluid Mech.*, 427:1–28, 2001.
59. A. Chadwick, K. Garry, and J. Howell. Transient aerodynamic characteristics of simple vehicle shapes by the measurement of surface pressures. Technical report, SAE Technical Paper, 2000.
60. S. Chaturantabut and D. C. Sorensen. Nonlinear model reduction via discrete empirical interpolation. *SIAM Journal on Scientific Computing*, 32(5):2737–2764, 2010.
61. B. Cheng and D. M. Titterton. Neural networks: A review from a statistical perspective. *Stat. Sci.*, 9:2–30, 1994.
62. N. J. Cherry, R. Hillier, and M. E. M. P. Latour. Unsteady measurements in a separated and reattaching flow. *J. Fluid Mech.*, 144:13–46, 7 1984.
63. M. Chevalier, J. Høpfner, E. Åkervik, and D.S. Henningson. Linear feedback control and estimation applied to instabilities in spatially developing boundary layers. *J. Fluid Mech.*, 588:163–187, 2007.

64. H. Choi, M. Hinze, and K. Kunisch. Instantaneous control of backward-facing step flows. *Appl. Numer. Math.*, 31:133–158, 1999.
65. H. Choi, W.-P. Jeon, and J. Kim. Control of flow over a bluff body. *Ann. Rev. Fluid Mech.*, 40:113–139, 2008.
66. H. Choi, P. Moin, and J. Kim. Active turbulence control for drag reduction in wall-bounded flows. *J. Fluid Mech.*, 262:75–110, 1994.
67. J. M. Chomaz. Global instabilities in spatially developing flows: non-normality and nonlinearity. *Ann. Rev. Fluid Mech.*, 37:357–393, 2005.
68. K.-B. Chun and H. J. Sung. Control of turbulent separated flow over a backward-facing step by local forcing. *Exp. Fluids*, 21(6):417–426, 1996.
69. D. Ciresan, U. Meier, and J. Schmidhuber. Multi-column deep neural networks for image classification. In *2012 IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, pages 3642–3649. IEEE, 2012.
70. K. R. Cooper. Truck aerodynamics reborn-lessons from the past. Technical report, SAE Technical Paper, 2003.
71. L. Cortelezzi, KH Lee, J Kim, and JL Speyer. Skin-friction drag reduction via robust reduced-order linear feedback control. *International Journal of Computational Fluid Dynamics*, 11(1-2):79–92, 1998.
72. L. Cortelezzi and J. L. Speyer. Robust reduced-order controller of laminar boundary layer transitions. *Phys. Rev. E*, 58(2):1906, 1998.
73. C. Cuvier, C. Braud, J. M. Foucaut, and M. Stanislas. Flow control over a ramp using active vortex generators. In *Proceedings of the 7th International Symposium on Turbulence and Shear Flow Phenomena (TSFP-7), Ottawa, Canada*, 2011.
74. C. Cuvier, J. M. Foucaut, C. Braud, and M. Stanislas. Characterisation of a high Reynolds number boundary layer subject to pressure gradient and separation. *J. Turb.*, 15(8):473–515, 2014.
75. J. Dandois, E. Garnier, and P. Sagaut. Numerical simulation of active separation control by a synthetic jet. *J. Fluid Mech.*, 574(1):25–58, 2007.
76. L. Davis. *Handbook of Genetic Algorithms*. Van Nostrand Reinhold Company, New York, 1991.
77. H. de Garis. Genetic Programming: Building artificial nervous systems using genetically programmed neural networks modules. In R. Porter and B. Mooney, editors, *Proceedings of the 7th International Conference on Machine Learning*, pages 132–139. Morgan Kaufmann, 1990.
78. J. Dean, G. Corrado, R. Monga, K. Chen, M. Devin, M. Mao, A. Senior, K. Tucker, P. and Yang, and Q. V. Le. Large scale distributed deep networks. In *Advances in Neural Information Processing Systems*, pages 1223–1231, 2012.
79. A. Debien, S. Aubrun, N. Mazellier, and A. Kourta. Salient and smooth edge ramps inducing turbulent boundary layer separation: Flow characterization for control perspective. *C. R. Mecanique*, 342(6-7):356–362, 2014.
80. A. Debien, K. A. F. F. von Krbek, N. Mazellier, T. Duriez, L. Cordier, B. R. Noack, M. W. Abel, and A. Kourta. Closed-loop separation control over a sharp-edge ramp using genetic programming. *Exp. Fluids*, 57(3):article 40, 2016.
81. S. C. R. Dennis, P. Nguyen, and S. Kocabiyik. The flow induced by a rotationally oscillating and translating circular cylinder. *J. Fluid Mech.*, 407:123–144, 2000.
82. N. Desbrosses. World energy expenditures. <http://www.leonardo-energy.org/blog/world-energy-expenditures>, 2011.
83. T. G. Dietterich. Ensemble methods in machine learning. In J. Kittler and F. Roli, editors, *Multiple Classifier Systems: Second International Workshop, MCS 2001 Cambridge, UK, July 2-4, 2001 Proceedings*, pages 1–15. Springer, Berlin Heidelberg, 2001.
84. D. L. Donoho. Compressed sensing. *IEEE Transactions on Information Theory*, 52(4):1289–1306, 2006.
85. A. P. Dowling and A. S. Morgans. Feedback control of combustion oscillations. *Ann. Rev. Fluid Mech.*, 37(151–182), 2005.

