## Practice TQS 120 Final

NAME: This is a sample final to be used for practice. This is *not a template* for the Final that will be given in class. Many of the questions on the Final will look quite di?erent than those appearing here.

[10] Let f & g, be functions.

- T F  $(f \circ g)(x) = (g \circ f)(x)$
- T F  $\left(\frac{f}{g}\right)(x) = \left(\frac{g}{f}\right)(x)$
- T F  $\sqrt{(x^2)} = x$  for all real numbers x.
- T F If  $h(x) = x^2 + 1$ , then h is an even function.
- T F  $\ln \frac{x}{y} = \ln x \ln y$  for all positive numbers x and y.
- T F  $\log(\log(10)) = 0.$
- T F Just as every integer is either even or odd, every function is either an even function or odd function.
- T F  $\sin(\frac{\pi}{3} + x) = \sin\frac{\pi}{3} + x$
- T F If  $\sin \theta > 0$  and  $\tan \theta < 0$ , then  $\cos \theta < 0$
- T F The range of  $\sin^{-1}$  is  $[0, \pi]$

Right answers will *not* get credit without supporting work. Note "undefined" and "no solution" are possible answers.

1. Find all x such that

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$$2(5 + (8 - x)^2)^{-\frac{1}{2}} - 1 = 0$$

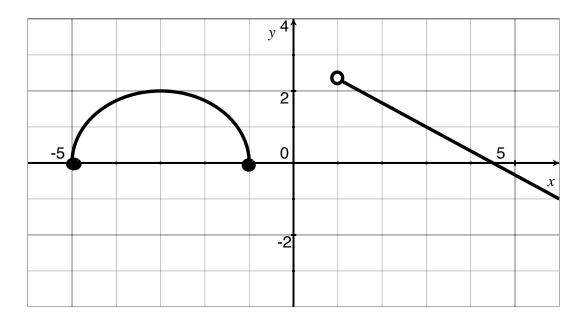
2. [2] Explain what a function is.

- 3. Given  $m(x) = \frac{x}{x-5}$ , and  $n(x) = \sqrt{4x-8}$ ,
  - (a) [4] If p(x) = 3m(x+1), find the domain and rule of p.

(b) [3] Find the domain and rule of  $n \circ m$ .

(c) [5] Find the domain and rule of  $\frac{n}{m}$ .

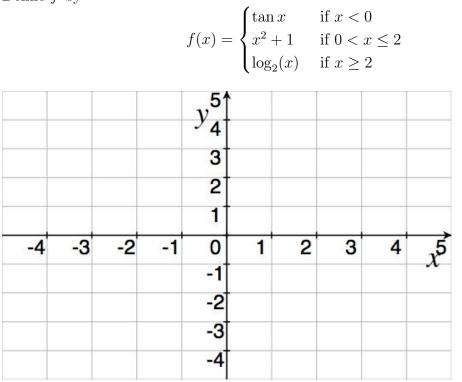
4. [3] Let the following be the graph of g.



- (a) What is the domain of g?
- (b) The function g is a piecewise defined function consisting of a straight line and a semicircle. Write down the rule for g.

- (c) Use the graph above to *estimate* all x value(s) so that g(x) = 1?
- (d) Find the total length (of the curve and the line) that is graphed above.

5. Define f by



- (a) [8] Graph f on the axes above.
- (b) [9] Find the following if possible: f(1) f(2) + f(3)

$$f(\frac{-13\pi}{4})$$

Range of 
$$f$$

f(0)

6. [16] Find all values x that satisfy the following (be sure to check your answers):

$$|-2x-6| = 2 5^{4x-1} = 7^x$$

7. [6] Assuming that  $\log_3 x = 5.3$  and  $\log_3 y = 2.1$  find the following exactly:  $27\pi^3$ 

$$\log_3 \frac{27x^3}{y^2} \qquad \qquad \log_9 3x$$

8. [4] Find all exact values for x that satisfy the following:  $\log(x - 16) = 2 - \log(x - 1)$   $3^{5x}9^x = 27$ 

9. Simplify:

$$\frac{\sqrt{c^2 d^6}}{\sqrt{4c^3 d^{-4}}}$$

 $2 - \log_5(25z)$ 

10. [7] Given f(3) = 0, use the factor theorem to find the other roots of  $x^4 - 3x^3 - 25x^2 + 75x$ 

11. Simplify:

$$\sin^{-1}(\sin\frac{3\pi}{4})$$

 $\frac{\cos x}{1-\sin x} + \frac{1-\sin x}{\cos x}$ 

12. [4] Let  $\frac{-\pi}{2} < \theta < 0$  and  $\cos \theta = \frac{1}{5}$ . Find  $\tan \theta$ .

13. [6] Let  $\frac{\pi}{2} < \phi < \pi$  and  $\frac{-\pi}{2} < \theta < 0$ . Given that  $\sin \phi = \frac{2}{3}$  and that  $\cos \theta = \frac{1}{5}$ , find  $\cos(\theta + \phi)$ . (You are free to use results from #10 above.)

14. [5] Your given a 16 oz mocha that is a rather weak 3% espresso. You, knowing you'll be up late studying mathematics, would rather like a 30% espresso drink. Realizing this you purchase an espresso machine. How much weak mocha do you discard and replace with straight espresso to have a 16 oz mocha with the desired concentration?

15. [5] Use the conventions from the book and class and let A be measure of the angle opposite the side with length a. Given that  $a = 10\sqrt{2}$ , b = 20, and  $A = \frac{\pi}{6}$  with the standard notation, determine if the information describes 0, 1, or 2 triangles and solve for them/it if they/it exist/s.

16. [5] Suppose a radioactive isotope is such that one-fifth of the atoms in a sample decay after three years. Find the half-life of this isotope

17. [5] The force of friction is sometimes calculated by multiplying the normal force (the force holding the object up) by the mass of the object and by a 'coefficient of friction'. The coefficient of friction is a dimensionless number that depends on the two surfaces being pressed together.

A 10kg block is sliding down a dry glass ramp with angle of elevation of  $60^{\circ}$  and with a coefficient of friction of .94. Find the force of friction acting on the block.