Exam 1

TMath 120

Autumn 2018

NAME:

1. [3] TRUE/FALSE: Circle T in each of the following cases if the statement is *always* true. Otherwise, circle F.

T F
$$\frac{1}{b+1} + \frac{1}{b} = \frac{3}{b+1}$$

T F $(1-2i)(4-i) = 6 - 9i$
T F $\frac{-1}{3-i} = \frac{-3}{10} - \frac{1}{10}i$

Show all your work. Reasonable supporting work must be shown to earn credit.

- 2. A tractor is purchased for \$17,000 and depreciates linearly at a rate of \$1,700 a year.
 - (a) [3] (Quiz1 #1) Write a function that returns the value of the tractor at a certain time. Be sure to define any variables that you create!

(b) [2] (WebHW2 #22) When will the tractor have no value?

3. Let f be the piece-wise defined function comprised a line and a parabola shown below.



- iv. [1] (§1.1 #104) the minimum of f.
- v. [1] (Transformations Activity #5) all possible x such that f(x) = -4.
- (b) [4] (PracticeExam #4) Find the formula for f in the indicated form:

$$f(x) = \begin{cases} & \text{if } -5 \le x \le -2\\ & \text{if } -2 < x \le 4 \end{cases}$$

(c) [3] (WebHW3 #16) Graph $\frac{1}{2}f(x) - 1$.

4. Let *h* be the *function* defined by: $h(x) = \begin{cases} \frac{1}{2}x - 2 & -4 \le x \le 2\\ 2x - 5 & 2 < x < 4 \end{cases}$

	``								
				$y_{4}^{5\uparrow}$					
				3					
				2					
				1					
n of <i>h</i> ? -4	-3	-2	-1	0	1	2	3	4	5
				-1					- <i>A</i>
				-2					
				-3					
ю. 				-4					
	of <i>h</i> ? -4	-4 -3	-4 -3 -2	-4 -3 -2 -1	of h? -4 -3 -2 -1 0 -1 -2 -3	of h? -4 -3 -2 -1 0 1 -2 -3	of h? -4 -3 -2 -1 0 1 2 -4 -3 -2 -1 0 1 2 -4 -3 -2 -1 0 1 2 -1 -1 -2 -3	of h? -4 -3 -2 -1 0 1 2 3 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -	of h? -4 -3 -2 -1 0 1 2 3 4 -1 -2 -3

- (d) [2] (§1.7 #44) Graph h^{-1} if it exists.
- 5. Provide a graph AND an algebraic rule/expression for each of the functions described below:
 - (a) [3] (Polynomial Activity#4) A 4 degree polynomial whose only roots are 2 & -3.

				y 1					
				3					
			-	2					
				1			C.		
-4	-3	-2	-1	0	1	2	3	4	,5
				-1					A
				-2					
				-3					
				-4					

(b) [3] (Line Activity#13) A line perpendicular to y = 3x - 2.

			_	y4	_			_	
				3					
				2					
				1					
-4	-3	-2	-1	0	1	2	3	4	v
				-1					л
				-2					
				-3					
				-4					

6. Let $\alpha(x) = \frac{2}{x-3}$. The graph of α is shown below. (a) [2] (§1.3 #32) Find $\alpha(x+h) - \alpha(x)$ and simplify.

x

(b) [3] (§1.7 #78) Find the algebraic rule/expression for $\alpha^{-1}(x)$.

7. [3] (Autumn120Exam1 #7) Find the real or complex solutions to $\frac{2}{5}(x-1)^2 + \frac{7}{2} = 0$.

8. [4] (WebHW6 #17) The area of a rectangle is $3x^4 - 6x^3 + 14x^2 - 4x + 8$ square centimeters. The length is $x^2 - 2x + 4$ cm. Find its width (as a function of x!).

- Choose ONE of the following. Clearly identify which of the two you are answering and what work you want to be considered for credit.
 No, doing both questions will not earn you extra credit.
 - (a) (WebHW4 #14) A rancher with 150 meters of fence would like to enclose a rectangular region next to a river which can serve as a natural boundary meaning no fencing is needed.
 - i. [3] Write a rule/expression that returns the area enclosed by the fence as a function of the width of the rectangular region.
 - ii. [2] Find the maximum area that can be enclosed.
 - (b) (WordProblems #3)) You have 8oz of coffee which has about .003oz of caffeine sitting in a 24oz cup. You would like a higher dose of caffeine and plan to add espresso which has .0028oz per 2oz shot.
 - i. [3] Write a rule/expression that returns the percentage (as a decimal) of caffeine in the cup as a function of espresso that you add.
 - ii. [2] Give the domain of this function and justify your answer.