86. J. C. Doyle. Guaranteed margins for LQG regulators. *IEEE Transactions on Automatic Control*, 23(4):756–757, 1978.
87. J. C. Doyle, B. A. Francis, and A. R. Tannenbaum. *Feedback control theory*. Courier Corporation, 2013.
88. J. C. Doyle, K. Glover, P. P. Khargonekar, and B. A. Francis. State-space solutions to standard H_2 and H_∞ control problems. *IEEE Transactions on Automatic Control*, 34(8):831–847, 1989.
89. J. C. Doyle and G. Stein. Multivariable feedback design: concepts for a classical/modern synthesis. *IEEE Transactions on Automatic Control*, 26(1):4–16, 1981.
90. D. C. Dracopoulos. *Evolutionary Learning Algorithms for Neural Adaptive Control*. Perspectives in Neural Computing. Springer-Verlag, London, etc., 1997.
91. D. C. Dracopoulos and S. Kent. Genetic programming for prediction and control. *Neural Comput. & Appl.*, 6:214–228, 1997.
92. R. O. Duda, P. E. Hart, and D. G. Stork. *Pattern Classification*. Wiley-Interscience, 2000.
93. G. E. Dullerud and F. Paganini. *A Course in Robust Control Theory: A Convex Approach*. Texts in Applied Mathematics. Springer, Berlin, Heidelberg, 2000.
94. T. Duriez, S. L. Brunton, and B. R. Noack. OpenMLC, Matlab implementation of MLC. <http://github.com/MachineLearningControl/OpenMLC-Matlab>, 2016.
95. M. Efe, M. Debiassi, P. Yan, H. Özbay, and M. Samimy. Control of subsonic cavity flows by neural networks-analytical models and experimental validation. In *43rd AIAA Aerospace Sciences Meeting and Exhibit*, 2005. AIAA Paper 2005-0294.
96. M. El-Alti, V. Chernoray, P. Kjellgren, L. Hjelm, and L. Davidson. Computations and full-scale tests of active flow control applied on a VOLVO truck-trailer. In Dillmann, A. and A. Orellano, editors, *Aerodynamics of Heavy Vehicles III: Trucks, Buses and Trains*, volume 79 of *Lecture Notes in Applied and Computational Mechanics*. Springer-Verlag, 2016.
97. R. J. Englar. Advanced aerodynamic devices to improve the performance, economics, handling and safety of heavy vehicles. Technical report, SAE Technical Paper 2001-01-2072, 2001.
98. R. J. Englar. Pneumatic heavy vehicle aerodynamic drag reduction, safety enhancement, and performance improvement. In R. McCallen and F. Browand, editors, *The Aerodynamics of Heavy Vehicles: Trucks, Buses, and Trains*, pages 277–302. Springer, 2004.
99. N. B. Erichson, S. L. Brunton, and J. N. Kutz. Compressed dynamic mode decomposition for real-time object detection. Preprint arXiv:1512.04205, 2015.
100. R. Everson and L. Sirovich. Karhunen–Loeve procedure for gappy data. *Journal of the Optical Society of America A*, 12(8):1657–1664, 1995.
101. N. Fabbiane, O. Semeraro, S. Bagheri, and D. S. Henningson. Adaptive and model-based control theory applied to convectively unstable flows. *Appl. Mech. Rev.*, 66(6):060801–1..20, 2014.
102. Brian F Farrell and Petros J Ioannou. State estimation using a reduced-order Kalman filter. *Journal of the Atmospheric Sciences*, 58(23):3666–3680, 2001.
103. P. J. Fleming and R. C. Purshouse. Evolutionary algorithms in control systems engineering: a survey. *Control Engineering Practice*, 10(11):1223–1241, 2002.
104. J. B. Freund and M. G. Mungal. Drag and wake modification of axisymmetric bluff bodies using Coanda blowing. *J. Aircraft*, 31(3):572–578, 1994.
105. Y. Freund and R. E. Schapire. A decision-theoretic generalization of on-line learning and an application to boosting. *Journal of Computer and System Sciences*, 55(1):119–139, 1997.
106. U. Frisch. *Turbulence*. Cambridge University Press, Cambridge, 1st edition, 1995.
107. X. Fu, S. L. Brunton, and J. N. Kutz. Classification of birefringence in mode-locked fiber lasers using machine learning and sparse representation. *Optics Express*, 22(7):8585–8597, 2014.
108. M. Gad-el Hak. Flow control. *Appl. Mech. Rev.*, 42(10):261–293, 1989.
109. B.G. Galerkin. Rods and plates: series occurring in various questions regarding the elastic equilibrium of rods and plates (translated). *Vestn. Inzhen.*, 19:897–908, 1915.

110. S. Gaucel, M. Keijzer, E. Lutton, and A. Tonda. Learning dynamical systems using standard symbolic regression. In M. Nicolau, K. Krawiec, M.I. Heywood, M. Castelli, P. Garcia-Sánchez, J.J. Merelo, V.M. Rivas Santos, and K. Sim, editors, *Genetic Programming: 17th European Conference, EuroGP 2014, Granada, Spain, April 23-25, 2014, Revised Selected Papers*, pages 25–36. Springer Berlin Heidelberg, 2014.
111. N. Gautier. *Flow Control Using Optical Sensors*. PhD thesis, Ecole doctorale: Sciences Mécaniques, Acoustique, Électronique & Robotique (UPMC), ESPCI, Laboratoire PMMH, 2014.
