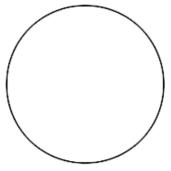
Show all your work. Reasonable supporting work must be shown to earn credit.

- 1. [10] Let A, B, C, and D be points with coordinates a, b, c, and d respectively. Determine if the following make sense/could be true and be sure to justify your answer:
 - (a) A = a
 - (b) A = B
 - (c) A < B
 - (d) $A \in \overline{CD}$
 - (e) $AB \in \overline{CD}$
- 2. Consider: $\forall n \in \mathbb{R}, \frac{d}{dx}x^n = n \cdot x^{n-1}$.
 - (a) [2] (ProofsActivity #3) Use as few symbols as possible to interpret the meaning with words.
 - (b) [2] (HW1 #1.13) Negate the above statement symbolically without using the \forall symbol.
- 3. [2] (Complete this question last!!) What concept did you study well and not see on the exam?

Definition 1. If A and B are arbitrary points with coordinates a and B respectively, then the distance AB from A to B is defined as:

$$AB = \begin{cases} |a-b| & \text{if } |a-b| \le \lambda \\ 2\lambda - |a-b| & \text{if } |a-b| > \lambda \end{cases}$$

- 4. Consider the circle with circumference 2π so we let $\lambda = \pi$ in the distance defined above.
 - (a) [2] (Practice3.1) Find the distance between the points with coordinates $\frac{\pi}{4}$ and $\frac{9\pi}{4}$.



- (b) [3] (1dFolding Activity #5) Recall on the line that B is between A and C if AB + BC = AC. Let us define between similarly on the circle. Identify three points on the circle such that no point is between the others.
- 5. (Activity 4.5) A Möbius strip can be considered as a vertically infinity strip of paper with left and right sides glued together via a half-twist.
 - (a) [4] There are several possible "lines" that might be defined on this space. Describe (and consider sketching!) at least three significantly different shaped "lines". (Recall that a similar exercise was done on an infinitely long cylinder in class.)

- (b) [3] Identify which of the kinds of "lines" you found above satisfy Postulate 3. (Every line l determines a decompositions of the plane into 3 distinct sets: H_0 , H_1 , and l where:
 - Every pair of points in one of the H_i are on the same side of l, and
 - Every pair of points where one is in H_0 and the other is in H_1 are on opposite sides of l.)

6. [5] (2Dintro Activity) Critique the following theorem and proof.

Theorem 1. Two distinct lines can intersect in at most one point

Proof. Pick distinct points A, B, and C. Then Postulate 1 implies that both \overrightarrow{AB} and \overrightarrow{AC} determine unique lines, and then intersect in point A, so there is one point of intersection.

7. [8] (HW2 #2.29/2.7) Prove the following: Let A and B be points with coordinates a and b respectively, and let ϕ be the fold with crease B. Then the coordinate of $\phi(A)$ is 2b-a.

Postulate Origametry 1. Any two points determine a unique line.

Postulate Origametry 2. Given any two distinct points on a line, there is a one-to-one correspondence, called a ruler between all points on the line with the real numbers that sends one of the two given points to 0, and the other to some number greater than 0. The number p assigned to a point P by the ruler is called the coordinate.

Postulate Euclid 1. We can draw a unique line from any point to any point.

Postulate Euclid 2. We can increase a finite line continuously into a line.

8. [9] The first two postulates for 2 dimensions from our textbook are above along with the first two postulates created by Euclid about 2219 years ago to describe geometry. Recall that postulates are "common notions" which "everyone" agrees must be true and so can be assumed and used to build theorems. Generally this question is asking you to compare and contrast these different postulates chosen by the author of our text and Euclid. Does one set imply the other and/or vice versa? Does one set seem superior to you than the other and if so explain why. (You do not have to prove anything formally in this exercise, but you do have to provide compelling evidence.)