

Key

# TMATH 124: Quiz 1

Reasonable supporting work must be shown to earn credit.

1. [4] Use the graph of  $h$  below to find the limits (either numerically, graphically, or algebraically), if they exist:

$\lim_{x \rightarrow 3^+} h(x)$

4

as I approach 3 from above so 3.1 or 3.01...

Table

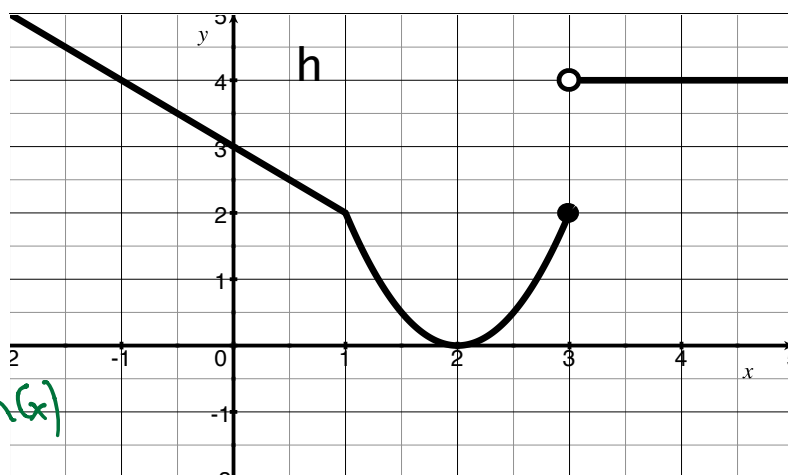
x	y
3.1	4
3.01	4
3.001	4

$\lim_{x \rightarrow 3} h(x)$

$\lim_{x \rightarrow 3^-} h(x) = 2$

$\neq \lim_{x \rightarrow 3^+} h(x)$

DNE



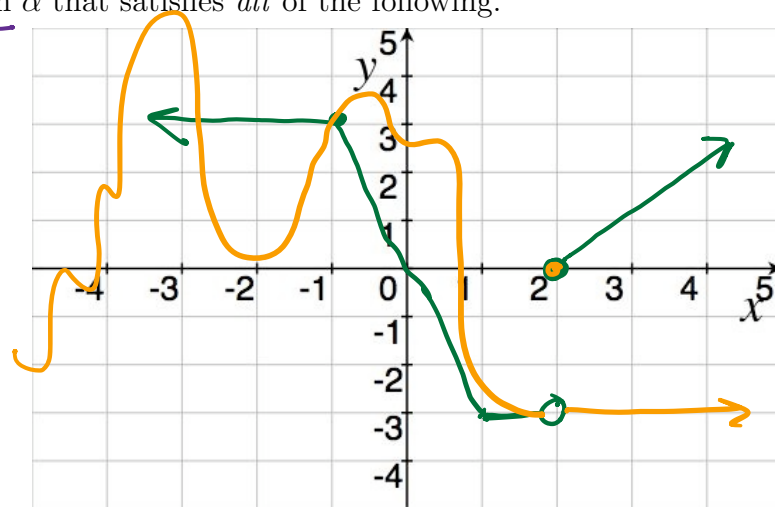
2. [4] Sketch the graph of a function  $\alpha$  that satisfies all of the following.

(a)  $\lim_{x \rightarrow -1} \alpha(x) = 3$

(b)  $\lim_{x \rightarrow 2^-} \alpha(x) = -3$

(c)  $\alpha(2) = 0$

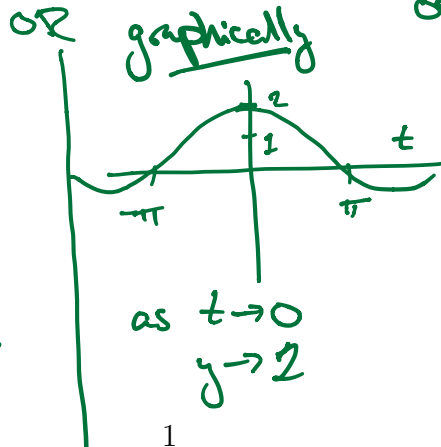
So many answers!  
another possible answer in orange



3. [2] Find the limit (either numerically, graphically, or algebraically), if it exists:  $\lim_{t \rightarrow 0} \frac{2 \sin(t)}{t}$

Numerically

t	$\frac{2 \sin(t)}{t}$
-0.1	1.99
-0.01	1.999967
-0.001	1.9999997
0	DNE
0.001	1.9999997
0.01	1.999967
0.1	1.99



OR algebraically

Recall Fact from Videos

$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

$$\lim_{t \rightarrow 0} \frac{2 \sin(t)}{t} = \lim_{t \rightarrow 0} 2 \cdot \frac{\sin(t)}{t}$$

$$= 2 \cdot \lim_{t \rightarrow 0} \frac{\sin(t)}{t} = 2 \cdot 1 = 2$$

2

graph reading +.5  
from above so +.5  
got it +1  
if note 2 +1 partial

graph reading +.5  
left and right +.5  
got it +1  
if give 1-sided +1 partial

start +.5  
notation +.5  
def of limit +.5  
got it +.5