TMATH 126: Quiz 5

You may use any work of yours that you made from last week. This includes, practice problems from the book and worked out WebAssign problems. This *does not* include photocopies of notes from the book or tutorials shown on WebAssign. You may also use a calculator, but you are not allowed to use any device that can access the internet.

Show *all* your work (numerically, algebraically, or geometrically) for each and simplify. No credit is given without supporting work.

- 1. [6] TRUE/FALSE: Circle T in each of the following cases if the statement is *always* true and provide a brief justification. Otherwise, circle F and provide either counterexample or reasoning for your answer.
 - T F Riemann sums have nothing to do with double integrals.

T F
$$\int_0^2 \int_1^3 (20x^3 - 36x^2y^2) \, dy \, dx = \int_1^3 \int_0^2 (20x^3 - 36x^2y^2) \, dx \, dy$$

T F
$$\int_{-2}^{0} \int_{x}^{\sqrt{x+2}} (20x^3 - 36x^2y^2) \, dy \, dx = \int_{x}^{\sqrt{x+2}} \int_{-2}^{0} (20x^3 - 36x^2y^2) \, dx \, dy.$$

2. [4] Calculate the double integral: $\iint_R 2\cos(x+2y) \, dA \text{ over the region}$ $R = \{(x,y)|0 \le x \le 3\pi, 0 \le y \le \frac{\pi}{2}\}$

3. [3] Reverse the order of integration in the following but do not integrate

$$\int_0^{16} \int_{\sqrt{x}}^4 \frac{5}{y^3 + 1} \, dy \, dx$$

4. [7] Find the signed volume of the solid under the surface z = 6xy and above the triangle with vertices (1, 1), (3, 1), and (1, 5).