## Extrema §4.1

1. Draw graphs of two functions $f$ and $g$ so that:
(a) $f$ is continuous on $[0,5)$
(b) $f$ has a local max when $x=3$
(c) $f^{\prime}(3)=0$
(d) $g$ is continuous on $(-5,0]$
(e) $g$ has a local max when $x=-3$
(f) $g^{\prime}(-3)$ is not defined.

2. Consider $m(x)=x^{3}-9 x^{2}-48 x-5$.
(a) Find the critical points of $m$.
(b) Find all local extrema and their values.

## Mean Value Theorem §4.2

1. Consider the function $f(x)=\cos 2 x$ with a domain of $[\pi / 8,7 \pi / 8]$.
(a) State Rolle's Theorem.
(b) Verify the three hypotheses of Rolle's Theorem.
(c) Find all numbers $c$ that satisfy the conclusion of Rolle's Theorem.
2. Exhibit the Mean Value Theorem for $y=x^{3}+x-1$ on the interval [1,2].
