

Note: This is a practice exam and is intended only for study purposes. The actual exam will contain different questions and may have a different layout.

1. TRUE/FALSE: Identify a statement as True in each of the following cases if the statement is *always* true and provide a brief justification. Otherwise, identify it as false and provide a counterexample.

Let  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  be vectors in  $\mathbb{R}^3$ .

Recall that  $\cdot$  refers to the dot product, and  $\times$  refers to the cross product.

- (a) Let  $f$  be a function of  $x$  and  $y$ . If  $\nabla f(c, d) = (2, 1)$ , then the vector  $\langle 2, 1 \rangle$  is tangent to the contour line of the surface of  $f$  at  $(c, d, f(c, d))$ .

- (b)  $\int_{-1}^2 \int_0^6 x^2 \sin(x - y) dx dy = \int_0^6 \int_{-1}^2 x^2 \sin(x - y) dy dx$

- (c)  $\int_{-1}^x \int_0^6 x^2 \sin(x - y) dx dy = \int_0^6 \int_{-1}^x x^2 \sin(x - y) dy dx$

Note: This practice exam is light on Section 14.6 but I wanted to get *something* to you!!! Check out class activities, WebHW & WrittenHW from the section and add that here! (Pick something with pictures, I like pictures.)

2. You are given the following data of a function  $g(x, y)$ . Your boss wants you to approximate  $g(.8, 1.4)$  and wants to be convinced you're doing something sophisticated. Find a linear approximation for your boss and explain your choices (there are many that you will make!).

$x$	$y$	$g(x, y)$
0.55	1.2	27
0.65	1.0	31
0.65	1.1	29
0.75	1.2	50

3. Find the maximum and minimum volumes of a rectangular box with the constraints that the surface area is  $1500\text{cm}^2$  and total edge length is  $200\text{cm}$ .

4. Common blood types are determined by three alleles,  $A$ ,  $B$ , and  $O$ . If  $p$  is the percent of allele  $A$  in the population,  $q$  is the percent of allele  $b$  in the population and  $r$  is the percent of allele  $O$  in the population then the proportion of individuals with a mixed blood type (e.g.  $AB$ ,  $AO$  or  $BO$ ) is  $P(p, q, r) = 2pq + 2pr + 2qr$ . Find the maximal  $P$  value.

5. Consider the double integral

$$\int_0^1 \int_{\arcsin y}^{\frac{\pi}{2}} \cos(x) \sqrt{1 + \cos^2 x} \, dx dy$$

(a) Sketch the region in the  $xy$ -plane where the integral is taken over.

(b) Switch the order of integration.

(c) Compute the double integral.