Exercise 1-1 Compute the derivative of the following functions

- (a) $f(x) = \sin(x^3)$
- (b) $f(x) = e^{x^2} \sin(x)$

Exercise 1-2 Solve the following linear differential equation by hand:

$$\dot{x} = \lambda x, \quad x(0) = 1$$

Plot the solution for t = 0 to t = 5 for $\lambda = -2, -1, 0, 0.1, 0.2$. Please plot these all on the same figure using the hold on command in Matlab. Label your axes (>> doc xlabel, >> doc ylabel) and include a legend (e.g., legend('lambda 1', 'lambda 2', 'lambda 3', ...)).

Exercise 1-3 Compute the Taylor series expansion for $f(x) = x \sin(x)$ by hand.

Plot the function f(x) and the three term expansion (i.e., the first three nonzero terms) from x = -5 to x = 5.

Exercise 1-4 Write down the solution to the following differential equation (by hand):

 $\ddot{x} - \lambda x = 0,$

for an arbitrary initial position x(0) and zero velocity $\dot{x}(0)$. What does the solution look like for $\lambda > 0$? How about for $\lambda < 0$? Please sketch solutions.

Exercise 1-5 Please solve the following differential equation (by hand):

$$\ddot{x} + \dot{x} - 2x = 0$$

with the following initial conditions:

$$\begin{aligned} x(0) &= 2\\ \dot{x}(0) &= -1 \end{aligned}$$

What is the long-time behavior of this system?