## TMath 124

Practice



Note: This is a practice midterm and is intended only for study purposes. The actual exam will contain different questions and perhaps a different layout.

1. [] TRUE/FALSE: Circle T in each of the following cases if the statement is *always* true. Otherwise, circle F. Let f and g be functions.

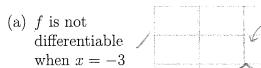
T  $\widehat{\mathbb{F}}$   $\frac{d}{dx}b^c=cb^{c-1}$  for a fixed b and c

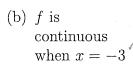
T (F) 
$$(x+y)^2 = x^2 + y^2$$
 (xy) = x + xy + y + y T

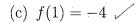
T (F)  $\frac{d}{dx}2^x = x2^{x-1}$  (xy) =  $2^x$  (xy) =  $2^x$ 

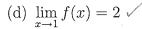
Show your work for the following problems. The correct answer with no supporting work will receive NO credit (this includes multiple choice questions).

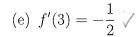
2. [] Sketch the graph of an example function f that satisfies the following conditions:





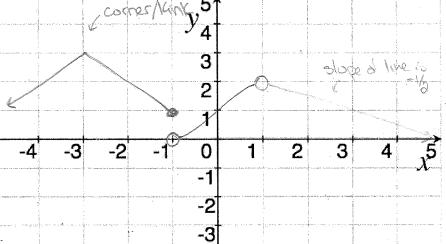






(f) 
$$\lim_{x \to -1^+} f(x) = 0$$

(g) 
$$\lim_{x \to -1^-} f(x) = 1$$



Find a brough for the above graph

$$S(x) = \begin{cases} -x + 6 & \text{if } x \le -3 \\ -x & \text{if } -3 \le x \le -1 \\ x + 1 & \text{if } -1 < x \le 1 \\ 4 & 1 \text{if } x = 1 \\ -3 & 1 \le x \le 1 \end{cases}$$

3. Find the following:

$$\lim_{x \to 0} \frac{3\sin(4x)}{2\sin(3x)} \cdot \frac{\partial x}{\partial x} = \lim_{x \to 0} \left(\frac{\sin 4x}{4x}\right) \left(\frac{3\cdot 2x}{\sin 3x}\right)$$

$$= \lim_{x \to 0} \frac{3\sin(4x)}{2\sin(3x)} \cdot \frac{\partial x}{\partial x} = \lim_{x \to 0} \left(\frac{\sin 4x}{4x}\right) \left(\frac{3\cdot 2x}{\sin 3x}\right)$$

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$$\lim_{x \to 0} \frac{\cos x - 1}{\sin x} \quad (\cos x + 1)$$

4. Suppose that f(2) = -3, g(2) = 4, f'(2) = -2, and g'(2) = 7. Find h'(2) where h is: h(x) = 5f(x) - 4g(x)

$$= \frac{1}{h(x)} = \frac$$

$$h(x) = \frac{g(x)}{1+f(x)}$$

$$h(x) = \left[\frac{g(x)}{1+f(x)}\right] - \left[\frac{g(x)}{1+f(x)}\right]$$

$$= 7 h'(2) = 9(2) g'(2) - g(2) g'(2) = (4x-2) - (-3)(7)$$

$$= (-8+2) f(2) = 13 f(2)$$

5. If F(x) = f(g(x)), where f(-2) = 8, f'(-2) = 4, f'(5) = 3, g(5) = -2, and g'(5) = 6, find F'(5).

$$\left(\frac{3mx}{asx}\right)' = \frac{cosx}{cossx} \frac{cosx}{s} - \frac{smx}{smx} \left(\frac{smx}{smx}\right)$$

$$= \frac{cossx}{cossx} = \frac{sec^2x}{smx}$$

rak: no regrest to simply?

7. Find the  $\frac{dy}{dx}$  of the following:

$$y = (2x^{2} + 7x^{2})(3^{x} - 2^{x})$$

$$= (9x^{2})(3^{x} - 2^{x}) \qquad \text{product ob}$$

$$= (9x^{2})(3^{x} - 2^{x}) \qquad \text{product ob}$$

$$= (9x^{2})(3^{x} - 2^{x}) + (3^{x} - 2^{x})$$

$$y = \frac{\sin(x) + x^2 \cos(x)}{\cos(x)}$$

$$\frac{1}{2} = \cos x (\cos x + x^{2} (-\sin x) + 2 \cos x)$$

$$\frac{\sin^{2}(x^{3})}{\cos^{2} x} = (-\sin^{2}(x^{3}))^{2}$$

$$\frac{\sin^{2}(x^{3})}{\cos^{2} x} = (-\sin^{2}(x^{3}))^{2}$$

$$y' = x (-\sin^{2}(x^{3}))^{2} - (-\sin^{2}(x^{3}))^{2}$$

$$= x (-\sin^{2}(x^{3}))^{2} - (-\sin^{2}(x^{3}))^{2}$$

$$= x (-\cos^{2}(x^{3}))^{2} - (-\cos^{2}(x^{3}))^{2}$$

00 grahed No Product

$$y = \sqrt{\frac{x^2 + 1}{4x^5 - 3x}}$$
Chan

Inside  $g(x) = \frac{x^2 + 1}{4x^5 - 3x}$ 

$$G'(x) = \frac{x^2 + 1}{4x^5 - 3x}$$

$$G'(x) = \frac{x^2 + 1$$

inside  $g(x) = e^{\sin(x)}$   $g'(x) = e^{\sin(x)} \cdot \partial x$ where  $g(x) = e^{\sin(x)}$ 

