

1. Let  $f(x, y) = \int_x^y \frac{1}{t} dt$ . Show your work for each of the following:
  - (a) [2] If possible find  $f(e^2, e)$ .
  - (b) [1] If possible find  $f(-1, 1)$ .
  - (c) [2] Find the domain of  $f$ .
  
2. The length of time that one waits in line, on average is  $W(x, y) = \frac{1}{x - y}$ , where  $y$  is the average arrival rate (with units of customers per unit of time) and  $x$  is the average service rate (with units of customers per unit of time).
  - (a) [2] Find the domain of  $W$ .
  - (b) [2] Evaluate  $W(12, 7)$  and explain its meaning.
  - (c) [2] Find  $\lim_{(x,y) \rightarrow (1,0)} W(x, y)$  and explain its meaning.
  
3. [4] Create a function  $f(x, y)$  with the following properties:
  - (a) continuous at  $(0, 0)$
  - (b)  $\lim_{(x,y) \rightarrow (3,0)} f(x, y) = \infty$
  - (c)  $f(3, 0) = -1$

1. Let  $f(x, y) = y^2 \log_2(x)$ 
  - (a) [2] Find  $\nabla f$ .
  - (b) [4] Find  $f_{xx}$ ,  $\frac{\partial}{\partial y}(\frac{\partial f}{\partial x})$ ,  $z_{yx}$ , and  $\frac{\partial^2 f}{\partial y^2}$
  - (c) [4] Find the derivative of  $f$  in the direction  $\overrightarrow{PQ}$  where  $P(1, 2)$  and  $Q(4, 3)$ .
2. A company makes a freestanding wood-burning stove and a fireplace-insert model. The cost function for producing  $x$  freestanding and  $y$  fireplace-insert stoves is

$$C = 32\sqrt{xy} + 175x + 205y + 1050.$$

- (a) [3] Find the marginal costs with respect to  $x$  and with respect to  $y$  when  $x = 80$  and  $y = 20$ .
- (b) [2] When additional production is needed, which model of stove would be more cost effective to produce (i.e. keep costs lower)? Explain your reasoning.