

Key

## Quiz 5

1. [1] TRUE/FALSE: Circle T in each of the following cases if the statement is *always* true. Otherwise, circle F. Let  $x$ ,  $y$ , and  $z$  be real numbers.

T  F  $(\sin x)^2 + (\cos x)^2 = 1$

T  F  $\sin(u + v) = \sin(x) + \sin(y)$

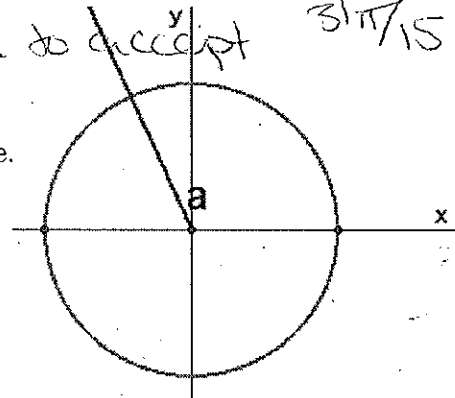
Show *all* your work algebraically for each and simplify. No credit is given without supporting work. There are *two* sides to this quiz.

2. [1] Find an angle that is coterminal with  $\frac{31\pi}{15}$ .

$$\frac{31\pi}{15} - 2\pi = \frac{31\pi}{15} - \frac{30\pi}{15} = \frac{\pi}{15}$$

note  $\frac{31\pi}{15} \approx 372^\circ$   
 $\frac{\pi}{15} \approx 12^\circ$

3. [2] (WebHW12 #1) Consider the angle pictured here. The angle  $a$  is an integer when measured in radians. Give the radian measure of the angle.



integer (+)

eyeballed radians right (+)

4. [3] (Circles & Angles Wks) Find the point(s) on the unit circle whose first coordinate is  $-\frac{2}{3}$ .

$$x^2 + y^2 = 1 \quad (+, -)$$

so

$$\left(-\frac{2}{3}\right)^2 + y^2 = 1$$

(+,-)

$$y^2 = 1 - \frac{4}{9}$$

$$y^2 = \frac{5}{9}$$

$$y = \pm \sqrt{\frac{5}{9}}$$

alg (+)

and

$$\left(-\frac{2}{3}, \frac{\sqrt{5}}{3}\right)$$

$$\left(-\frac{2}{3}, -\frac{\sqrt{5}}{3}\right)$$

signs (+, -)

5. [3] (§5.3 #24) If  $\cos \theta = -\frac{2}{3}$  and  $\theta$  is between  $\pi$  and  $2\pi$ , find  $\sin \theta$ .

$$\cos^2 \theta + \sin^2 \theta = 1 \quad (+)$$

$$\left(-\frac{2}{3}\right)^2 + \sin^2 \theta = 1$$

(+,-)

$$\sin^2 \theta = 1 - \frac{4}{9}$$

$$\sin^2 \theta = \frac{5}{9}$$

$$\sin \theta = \pm \sqrt{\frac{5}{9}}$$

alg (+)

signs (+, -)

$$\sin \theta = -\frac{\sqrt{5}}{3}$$