§1.5 WrittenHW #2 TCSS 321

- 1. [3] Let F(x, y) mean that "x can fool y", where the domain consists of all people in the world. Use quantifiers to express each of these statements.
 - (a) Everybody can fool Sammy.
 - (b) Everyone can be fooled by somebody.
- 2. [2] Use predicates, quantifiers, logical connectives, and mathematical operators to express the statement that there is a positive integer that is not the sum of three eel numbers squared.
- 3. [2] Determine the truth value of each of these statements if the domain of each variable consists of all real numbers.
 - (a) $\forall x \exists y (x^2 = y)$
 - (b) $\forall x \exists y (x = y^2)$
- 4. [3] Rewrite each of these statements so that negations appear only within predicates (that is, so that no negation is outside a quantifier or an expression involving logical connectives).
 - (a) $\neg \exists y \exists x P(x, y)$
 - (b) $\neg \exists y (Q(y) \land \forall x \neg R(x, y))$
 - (c) $\neg \exists y (\forall x \exists z T(x, y, z) \lor \exists x \forall z U(x, y, z))$

$\$_{1.6}$ WrittenHW #2 TCSS 321

- 1. [3] For the following set of premises, what relevant conclusion or conclusions can be drawn? Explain yourself using the formal rules of inference.
 - (a) "All foods that are healthy to eat do not taste good."
 - (b) "Tofu is healthy to eat."
 - (c) "You only eat what tastes good."
 - (d) "Cheeseburgers are not healthy to eat."
- 2. [4] For each of the arguments below, determine whether the arguments is correct or incorrect. Explain why.
 - (a) All students in Discrete 1 understand logic. Peter is a student in this class. Therefore, Peter understands logic.
 - (b) Every computer science major takes Discrete 1. Xavier is taking Discrete 1. Therefore, Xavier is a computer science major.
- 3. [3] Identify the error or errors in this argument that supposedly shows that: if $\forall x(P(x) \lor R(x))$ is true, then $\forall xP(x) \lor \forall xR(x)$ is true.

1. $\forall x(P(x) \lor R(x))$	Premise
2. $P(c) \lor R(c)$	Universal instantiation form (1)
3. $P(c)$	Simplification from (2)
4. $\forall x P(x)$	Universal generalization from (3)
5. $R(x)$	Simplification from (2)
6. $\forall x R(x)$	Universal generalization from (5)
7. $\forall x (P(x) \lor \forall x R(x))$	Conjunction from (4) and (6)

- §1.7 &1.8 WrittenHW #2 TCSS 321
- 1. [2] Consider the following steps for finding the solutions to $\sqrt{x+3} = x-3$. Determine if the steps are correct, or not. If not, identify what step(s) contain the error.
 - (a) $\sqrt{x+3} = x-3$ is given;
 - (b) $x + 3 = x^2 6x + 9$ by squaring both sides of 1.
 - (c) $0 = x^2 7x + 6$ obtained by subtracting x + 3 from both sides of 2.
 - (d) 0 = (x 1)(x 6) obtained by factoring the right-hand side of 3.
 - (e) x = 1 or x = 6 with follows from 4, because ab = 0 implies that a = 0 or b = 0.
- 2. [3] Prove that if n is a positive integer, then n is odd if and only if 5n + 6 is odd.
- 3. [3] Show if you pick three socks from a bin containing just red and white socks, you must get either a pair of red socks or a pair of white socks.
- 4. [2] Prove or disprove that there is a positive integer that equals the sum of the positive integers not exceeding it.