112. N. Gautier and J.-L. Aider. Feed-forward control of a perturbed backward-facing step flow. *J. Fluid Mech.*, 759:181–196, 2014.
113. N. Gautier, J.-L. Aider, T. Duriez, B. R. Noack, M. Segond, and M. W. Abel. Closed-loop separation control using machine learning. *J. Fluid Mech.*, 770:424–441, 2015.
114. G. Gelbert, J. Moeck, C. O. Paschereit, and R. King. Feedback control of unstable thermoacoustic modes in an annular Rijke tube. *Control Engineering Practice*, 20:770–782, 2012.
115. J. Gerhard, M. Pastoor, R. King, B. R. Noack, A. Dillmann, M. Morzyński, and G. Tadmor. Model-based control of vortex shedding using low-dimensional Galerkin models. In *33rd AIAA Fluids Conference and Exhibit*, Orlando, FL, USA, 2003. Paper 2003-4262.
116. T. A. Ghee and G. Leishman. Drag reduction of motor vehicles by active flow control using the coanda effect. *AIAA Journal*, 20(2):289–299, 1992.
117. D. Giannakis and A. J. Majda. Nonlinear laplacian spectral analysis for time series with intermittency and low-frequency variability. *Proc. Natl. Acad. Sci. USA*, 109(7):2222–2227, 2012.
118. A. M. Gilhaus and V. E. Renn. Drag and driving-stability-related aerodynamic forces and their interdependence—results of measurements on 3/8-scale basic car shapes. Technical report, SAE Technical Paper 860211, 1986.
119. K. Glover and J. C. Doyle. State-space formulae for all stabilizing controllers that satisfy an h_∞ -norm bound and relations to risk sensitivity. *Systems & Control Letters*, 11:167–172, 1988.
120. G. Godard and M. Stanislas. Control of a decelerating boundary layer. Part 1: Optimization of passive vortex generators. *Aerosp. Sci. Technol.*, 10(3):181–191, 2006.
121. G. Godard and M. Stanislas. Control of a decelerating boundary layer. Part 3: Optimization of round jets vortex generators. *Aerosp. Sci. Technol.*, 10(6):455–464, 2006.
122. D. E. Goldberg. *Genetic Algorithms*. Pearson Education India, 2006.
123. D. Greenblatt and I. J. Wygnanski. The control of flow separation by periodic excitation. *Prog. Aero. Sci.*, 36(7):487–545, 2000.
124. J. Grosek and J. N. Kutz. *Dynamic Mode Decomposition for Real-Time Background/Foreground Separation in Video*. Preprint arXiv:1404.7592, 2014.
125. J. Guckenheimer and P. Holmes. *Nonlinear Oscillations, Dynamical Systems, and Bifurcation of Vector Fields*. Springer, New York, 1986.
126. E. Guilmineau, O. Chikhaoui, G. Deng, and M. Visonneau. Cross wind effects on a simplified car model by a DES approach. *Computers & Fluids*, 78:29–40, 2013.
127. D. P. Hart. High-speed PIV analysis using compressed image correlation. *Journal of Fluids Engineering*, 120:463–470, 1998.
128. M. A. Z. Hasan. The flow over a backward-facing step under controlled perturbation: laminar separation. *J. Fluid Mech.*, 238:73–96, 5 1992.
129. S. Haykin. *Neural Networks: A Comprehensive Foundation*. Prentice Hall, Upper Saddle River, New Jersey, 2004.
130. L. Henning and R. King. Robust multivariable closed-loop control of a turbulent backward-facing step flow. *J. Aircraft*, 44:201–208, 2007.
131. A. J. G. Hey, S. Tansley, and K. M. Tolle. The fourth paradigm: Data-intensive scientific discovery. Microsoft Research Redmond, WA, 2009.
132. G. Hinton, L. Deng, D. Yu, G. E. Dahl, A. Mohamed, N. Jaitly, A. Senior, V. Vanhoucke, P. Nguyen, and T. N. et al. Sainath. Deep neural networks for acoustic modeling in speech recognition: The shared views of four research groups. *IEEE Signal Processing Magazine*, 29(6):82–97, 2012.

133. B. L. Ho and R. E. Kalman. Effective construction of linear state-variable models from input/output data. In *Proceedings of the 3rd Annual Allerton Conference on Circuit and System Theory*, pages 449–459, 1965.
134. C.-M. Ho and P. Huerre. Perturbed free shear layers. *Annu. Rev. Fluid Mech.*, 16:365–422, 1984.
135. M. Högberg, T. R. Bewley, and D. S. Henningson. Linear feedback control and estimation of transition in plane channel flow. *J. Fluid Mech.*, 481:149–175, 2003.
136. M. Högberg and D. S. Henningson. Linear optimal control applied to instabilities in spatially developing boundary layers. *J. Fluid Mech.*, 470:151–179, 2002.
137. J. H. Holland. *Adaptation in Natural and Artificial Systems: An Introductory Analysis with Applications to Biology, Control, and Artificial Intelligence*. University of Michigan Press, Ann Arbor, MI, USA, 1975.
138. P. Holmes, J. L. Lumley, G. Berkooz, and C. W. Rowley. *Turbulence, Coherent Structures, Dynamical Systems and Symmetry*. Cambridge University Press, Cambridge, 2nd paperback edition, 2012.
139. J. P. Howell. Shape features which influence crosswind sensitivity. Technical report, The Institution of Mechanical Engineers, IMechE 1993-9, Vehicle Ride and Handling, 1993.
