NAME: This is a sample midterm to be used for practice. This is not a template for the midterm that will be given in class. Many of the questions on the Midterm will look quite different than those appearing here.

1. TRUE/FALSE: Circle T in each of the following cases if the statement is always true. Otherwise, circle F.

 $\chi^2 \chi^3 = (\chi \chi)(\chi \chi \chi) = \chi^3$ 

log (x,y) = log x + log y

Let x and y be positive numbers.

T 
$$\bigcirc x^2x^3 = x^6$$

T 
$$\bigcirc$$
  $\log(x+y) = \log(x) \cdot \log(y)$ 

(T) F 
$$\log(\frac{x}{y}) = \log(x) - \log(xy)$$

$$TF \frac{\log x}{\log y} = \frac{x}{y}$$

$$T \widehat{F} \log_2 5x^7 = 7\log_2 5x$$

$$E = \log_2 6x - \log_2 6x$$

T F 
$$\log_2 5x^7 = 7\log_2 5x$$
 7  $\log_2 5x = \log_3 (5x)^7$   
T F  $\log(\log(10)) = 0$ .  $\log(\log(x)) = \log(10) = 0$   
T F For all numbers  $z, \sqrt{z^2} = z$   $\log(x) = 1$ 

LONG ANSWERS: Show all your work and circle you final answer. Correct answers will not get credit without supporting work.

2. Given  $-x = \frac{2xy}{2y-1}$ , solve for y.

$$(\partial y^{-1}) - x = \frac{\partial xy}{\partial y^{-1}} (\partial y^{-1})$$

$$-\partial xy + x = \partial xy$$

$$+\partial xy$$

$$+\partial xy$$

$$-\frac{x}{4x} = 4xy$$

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3. [2] Define the rule of the function log.

4. [4] Assume b, x,y > 0, simplify the following:

$$\frac{(b^x)^{x-1}}{b^{-x}}$$

 $\frac{(b^x)^{x-1}}{b^{-x}}$  we  $(b^a)^c = b^{ac}$ 

$$= \frac{b^{-x}}{(b^{-x})^{2}} = \frac{b^{-x}}{b^{-x}}$$

$$= \frac{b^{-x}}{b^{-x}} = \frac{b^{-x}}{b^{-x}}$$

2 - [logs 25 + logs 2] 2 - logs 52 - logs 2 2-2-logs&

$$\frac{\sqrt[3]{x^2}(y^2)^{\frac{3}{2}}}{x^{\frac{2}{3}}y^2}$$

$$\log_2 \tfrac{1}{4} + 2$$

5. [3] Find 
$$x$$
 in the following:

$$2^{4x-1} = 3^{1-x}$$

$$\ln 3^{1-x} = \ln 3^{1-x}$$

$$(4x-1)\ln 3 = (1-x)\ln 3$$

$$4x\ln 3 - \ln 3 = \ln 3 - x\ln 3$$

$$4x\ln 3 + x\ln 3 = \ln 3 + \ln 3$$

$$x(4\ln 3 + \ln 3) = \ln 3 + \ln 3$$

$$x = \frac{\ln 3 + \ln 3}{4\ln 3 + \ln 3}$$
6. Find a formula for the inverse function

6. Find a formula for the inverse function 
$$f^{-1}$$
 of the indicated function  $f$ .

$$f(x) = 4x^{\frac{3}{7}} - 1$$

$$X = 4y^{\frac{3}{7}} - 1$$

$$X + 1 = 4y^{\frac{3}{7}}$$

$$\frac{X+1}{4} = y^{\frac{3}{7}}$$

$$(\frac{X+1}{4})^{\frac{7}{3}} = y$$

7. Write the given expression as a single logarithm.

$$2\ln 2x - 3(\ln x^2 + \ln x)$$

$$2\ln 3x - 3(\ln x^{2} \cdot x)$$
  
 $2\ln 3x - 3(\ln x^{2} \cdot x)$   
 $2\ln 3x - 3(\ln x^{2} \cdot x)$   
 $2\ln 3x - 3(\ln x^{2} \cdot x)$   
 $2\ln (3x)^{2} - \ln (x^{3})^{3}$   
 $2\ln (4x^{2}) - \ln x^{9}$   
 $2\ln \frac{4x^{2}}{x^{9}}$   
 $2\ln \frac{4}{x^{7}}$ 

$$5^{x} = 2$$

$$\ln 5^{x} = \ln 2$$

$$x \ln 5 = \ln 2$$

$$x = \frac{\ln 2}{\ln 5}$$

$$f(x) = 3 \cdot 2^{x} + 4$$

$$X = 3 \cdot 2^{y} + 4$$

$$X - 4 = 3 \cdot 2^{y}$$

$$X$$

$$\log(x-16) = 2 - \log(x-1)$$

$$\log(x-16) + \log(x-1) = 0$$

$$\log(x-16) + \log(x-16) = 0$$

$$\log$$

- 9. [] Chani has \$20,000 in student loans at the end of her college education with 8% interest compounded quarterly. Chani chooses not to make payments after graduation since she has had trouble securing employment.
  - (a) How much money will Chani owe after 2 years assuming no extra fees will be incurred?

$$20,000 \left(1+\frac{.03}{4}\right)^{4.2}$$

## (b) How long will it take for Chani's loan to double?

when will
$$40,000 = 20,000(1+\frac{03}{4})^{44}$$

$$2 = (1+\frac{03}{4})^{44}$$

$$\ln 2 = \ln (1+\frac{03}{4})^{44}$$

$$\ln 2 = 44 \ln (1+\frac{03}{4})$$

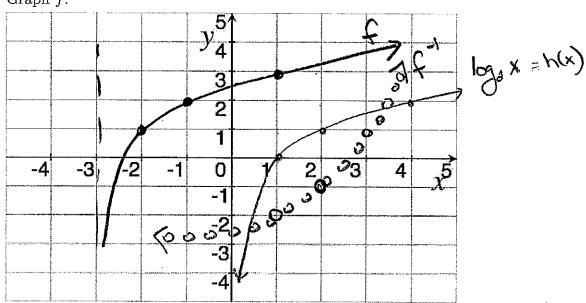
$$\ln (1+\frac{03}{4}) = 44$$

$$\ln (1+\frac{03}{4}) = 4$$

- 10. Let  $h(x) = \log_2 x$  and  $f(x) = \log_2(x+3) + 1$ .
  - (a) List the transformations needed to transform the graph of h to the graph of f.

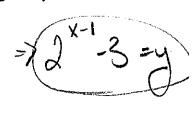
shift up I und shift left 3 unds

(b) Graph f.



5 pusses the hours. The ket so I has an inverse note (c) Find the inverse function to f.

X=log (y+3)+1 2 x -1 = 10x oly +3) 5 2x-1 = y+3 = 2x-1



- (d) Graph the inverse function to f.

  (a) Graph the inverse function to f.

  (b) Simplifying f (1,-2)

  11. Find the distance between the zero of  $\log_2 x$  and the point (-2,3).

note the zero of lay x 15 when 100 x =0 => X=1

So we want the distance between (110) 4 (-2,3)

