

# 2 Dimensional Congruence

definitions & theorems from Origametry by Daniel Heath.

While working in a group make sure you:

- Expect to make mistakes but be sure to reflect/learn from them!
- Are civil and are aware of your impact on others.
- Assume and engage with the strongest argument while assuming best intent.

Mark distinct  $A$  and  $B$  points on a patty paper. Use a ruler to measure the distance  $AB$ , and then mark any other two points  $C$  and  $D$  so that  $AB = CD$ .

1. Can you find a fold  $\phi$  so that  $\phi(\overline{AB}) = \overline{CD}$ . (Note that if  $S$  is a set, we define  $\phi(S) = \{\phi(X) | X \in S\}$ ).

2. Can you find a fold  $\phi$  so that  $\phi(A) = C$  and  $\phi(B) = D$ ? If so describe how to define  $\phi$  given arbitrary points  $X, Y, Z$ , and  $W$  so that  $XY = ZW$ .

3. Can you find a fold  $\phi$  so that  $\phi(A) = D$  and  $\phi(B) = C$ ? If so describe how to define  $\phi$  given arbitrary points  $X, Y, Z$ , and  $W$  so that  $XY = ZW$ .

4. Recall in 1 dimension that a translation by  $t$  (where a point with coordinate  $x$  was shifted to coordinate  $x + t$ ) could be created by composing two folds. Can translations be created in 2 dimensions as well? If so, describe how. If not, explain why not.

5. Consider composing two folds  $\phi_1$  and  $\phi_2$  with respective creases that intersect. Describe the effect.