140. W.-H. Hucho. *Aerodynamics of Road Vehicles*. Society of Automotive Engineers, 1998.
141. L. Hung, M. Parviz, and J. Kim. Direct numerical simulation of turbulent flow over a backward-facing step. *J. Fluid Mech.*, 330:349–374, 1997.
142. M. Ilak and C. W. Rowley. Modeling of transitional channel flow using balanced proper orthogonal decomposition. *Phys. Fluids*, 20:034103, 2008.
143. S. J. Illingworth, A. S. Morgans, and C. W. Rowley. Feedback control of flow resonances using balanced reduced-order models. *Journal of Sound and Vibration*, 330(8):1567–1581, 2010.
144. S. J. Illingworth, A. S. Morgans, and C. W. Rowley. Feedback control of cavity flow oscillations using simple linear models. *J. Fluid Mech.*, 709:223–248, 2012.
145. M. Islam, F. Decker, E. De Villiers, A. Jackson, J. Gines, T. Grahs, A. Gitt-Gehrke, and J. Comas i Font. Application of Detached-Eddy Simulation for automotive aerodynamics development. Technical report, SAE Technical Paper 2009-01-0333, 2009.
146. G. James, D. Witten, T. Hastie, and R. Tibshirani. *An Introduction to Statistical Learning*. Springer, 2013.
147. W. B. Johnson and J. Lindenstrauss. Extensions of Lipschitz mappings into a Hilbert space. *Contemporary Mathematics*, 26(189-206):1, 1984.
148. D.W. Jordan and P. Smith. *Nonlinear Ordinary Differential Equations*. Clarendon Press, Oxford, 1988.
149. P. Joseph, X. Amandolese, C. Edouard, and J.-L. Aider. Flow control using MEMS pulsed micro-jets on the ahmed body. *Exp. Fluids*, 54(1):1–12, 2013.
150. J. N. Juang. *Applied System Identification*. Prentice Hall PTR, Upper Saddle River, New Jersey, 1994.
151. J. N. Juang and R. S. Pappa. An eigensystem realization algorithm for modal parameter identification and model reduction. *Journal of Guidance, Control, and Dynamics*, 8(5):620–627, 1985.
152. J. N. Juang, M. Phan, L. G. Horta, and R. W. Longman. Identification of observer/Kalman filter Markov parameters: Theory and experiments. Technical Memorandum 104069, NASA, 1991.
153. W. J. Jung, N. Mangiavacchi, and R. Akhavan. Suppression of turbulence in wall-bounded flows by high-frequency spanwise oscillations. *Phys. Fluids A*, 4:1605–1607, 1992.
154. E. Kaiser, B. R. Noack, L. Cordier, A. Spohn, M. Segond, M. W. Abel, G. Daviller, J. Östh, S. Krajnović, and R. K. Niven. Cluster-based reduced-order modelling of a mixing layer. *J. Fluid Mech.*, 754:365–414, 2014.
155. E. Kaiser, B. R. Noack, A. Spohn, L. N. Cattafesta, and M. Morzyński. Cluster-based control of nonlinear dynamics. *Theor. Comput. Fluid Dyn.*, under review, see arXiv:1602.05416, 2016.

156. R. E. Kalman. A new approach to linear filtering and prediction problems. *Journal of Fluids Engineering*, 82(1):35–45, 1960.
157. J. Karhunen and J. Joutsensalo. Representation and separation of signals using nonlinear PCA type learning. *Neural Networks*, 7(1):113–127, 1994.
158. W. Kerstens, J. Pfeiffer, D. Williams, R. King, and T. Colonius. Closed-loop control of lift for longitudinal gust suppression at low Reynolds numbers. *AIAA Journal*, 49(8):1721–1728, 2011.
159. J. Kim. Control of turbulent boundary layers. *Phys. Fluids*, 15(5):1093–1105, 2003.
160. J. Kim. Physics and control of wall turbulence for drag reduction. *Phil. Trans. R. Soc. A*, 369(1940):1396–1411, 2011.
161. J. Kim and T.R. Bewley. A linear systems approach to flow control. *Ann. Rev. Fluid Mech.*, 39:383–417, 2007.
162. B. O. Koopman. Hamiltonian systems and transformation in Hilbert space. *Proc. Natl. Acad. Sci. USA*, 17(5):315–318, 1931.
163. B. O. Koopman and J. v. Neumann. Dynamical systems of continuous spectra. *Proc. Natl. Acad. Sci. USA*, 18(3):255, 1932.
164. J. R. Koza. *Genetic Programming: On the Programming of Computers by Means of Natural Selection*, volume 1. MIT Press, 1992.
165. J. R. Koza, F. H. Bennett, M. A. Andre, M. A. Keane, and F. Dunlap. Automatic synthesis of analog circuits by means of genetic programming. *IEEE Transactions on Evolutionary Computation*, 1(2):109–128, 1997.
166. J. R. Koza, F. H. Bennett III, and O. Stiffelman. Genetic programming as a Darwinian invention machine. In *Genetic Programming: Second European Workshop, EuroGP'99 Göteborg, Sweden, May 26-27, 1999, Proceedings*, pages 93–108. Springer, 1999.
167. N. Kryloff and N. Bogoliubov. *Introduction to Non-Linear Mechanics*. Princeton University Press, Princeton, 3rd printing edition, 1952.
