

# 2 Dimensional Euclid

definitions & theorems from Origametry by Daniel Heath.

While working in a group make sure you:

- Expect to make mistakes but be sure to reflect/learn from them!
- Are civil and are aware of your impact on others.
- Assume and engage with the strongest argument while assuming best intent.

1. Given a line  $l$ , on patty paper and a point  $A$  not on the line, what steps can you take to fold a line through  $A$  that is parallel to  $l$ ?

2. Begin with two parallel lines on a sheet of patty paper an fold any transversal over the parallel lines. What can you say about the alternating interior angles?

**Theorem 6.4.** *If two distinct lines  $l_1$  and  $l_2$  are parallel, then there is a unique fold  $\phi$  that takes  $l_1$  to  $l_2$ .*

3. Begin with patty paper with two parallel lines  $l$  and  $m$  and a point  $A$  not on either line. Let  $\phi_l$  be the fold with crease  $l$  and  $\phi_m$  be the fold with crease  $m$ .

(a) Find  $\phi_l(A) = A'$  and  $\phi_m(A') = B$ .

(b) Fold the line  $\overleftrightarrow{AB}$  and mark points  $C = l \cap \overleftrightarrow{AB}$  and  $D = m \cap \overleftrightarrow{AB}$ .

(c) Find a relationship between  $AB$  and  $CD$  that is true in general.

**Theorem 6.7.** *Let  $l$  and  $m$  be parallel lines, and  $\phi_l$  and  $\phi_m$  be the fold with crease  $l$  and  $m$  respectively. Let  $A$  be any point and  $B = \phi_m \circ \phi_l(A)$ . Then  $l \perp \overleftrightarrow{AB}$  and  $AB = CD$ .*