$$f(u) = u^{3} \qquad g'(x) = chown? t$$

$$f(u) = u^{3} \qquad g'(x) = du$$

$$f'(g(x))g'(x) = d(sin(x^{3})) \cdot Cos(x^{3}) \cdot 3x^{3}$$

$$f(u) = x^{3} \qquad f'(x) = 3x^{2}$$

$$f(u) = sinu \qquad f'(u) = cosu$$

$$y = (sin x)^{1be^{2}} = (6in(x))^{2}$$

$$nonce \qquad ln e^{2} = d$$

$$g(x) = sinx \qquad g'(x) = cosx$$

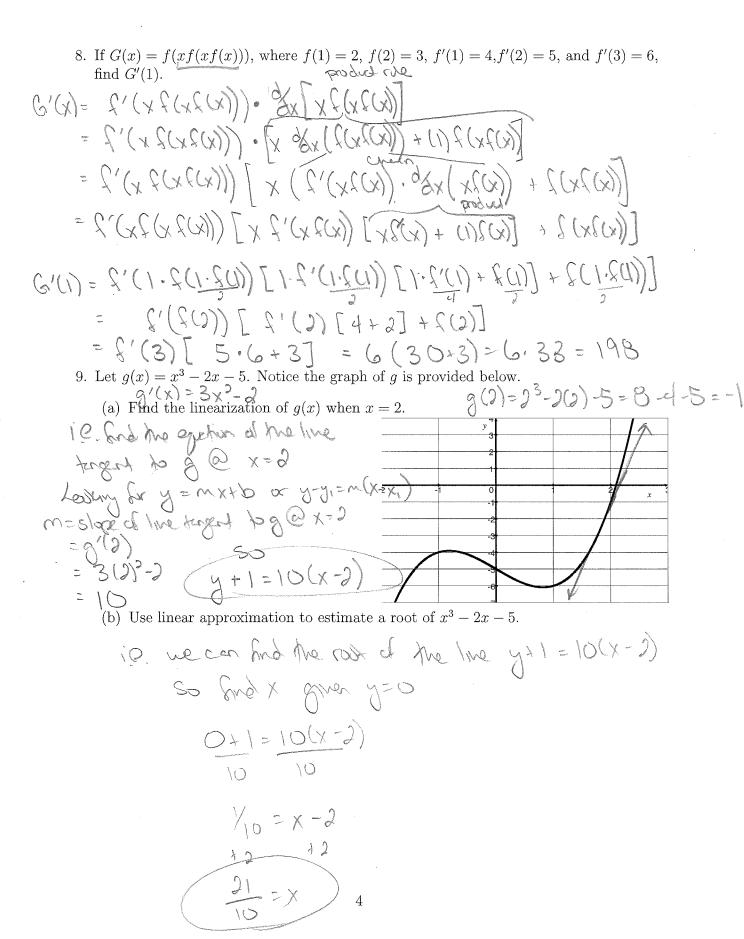
$$f'(u) = du$$

$$y' = f'(g(x))g'(x) = f'(sinx) \cdot cosx$$

$$= dsinx \cdot cosx$$

 $y' = f'(g(x))g'(x) = f'(o sin(x^2))g'(x)$   $= cos(e sin(x^2)) \cdot e sin(x^2) \cdot dx$   $= cos(x^2) \cdot dx$ 8(w)=e" (a(x)) (x) = ((2) (x), (m) (x), 3x (cos(x)).2x