168. J. N. Kutz. *Data-Driven Modeling & Scientific Computation: Methods for Complex Systems & Big Data*. Oxford University Press, 2013.
169. O. A. Ladyzhenskaya. *The Mathematical Theory of Viscous Incompressible Flow*. Gordon and Breach, New York, London, 1st edition, 1963.
170. Y. Lan and I. Mezić. Linearization in the large of nonlinear systems and koopman operator spectrum. *Phys. D*, 242(1):42–53, 2013.
171. C. Lee, J. Kim, D. Babcock, and R. Goodman. Application of neural networks to turbulence control for drag reduction. *Phys. Fluids*, 9(6):1740–1747, 1997.
172. H. W. Liepmann, G. L. Brown, and D. M. Nosenchuck. Control of laminar instability waves using a new technique. *J. Fluid Mech.*, 118:187–200, 1982.
173. J. C. Lin. Review of research on low-profile vortex generators to control boundary-layer separation. *Prog. Aero. Sci.*, 38(4):389–420, 2002.
174. L. Ljung. *System Identification: Theory for the User*. Prentice Hall, 1999.
175. K. R. Low, Z. P. Berger, S. Kostka, B. El Hadidi, S. Gogineni, and M. N. Glauser. Noise source identification and control in a Mach 0.6 turbulent jet with simultaneous time resolved PIV, pressure and acoustic measurements. *Exp. Fluids*, 54(4):1–17, 2013.
176. D. M. Luchtenburg, B. Günter, B. R. Noack, R. King, and G. Tadmor. A generalized mean-field model of the natural and actuated flows around a high-lift configuration. *J. Fluid Mech.*, 623:283–316, 2009.
177. D. M. Luchtenburg and C. W. Rowley. Model reduction using snapshot-based realizations. *Bulletin of the American Physical Society*, 56, 2011.
178. D. M. Luchtenburg, M. Schlegel, B. R. Noack, K. Aleksić, R. King, G. Tadmor, and B. Günther. Turbulence control based on reduced-order models and nonlinear control design. In R. King, editor, *Active Flow Control II*, volume 108 of *Notes on Numerical Fluid Mechanics and Multidisciplinary Design*, pages 341–356, Berlin, 26-28 May 2010, 2010. Springer-Verlag.
179. J.L. Lumley and P.N. Blossey. Control of turbulence. *Ann. Rev. Fluid Mech.*, 30:311–327, 1998.

180. D. L. Ly and H. Lipson. Learning symbolic representations of hybrid dynamical systems. *J. Mach. Learn. Res.*, 13:3585–3618, 2012.
181. Z. Ma, S. Ahuja, and C. W. Rowley. Reduced order models for control of fluids using the eigensystem realization algorithm. *Theor. Comput. Fluid Dyn.*, 25(1):233–247, 2011.
182. D. G. Mabey. Analysis and correlation of data on pressure fluctuations in separated flow. *J. Aircraft*, 9(9):642–645, 1972.
183. L. Mathelin, 2015. Private communication.
184. R. C. McCallen, K. Salari, J. M. Ortega, L. J. DeChant, B. Hassan, C. J. Roy, W. D. Pointer, F. Browand, M. Hammache, T. Y. Hsu, et al. DOE’s effort to reduce truck aerodynamic drag – joint experiments and computations lead to smart design. In *AIAA Paper, 2014-2249*, 2004.
185. T. McConaghy. FFX: Fast, scalable, deterministic symbolic regression technology. In R. Riolo and E. Vladislavleva, editors, *Genetic Programming Theory and Practice IX (Genetic and Evolutionary Computation)*, pages 235–260. Springer, 2011.
186. T. T. Medjo, R. Temam, and M. Ziane. Optimal and robust control of fluid flows: Some theoretical and computational aspects. *Appl. Mech. Rev.*, 61(1):010801, 2008.
187. I. Mezić. Spectral properties of dynamical systems, model reduction and decompositions. *Nonlinear Dynamics*, 41(1-3):309–325, 2005.
188. I. Mezić. Analysis of fluid flows via spectral properties of the Koopman operator. *Ann. Rev. Fluid Mech.*, 45:357–378, 2013.
189. M. Milano and P. Koumoutsakos. Neural network modeling for near wall turbulent flow. *J. Comp. Phys.*, 182(1):1–26, 2002.
190. T. M. Mitchell. *Machine Learning*. McGraw Hill, 1997.
191. R. Mittal, R. Kotapati, and L. Cattafesta. Numerical study of resonant interactions and flow control in a canonical separated flow. In *AIAA 43rd Aerospace Sciences Meeting and Exhibit*, Reno, NV, USA, 2005. AIAA Paper 2005-1261.
192. B. C. Moore. Principal component analysis in linear systems: Controllability, observability, and model reduction. *IEEE Transactions on Automatic Control*, AC-26(1):17–32, 1981.
193. S. D. Müller, M. Milano, and P. Koumoutsakos. Application of machine learning algorithms to flow modeling and optimization. In *Annual Research Briefs*, pages 169–178, Center for Turbulence Research, University of Stanford, 1999.
194. K. P. Murphy. *Machine Learning: A Probabilistic Perspective*. MIT Press, 2012.
195. A. G. Nair and K. Taira. Network-theoretic approach to sparsified discrete vortex dynamics. *J. Fluid Mech.*, 768:549–571, 2015.
