

+4EL

Correct

Extra Credit #8

A rectangle's length is increasing at a rate of  $8\text{ cm/s}$  and its width is increasing at a rate of  $3\text{ cm/s}$ . When the length is  $20\text{ cm}$  and the width is  $10\text{ cm}$ , how fast is the area of the rectangle increasing? Find a formula for how fast the area of the rectangle increases when the width of the rectangle is  $w$  and the length is  $l$ .

$$a = lw \quad (\text{area} = \text{length}(\text{width}) \Leftarrow \text{area of a rectangle})$$

Product

$$\frac{da}{dt} = l \frac{dw}{dt} + w \frac{dl}{dt} \quad \Leftarrow \text{here we took the derivative of our "area of a rectangle"}$$

Product Rule

with respect to time ( $d/dt$ )

now, we know "is increasing at a rate of" is fancy for derivative, so we have all our numbers and can simply plug them in:

$$\frac{da}{dt} = (8)(10) + (20)(3)$$

$w=10$   
 $l=20$

$$= 80 + 60 = 140 \quad \Leftarrow \text{simplify}$$

derivative  
at a  
particular  
point in  
time.

$$140 \text{ cm}^2/\text{s} \quad \Leftarrow \text{solve and add your units}$$

since you mention units?