$$\lim_{x \to \pm \infty} f(x)$$

1. Find the positive horizontal asymptote(s) if they exist for each of the following:

$$\frac{x+2}{6x-4} \qquad \qquad \frac{3x^2-x-2}{5x^2+4x+1}$$

$$\frac{x^2 - x}{3x - 5}$$

$$\frac{x^2 + x}{3 - x} \qquad \qquad \frac{x - 2}{x^2 + 1}$$

Check your answers by reading Examples 3, 10, 4, 11 & problem #17 from §2.6.

Derivatives

y₄

3 2 1

0

-1 -2

-3

-4

1

2

x⁵

4

3

2. Let $f(x) = \frac{1}{x}$.

(a) Find f'(2).

(b) Find the equation of the line that is tangent to f at x = 2.

(c) Draw the graph of f and your line and verify your results.

3. Recall that average velocity is $\frac{\text{total distance}}{\text{time it took}}$. What do you think instantaneous velocity is?

-3

-4

-2

-1

4. If a grapefruit was dropped from a building, it's distance from where it was dropped varies with time by the equation $-4.9t^2$. Use your answer from (3) (or look at §2.7) to find the instantaneous speed of the grapefruit one second after its release. *Hint: we've already done this computation today.*