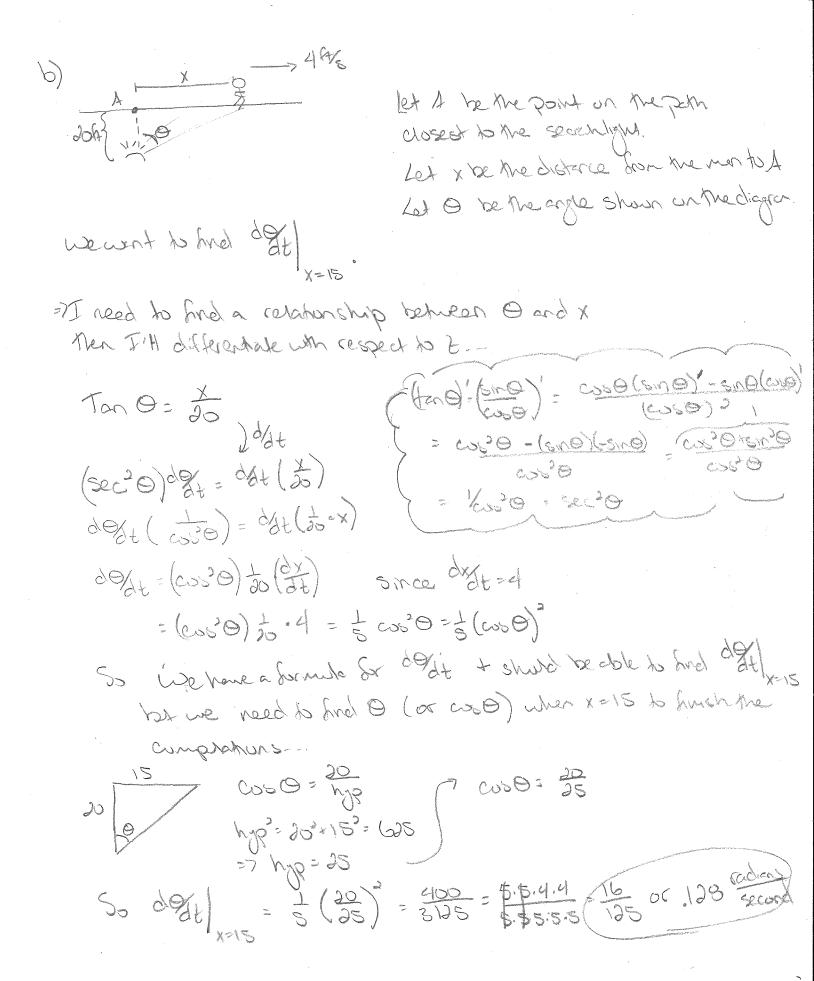
S (g(xi) /



- 9. [5] Choose *ONE* of the following. Clearly identify which of the two you are answering and what work you want to be considered for credit.

  No, doing both questions will not earn you extra credit.
  - (a) (§3.9 #21) [5] Ryan and Stella were being chased by a pack of zombies. At point P they decided to split up and Stella ran south at 12 ft/s. Ryan waited for ten seconds to try to draw most of the zombies towards him and then started to run east at 15 ft/s. One minute later the two of them are still alive and running in their respective directions. At what rate are Ryan and Stella moving apart at this instant?
  - (b) A man walks along a straight path at a speed of 4ft/s. A searchlight is located on the ground 20 ft from the path and is kept focused on the man. At what rate is the searchlight rotating when the man is 15ft from the point on the path closest to the searchlight?

where x = distance Ryon cons at threet
y = distance Stella runs at threet
d = distance seekeen cyant stella was 1 = 717 x=1594.60x=900x



- 10. [5] Choose *ONE* of the following. Clearly identify which of the two you are answering and what work you want to be considered for credit.

  No, doing both questions will not earn you extra credit.
  - (a) (Story Problem Worksheet #10) If a current i passes through a resistor with resistance r, Ohm's Law states that the voltage drop is v=ri. Assume that voltage remains a constant 20 volts. An unreliable resistor claims a resistance of 10 ohms but may be off by up to 1.5 ohms. Use the linear approximation to approximate the error when calculating i.
  - (b) (§3.10) #35) The circumference of a sphere was measured to be 84cm with a possible error of 0.5cm. Use linear approximation to find and upper bound and lower bound for the surface areas of this sphere.

b) I'd like to bird a tounda coloting circularence it a sphere to The sifuce area. Then I'll use of live largest to the graph of This famula to kid my yess above bounds Recall: Let The the radius of a sphere, Che acomferce, and S me sifuce ones. Then ord S=410 C= 2000 => = 4T(2T) = 4+C2 = C2 Finding the equation of the line tengent to the graph when C=84.

Lessling for y=mxro

Thinding S'

S' (C') = &(F') = &(FC')

To graph Swhen C=84

= Less (C') = 2.C'

= Less (C') = 2.C' 84 The live prises Mrs (84, 84) or (84, 7056) & (84, 2247.134) So 2247.134 = 53,503 (84) xb => b= -2247.118 Darked live equation is: x=53.503x-20217.119 An upper bound occurs is C=84+.5 =84.5 So the upper bound of S 253.503. (84.5) -22-17.118 = 2273 A lower bound occurs if C=84-.5=83.5

So the laver bound of 5 = 53.503(83.5)-2247.119 = 2220.3834

well went bexomine I as a function of &

to appositivate the error we'll use a linear approximation of

The Suchan I = 3%

ic the live trangent to I=29/2
when Z=10.

where y is I and X, & & (x-x.)

m = slope of line target

4 I 3/2 wer 8/10

I, = 90(-1)5-3 pl bonacy6

The live pusses thro (10, 13)= (10,2)

=> P=8+8=4

4-2= 5x+2

式=一省RY4

R could be anywhere

behiller

10-1,5=8,5 or 10+1,5=11,5

=> The goponinok: I values
uple thus eagle from

-8(8.5)+4 to 3(1.5)+4

belon 2.3 how 1.7

II Rus exact I would

De 30 = 2

Thus an appear bunder

ion the error is

Worning: The graph suggests
That De are underestimating

Ne existy