196. B. R. Noack, K. Afanasiev, M. Morzyński, G. Tadmor, and F. Thiele. A hierarchy of low-dimensional models for the transient and post-transient cylinder wake. *J. Fluid Mech.*, 497:335–363, 2003.
197. B. R. Noack, M. Morzyński, and G. Tadmor. *Reduced-Order Modelling for Flow Control*. Number 528 in CISM Courses and Lectures. Springer-Verlag, Vienna, 2011.
198. B. R. Noack and R. K. Niven. Maximum-entropy closure for a Galerkin system of an incompressible periodic wake. *J. Fluid Mech.*, 700:187–213, 2012.
199. B. R. Noack, M. Schlegel, B. Ahlborn, G. Mutschke, M. Morzyński, P. Comte, and G. Tadmor. A finite-time thermodynamics of unsteady fluid flows. *J. Non-Equilib. Thermodyn.*, 33:103–148, 2008.
200. H. Nyquist. Certain topics in telegraph transmission theory. *Transactions of the A. I. E. E.*, pages 617–644, FEB 1928.
201. K. Oberleithner, 2014. Private communication.
202. Council of European Union. Regulation (ec) no 715/2007 of the european parliament and of the council of 20 june 2007 on type approval of motor vehicles with respect to emissions from light passenger and commercial vehicles (euro 5 and euro 6) and on access to vehicle repair and maintenance information, 2007.
203. E. Oja. Principal components, minor components, and linear neural networks. *Neural Networks*, 5(6):927–935, 1992.
204. E. Oja. The nonlinear PCA learning rule in independent component analysis. *Neurocomputing*, 17(1):25–45, 1997.

205. J. Östh, S. Krajnović, B. R. Noack, D. Barros, and J. Borée. On the need for a nonlinear subscale turbulence term in pod models as exemplified for a high Reynolds number flow over an ahmed body. *J. Fluid Mech.*, 747:518–544, 2014.
206. V. Parezanovic, J. C. Laurentie, T. Duriez, C. Fourment, J. Delville, J.-P. Bonnet, L. Cordier, B. R. Noack, M. Segond, M. Abel, T. Shaqarin, and S. Brunton. Mixing layer manipulation experiment – from periodic forcing to machine learning closed-loop control. *Flow Turb. Comb.*, 91(1):155–173, 2015.
207. H. Park, J.-H. Cho, J. Lee, D.-H. Lee, and K.-H. Kim. Aerodynamic drag reduction of ahmed model using synthetic jet array. Technical report, SAE Technical Paper, 2013.
208. M. Pastoor. *Niederdimensionale Wirbelmodelle zur Kontrolle von Scher- und Nachlaufströmungen*. PhD thesis, Berlin Institute of Technology, Germany, 2008.
209. M. Pastoor, L. Henning, B. R. Noack, R. King, and G. Tadmor. Feedback shear layer control for bluff body drag reduction. *J. Fluid Mech.*, 608:161–196, 2008.
210. B. Peherstorfer, D. Butnaru, K. Willcox, and H.-J. Bungartz. Localized discrete empirical interpolation method. *SIAM Journal on Scientific Computing*, 36(1):A168–A192, 2014.
211. J. Pfeiffer and R. King. Multivariable closed-loop flow control of drag and yaw moment for a 3D bluff body. In *6th AIAA Flow Control Conference*, pages 1–14, Atlanta, USA, 2012.
212. J. Pfeiffer and R. King. Linear parameter varying active flow control for a 3d bluff body exposed to cross-wind gusts. In *32nd AIAA Applied Aerodynamics Conference, AIAA Aviation*, pages 1–15, 2014. AIAA-Paper 2014-2406.
213. M. Phan, L. G. Horta, J. N. Juang, and R. W. Longman. Linear system identification via an asymptotically stable observer. *Journal of Optimization Theory and Applications*, 79:59–86, 1993.
214. J. T. Pinier, J. M. Ausseur, M. N. Glauser, and H. Higuchi. Proportional closed-loop feedback control of flow separation. *AIAA Journal*, 45(1):181–190, 2007.
215. J. L. Proctor, S. L. Brunton, B. W. Brunton, and J. N. Kutz. Sparsity in complex systems. *European Physical Journal*, 2014.
216. J. L. Proctor, S. L. Brunton, and J. N. Kutz. Dynamic mode decomposition with control. *SIAM Journal on Applied Dynamical Systems*, 15(1):142–161, 2016.
217. J. L. Proctor and P. A. Eckhoff. Discovering dynamic patterns from infectious disease data using dynamic mode decomposition. *International Health*, 2(7):139–145, 2015.
218. B. Protas. Linear feedback stabilization of laminar vortex shedding based on a point vortex model. *Phys. Fluids*, 16(12):4473–4488, 2004.
219. M. Quade, M. Abel, N. Shafi, R. K. Niven, and B. R. Noack. Prediction of dynamical systems by symbolic regression. *Phys. Rev. E.*, in revision, see arXiv:1602.04648 [physics.data-an], 2016.
220. A. Quarteroni and G. Rozza. *Reduced Order Methods for Modeling and Computational Reduction*, volume 9 of *MS&A – Modeling, Simulation & Applications*. Springer, 2013.
221. J. R. Quinlan. Induction of decision trees. *Machine Learning*, 1(1):81–106, 1986.
222. K. J. Åström and R. M. Murray. *Feedback Systems: An Introduction for Scientists and Engineers*. Princeton University Press, Princeton, 2010.
