

### Quick Review:

Position as a function of time:  $f(t)$

Velocity =  $f'(t)$

Acceleration =  $f''(t)$

And for any general function:

First derivative:

If  $f'(x) > 0$  over an interval, then  $f(x)$  is increasing over that interval.

If  $f'(x) < 0$  over an interval, then  $f(x)$  is decreasing over that interval.

If  $f'(x) = 0$  over an interval, then  $f(x)$  is a constant over that interval

Second derivative:

If  $f''(x) > 0$ , then  $f(x)$  is concave up.

If  $f''(x) < 0$ , then  $f(x)$  is concave down.

If  $f''(x) = 0$ , then  $f(x)$  is a line or  $f(x)$  is a constant. (need to know  $f'(x)$  also)

**Short cuts to differentiation (sometimes called rules of differentiation).**

Constant:

$$f(x) = c, f'(x) = 0.$$

Power rule:

$$f(x) = x^n, f'(x) = nx^{n-1}$$

Constant multiple rule:

$$f(x) = cx^n, f'(x) = cf'(x) = c nx^{n-1}$$

Sum rule:

Given that  $f(x)$  and  $g(x)$  are differentiable, then

$$\frac{d}{dx}(f(x) + g(x)) = \frac{d}{dx}f(x) + \frac{d}{dx}g(x) = f'(x) + g'(x)$$

Difference rule:

Given that  $f(x)$  and  $g(x)$  are differentiable, then

$$\frac{d}{dx}(f(x) - g(x)) = \frac{d}{dx}f(x) - \frac{d}{dx}g(x) = f'(x) - g'(x)$$

Exponential function rules:

$$f(x) = a^x, f'(x) = \ln(a)a^x$$

$$f(x) = e^x, f'(x) = \ln(e)e^x = (1)e^x \text{ thus } f'(x) = e^x$$

Trig functions:

$$f(x) = \sin(x), f'(x) = \cos(x)$$

$$f(x) = \cos(x), f'(x) = -\sin(x)$$

$$f(x) = \tan(x), f'(x) = \sec^2(x)$$

Logarithmic functions:

$$f(x) = \ln(x), f'(x) = 1/x$$

$$f(x) = \log(x), f'(x) = 1/(x \ln(10))$$

Product Rule:

If  $f'(x)$  and  $g'(x)$  exist and  $h(x) = f(x) * g(x)$ , then  $(h)'(x)$  also exists and is given by:

$$h'(x) = f'(x)*g(x) + f(x) * g'(x).$$

Quotient rule:

If  $f'(x)$  and  $g'(x)$  exist and  $h(x) = f(x) / g(x)$ , then  $(h)'(x)$  also exists and is given by:

$$h'(x) = [g(x)*f'(x) - f(x)*g'(x)]/g^2(x)$$

Chain Rule:

If  $f'(x)$  and  $g'(x)$  exist and  $h(x) = f(x)g(x)$ , then  $h'(x)$  also exists as is given by:

$$h'(x) = f'(g(x))*g'(x)$$

if  $h(x) = g(x)f(x)$  then

$$h'(x) = g'(f(x))*f'(x)$$