

# Quiz 2

Key

Show *all* your work. No credit is given without reasonable supporting work. There are *two* sides to this quiz.

1. (WebHW2 #11) Let  $f$  be the piecewise defined function whose graph is shown below on the right:

(a) (WebHW#7) [1] Approximate  $f(2)$  and  $f(-1)$ .

$f(2) \approx 5$

$f(-1) \approx -5$

(b) (Transformation Wks #5e) [1]

For what  $x$  value(s) does  $f(x) = 4$ ?

if  $x = 0$  then  $f(x) = 4$

(c) (WebHW #11) [1] What is the domain of  $f$ ?

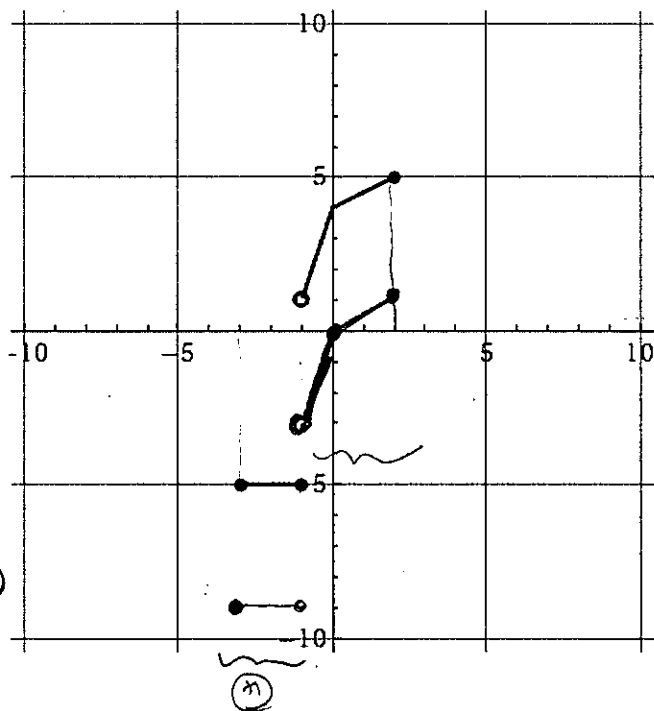
$[-3, 2]$

#'s  $+ .5$

endpts  $+ .5$

(d) (Transformation Wks #5c) [2]

Draw the graph of  $g(x) = f(x) - 4$ .



Answer #1 } The graph of  $g$  looks like the graph of  $f$  but shifted down 4 units  
 shift  $+ .5$   
 unit  $+ .5$

2. Let  $f(x) = \frac{2}{x}$  and  $g(x) = \frac{4}{x+4}$  for the following questions.

(a) (§2.1 #15) [2] Find  $g(a-1)$  and simplify.

$$g(a-1) = \frac{4}{\boxed{a-1}+4} = \frac{4}{a+3}$$

comp (+) simplify (+5)

(b) (§2.7 #5) [2] Find  $fg$  and the domain of  $fg$

$$(fg)(x) = f(x) \cdot g(x) = \frac{2}{x} \cdot \frac{4}{x+4} = \frac{8}{x(x+4)} \quad \left. \right\} (+1)$$

Domain: den can't equal zero (+5)

$$x(x+4) \neq 0$$

(+5)  $\Rightarrow x \neq 0$  and  $x+4 \neq 0$  So  $x \neq 0$  and  $x \neq -4$

(c) (WebHW3 #7) [1] Find  $(f \circ g)(3)$  and simplify.

$$\text{or } (-\infty, -4) \cup (-4, 0) \cup (0, \infty)$$

$$(f \circ g)(3) = f(g(3))$$

$$= f\left(\frac{4}{\boxed{3}+4}\right) = f\left(\frac{4}{7}\right) \quad \left. \right\} (+5)$$

$$= \frac{2}{\boxed{\frac{4}{7}}} = 2 \div \frac{4}{7} = 2 \cdot \frac{7}{4} = \frac{14}{4} = \frac{7}{2} \quad \left. \right\} (+5)$$