223. I. Rechenberg. *Evolutionsstrategie: Optimierung technischer Systeme nach Prinzipien der biologischen Evolution*. Frommann-Holzboog, Stuttgart, 1973.
224. D. Rempfer. On boundary conditions for incompressible Navier-Stokes problems. *Appl. Mech. Rev.*, 59(3):107–125, 2006.
225. M. Rouméas, P. Gilliéron, and A. Kourta. Drag reduction by flow separation control on a car after body. *Intl. J. Num. Meth. Fluids*, 60(11):1222–1240, 2009.
226. K. Roussopoulos. Feedback control of vortex shedding at low Reynolds numbers. *J. Fluid Mech.*, 248:267–296, 1993.
227. C. W. Rowley. *Modeling, simulation, and control of cavity flow oscillations*. PhD thesis, California Institute of Technology, 2002.
228. C. W. Rowley, I. Mezić, S. Bagheri, P. Schlatter, and D.S. Henningson. Spectral analysis of nonlinear flows. *J. Fluid Mech.*, 645:115–127, 2009.
229. C. W. Rowley, D. R. Williams, T. Colonius, R. M. Murray, and D. G. MacMynowski. Linear models for control of cavity flow oscillations. *J. Fluid Mech.*, 547:317–330, 2006.

230. C.W. Rowley. Model reduction for fluids using balanced proper orthogonal decomposition. *Int. J. Bifurcation and Chaos*, 15(3):997–1013, 2005.
231. C.W. Rowley and D.R. Williams. Dynamics and control of high-Reynolds number flows over open cavities. *Ann. Rev. Fluid Mech.*, 38:251–276, 2006.
232. W. J. Rugh and J. S. Shamma. Research on gain scheduling. *Automatica*, 36(10):1401–1425, 2000.
233. M. Samimy, M. Debiasi, E. Caraballo, J. Malone, J. Little, H. Özbay, M.Ö. Efe, X. Yan, X. Yuan, J. DeBonis, J.H. Myatt, and R.C. Camphouse. Strategies for closed-loop cavity flow control. In *42nd Aerospace Sciences Meeting and Exhibit*, Reno, NV, USA, 2004. AIAA Paper 2004-0576.
234. M. Samimy, M. Debiasi, E. Caraballo, A. Serrani, X. Yuan, and J. Little. Reduced-order model-based feedback control of subsonic cavity flows - an experimental approach. In R. King, editor, *Active Flow Control*, volume 25 of *Notes on Numerical Fluid Mechanics and Multidisciplinary Design (NNFM)*, pages 211–230, Berlin, 2007. Springer.
235. M. Samimy, J.-H. Kim, J. Kastner, I. Adamovic, and Y. Utkin. Active control of high-speed and high-Reynolds-number jets using plasma actuators. *J. Fluid Mech.*, 578:305–330, 2007.
236. R. E. Schapire. The boosting approach to machine learning: An overview. In *Nonlinear Estimation and Classification*, pages 149–171. Springer, 2003.
237. P. J. Schmid. Dynamic mode decomposition for numerical and experimental data. *J. Fluid Mech.*, 656:5–28, 2010.
238. P. J. Schmid and L. Brandt. Analysis of fluid systems: stability, receptivity, sensitivity. *Appl. Mech. Rev.*, 2014.
239. M. Schmidt and H. Lipson. Distilling free-form natural laws from experimental data. *Science*, 324(5923):81–85, 2009.
240. T. M. Schneider, B. Eckhardt, and J. Vollmer. Statistical analysis of coherent structures in transitional pipe flow. *Phys. Rev. E*, 75:66–313, 2007.
241. B. Schölkopf and A. J. Smola. *Learning with Kernels: Support Vector Machines, Regularization, Optimization, and Beyond*. The MIT Press, Boston, 2002.
242. H.-P. Schwefel. Kybernetische Evolution als Strategie der experimentellen Forschung in der Strömungstechnik. Master's thesis, Hermann-Föttinger-Institut für Strömungstechnik, Technische Universität Berlin, Germany, 1965. Diplom thesis.
243. A. Seifert and L. G. Pack. Effects of sweep on active separation control at high Reynolds numbers. *J. Aircraft*, 40(1):120–126, 2003.
244. O. Semeraro, S. Bagheri, L. Brandt, and D. S. Henningson. Feedback control of three-dimensional optimal disturbances using reduced-order models. *J. Fluid Mech.*, 677:63–102, 2011.
245. O. Semeraro, S. Bagheri, L. Brandt, and D. S. Henningson. Transition delay in a boundary layer flow using active control. *J. Fluid Mech.*, 731:288–311, 2013.
246. Jeff S Shamma and Michael Athans. Guaranteed properties of gain scheduled control for linear parameter-varying plants. *Automatica*, 27(3):559–564, 1991.
247. C. E. Shannon. A mathematical theory of communication. *Bell System Technical Journal*, 27(3):379–423, 1948.
248. T. Shaqarin, C. Braud, S. Coudert, and M. Stanislas. Open and closed-loop experiments to identify the separated flow dynamics of a thick turbulent boundary layer. *Exp. Fluids*, 54(2):1–22, 2013.
249. R. L. Simpson. Turbulent boundary-layer separation. *Annu. Rev. Fluid Mech.*, 21:205–232, 1989.
250. D. Sipp, O. Marquet, P. Meliga, and A. Barbagallo. Dynamics and control of global instabilities in open-flows: a linearized approach. *Appl. Rev. Mech.*, 63:251–276, 2010.
