

Note: This is a practice midterm and is intended only for study purposes. The actual exam will contain different questions and perhaps a different layout.

1. TRUE/FALSE: Circle T in each of the following cases if the statement is *always* true. Otherwise, circle F. Let f and g be functions, and x and y be real numbers.

T F $(2f)'(x) = 2f'(x)$

T F $\cos(x + y) = \cos(x) + \cos(y)$

T F If $f'(a) < 0$, then the graph of $f(x)$ is decreasing when $x = a$.

T F When $MC = MR$ the company may be maximizing profit.

Show your work for the following problems. The correct answer with no supporting work will receive NO credit (this includes multiple choice questions).

2. [] For each rule of f given below, find $f'(x)$.

$$f(x) = \sin(x) + \frac{3}{x}$$

$$f(x) = 2x^2 + \ln(7x^2)$$

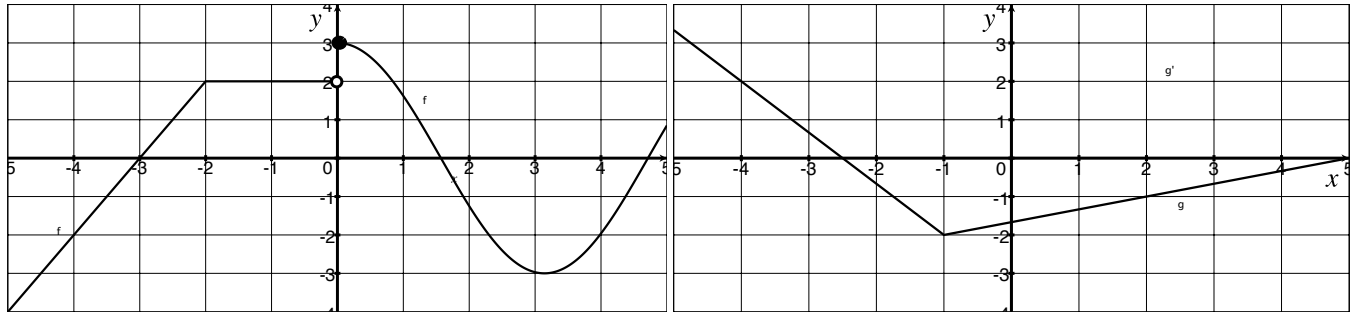
$$f(x) = \frac{3^x \cos(x)}{\sin(x)}$$

$$f(x) = (\sqrt{3x^4 - x})(e^x - 4)$$

$$f'(x) = \frac{6x^4 - x^{\frac{1}{3}}}{\sqrt{x}}$$

$$f(x) = (-4x + 7)^{12}(-2x^2 - 3x)^9$$

3. Let f be the function whose graph is on the left and g be the function whose graph is on the right.



- (a) [10] Estimate the following (if they exist):

$$f'(-3)$$

$$\left(\frac{f}{g}\right)'(-4)$$

$$(f \cdot g)'(-3)$$

$$(f \circ g)'(2)$$

4. The oil spill in the gulf is being fed by a well that produces approximately ??? cubic meters per day. Assume for now that the oil spill is approximately circular and the thickness of the oil is uniformly half a meter thick.

- (a) Write down a relationship between the total volume of the oil and the radius of the oil spill.
- (b) What rate is the volume of the oil cylinder expanding per hour?
- (c) How fast is the radius of the oil spill changing when the oil spill is 200 meters across?

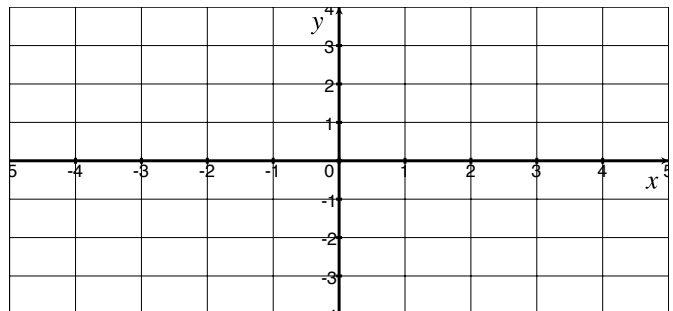
5. There is a “Rule of 70” or “Rule of 7” that commonly arises in economic or financial circles. The rule is as follows: The time it takes your money to double at an interest rate of r is approximately $\frac{70}{r}$. We will find out where this rule comes from.

(a) Assume you have P_0 dollars to invest. You find an investment that promises an effective annual interest rate of $r\%$. Write down a function that describes how much money you have after t years. (This is a throw back from §1.5.)

(b) We want to know when the investment doubles, that is, find t so that you have a total of $\$2P_0$.

(c) Draw the graph of $\ln x$ on the axis provided.

(d) Find the equation of the line that is tangent to the graph of $\ln x$ at $x = 1$.



(e) Use the line you found in (d) to approximate the function $\ln x$ when x is near 1 to simplify your answer in (b). Note, since r is usually closer to .05 than to .95, we can think of $1 + r$ as a number close to 1.

6. [] A manufacture has been selling 1000 televisions a week at \$360 each. A market survey indicates that for each \$26 rebate offered to a buyer, the number of sets sold will increase by 260 per week. Let q be the number of televisions demanded and p be the price.
- (a) Assume the relationship between the demand q and the price p is linear. Express p as a function of q .
- (b) Use the work from above to express the revenue, R , as *only* a function of q .
- (c) If the weekly cost function is $60000 + 120q$, where q is the number of television sets sold per week, how should it set the size of the rebate to maximize its profit?