251. S. Skogestad and I. Postlethwaite. *Multivariable Feedback Control: Analysis and Design*. John Wiley & Sons, Inc., Hoboken, New Jersey, 2 edition, 2005.
252. A. J Smola and B. Schölkopf. A tutorial on support vector regression. *Statistics and Computing*, 14(3):199–222, 2004.
253. P. G. Spazzini, G. Iuso, M. Onorato, N. Zurlo, and G. M. Di Cicca. Unsteady behavior of back-facing step flow. *Exp. Fluids*, 30(5):551–561, 2001.

254. R. F. Stengel. *Optimal Control and Estimation*. Courier Corporation, 2012.
255. B. Strom, S. L. Brunton, and B. Polagye. Intracycle angular velocity control of cross-flow turbines. Preprint.
256. J. T. Stuart. Nonlinear stability theory. *Ann. Rev. Fluid Mech.*, 3:347–370, 1971.
257. R. S. Sutton and A. G. Barto. *Reinforcement Learning: An Introduction*. MIT Press, Cambridge, 1998.
258. J. A. K. Suykens and J. Vandewalle. Least squares support vector machine classifiers. *Neural Processing Letters*, 9(3):293–300, 1999.
259. F. Takens. Detecting strange attractors in turbulence. *Lecture Notes in Mathematics*, 898:366–381, 1981.
260. J. A Taylor and M. N. Glauser. Towards practical flow sensing and control via POD and LSE based low-dimensional methods. *ASME J. Fluids Engrng*, 126:337–345, 2004.
261. H. Tennekes and J. Lumley. *A First Course in Turbulence*. MIT Press, 1972.
262. V. Theofilis. Global linear instability. *Ann. Rev. Fluid Mech.*, 43:319–352, 2011.
263. B. Thiria, S. Goujon-Durand, and J. E. Wesfreid. The wake of a cylinder performing rotary oscillations. *J. Fluid Mech.*, 560:123–147, 2006.
264. V. Thirunavukkarasu, H. A. Carlson, R. D. Wallace, P. R. Shea, and M. N. Glauser. Model-based feedback flow control development and simulation for a pitching turret. *AIAA Journal*, 50(9):1834–1842, 2012.
265. R. Tibshirani. Regression shrinkage and selection via the Lasso. *J. R. Statist. Soc. B*, 58(1):267–288, 1996.
266. J. A. Tropp and A. C. Gilbert. Signal recovery from random measurements via orthogonal matching pursuit. *IEEE Transactions on Information Theory*, 53(12):4655–4666, 2007.
267. M. Tsubokura, T. Kobayashi, T. Nakashima, T. Nouzawa, T. Nakamura, H. Zhang, K. Onishi, and N. Oshima. Computational visualization of unsteady flow around vehicles using high performance computing. *Computers & Fluids*, 38(5):981–990, 2009.
268. J. H. Tu and C. W. Rowley. An improved algorithm for balanced POD through an analytic treatment of impulse response tails. *J. Comp. Phys.*, 231(16):5317–5333, 2012.
269. J. H. Tu, C. W. Rowley, D. M. Luchtenburg, S. L. Brunton, and J. N. Kutz. On dynamic mode decomposition: theory and applications. *J. Comp. Dyn.*, 1(2):391–421, 2014.
270. A. Visioli. Tuning of PID controllers with fuzzy logic. In *Control Theory and Applications, IEEE Proceedings-*, volume 148, pages 1–8, 2001.
271. B. Vukasonovic, Z. Rusak, and A. Glezer. Dissipative small-scale actuation of a turbulent shear layer. *J. Fluid Mech.*, 656:51–81, 2010.
272. M. Wahde. *Biologically Inspired Optimization Methods: An Introduction*. WIT Press, 2008.
273. R. D. Wallace, P. R. Shea, M. N. Glauser, V. Thirunavukkarasu, and H. A. Carlson. Simulation-guided, model-based feedback flow control for a pitching turret. *AIAA Journal*, 50(8):1685–1696, 2012.
274. W. X. Wang, R. Yang, Y. C. Lai, V. Kovanis, and C. Grebogi. Predicting catastrophes in nonlinear dynamical systems by compressive sensing. *Phys. Rev. Lett.*, 106:154101–1–154101–4, 2011.
275. N. Wiener. *Cybernetics or Control and Communication in the Animal and the Machine*. MIT Press, Boston, 1st edition, 1948.
276. K. Willcox and J. Peraire. Balanced model reduction via the proper orthogonal decomposition. *AIAA Journal*, 40(11):2323–2330, 2002.
277. C. E. Willert and M. Gharib. Digital particle image velocimetry. *Exp. Fluids*, 10(4):181–193, 1991.
278. J. Wright, A. Yang, A. Ganesh, S. Sastry, and Y. Ma. Robust face recognition via sparse representation. *IEEE Transactions on Pattern Analysis and Machine Intelligence (PAMI)*, 31(2):210–227, 2009.
279. X. Wu, V. Kumar, J. R. Quinlan, J. Ghosh, Q. Yang, H. Motoda, G. J. McLachlan, A. Ng, B. Liu, and S. Y. et al. Philip. Top 10 algorithms in data mining. *Knowledge and Information Systems*, 14(1):1–37, 2008.
280. K. B. M. Q. Zaman and A. K. M. F. Hussain. Turbulence suppression in free shear flows by controlled excitation. *J. Fluid Mech.*, 103:133–159, 2 1981.

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