NAME: This is a sample exam to be used for practice only. This is not a template for the exam that will be given in class. Many of the questions on the exam will look quite different than those appearing here.

1. TRUE/FALSE: Circle T in each of the following cases if the statement is always true. Otherwise, circle F.

Let x and y be positive numbers.

$$T (\widehat{F}) x^2 x^3 = x^6$$

$$\widehat{F} x^2 x^3 = x^6 \qquad \chi^2 \chi^3 : (\chi \chi) (\chi \chi \chi) = \chi^5$$

T (F)
$$\log(x+y) = \log(x) \cdot \log(y)$$

T (F)
$$\log(x+y) = \log(x) \cdot \log(y)$$
 $\log(x,y) = \log(x+\log y)$ Let $\chi = 10 = y$ then

T (F) $\log(x+y) = \log(x) \cdot \log(y)$ $\log(x,y) = \log(x+\log y)$ $\log(x+y) = \log(20)$

T) F $\log(\frac{x}{y}) = \log(x) - \log(y)$

$$(1) F \log(\frac{x}{y}) = \log(x) - \log(x)$$

$$T(\hat{F}) \frac{\log x}{\log y} = \frac{x}{y}$$

$$T \quad \widehat{\mathbb{F}} \quad \log_2 5x^7 = 7\log_2 5x \setminus_{\mathbb{C}}$$

T (F)
$$\log_2 5x^7 = 7\log_2 5x \log_2 5x^7 = \log_2 5 + \log_2 5 + 7 \log_2 x$$

T F
$$\log(\log(10)) = 0$$
. $\log(\log(10) = \log(1) = 0$
T F) For all numbers $z, \sqrt{z^2} = z$ Let $z = -2$ then $\sqrt{(z)^2} = 2 \neq -2$

LONG ANSWERS: Show all your work and circle you final answer. Correct answers will not get credit without supporting work.

2. Given
$$-x = \frac{2xy}{2y-1}$$
, solve for y .

$$-x = \frac{2xy}{2y^{4}} \cdot 2y^{-1}$$

3. [2] Define the rule of the function log.

4. [4] Assume b, x,y > 0, simplify the following:

$$\frac{(b^{x})^{x-1}}{b^{-x}} \quad \text{where} \quad (b^{a})^{c} = b^{ac}$$

$$\frac{(b^{x})^{x-1}}{b^{-x}} = \frac{b^{x}(x-1)}{b^{-x}}$$

$$= \begin{cases} x^2 - x - (-x) \\ x^2 - x + x \end{cases}$$

$$2 - \log_5(25z)$$

$$\frac{\sqrt[3]{x^{2}(y^{2})^{\frac{3}{2}}}}{x^{\frac{2}{3}}y^{2}} = \frac{\sqrt{2}\sqrt{3}}{\sqrt{3}} \sqrt{3}$$

$$= \sqrt{2}\sqrt{3}$$

$$= \sqrt{$$

$$\log_2 \frac{1}{4} + 2$$

5. [3] Find
$$x$$
 in the following:

$$2^{4x-1} = 3^{1-x}$$

$$\ln 3^{1-x} = \ln 3^{1-x}$$

$$(4x-1)\ln 3 = (1-x)\ln 3$$

$$4x\ln 3 - \ln 3 - x\ln 3$$

$$4x\ln 3 + x\ln 3 = \ln 3 + \ln 3$$

$$x = \frac{\ln 3 + \ln 3}{\ln 3 + \ln 3}$$

$$x = \frac{\ln 3 + \ln 3}{\ln 3 + \ln 3}$$
6. Find a formula for the inverse function f^{-1} of the indicated function f .

$$ln5^* = ln2$$
 $x ln5 = ln2$

 $5^x = 2$

$$x = \frac{\ln 2}{\ln 5}$$

$$f(x) = 4x^{\frac{3}{7}} - 1$$

$$X = 4y^{\frac{3}{7}} - 1$$

$$X + 1 = 4y^{\frac{3}{7}}$$

$$\frac{X+1}{4} = \frac{3}{7}$$

$$f(x) = 3 \cdot 2^x + 4$$

$$x = 3.23 + 4$$

 $x - 4 = 3.23$
 $x - 4 = 23$
 $(x - 4) = 23$
 $(x - 4) = 23$

7. Write the given expression as a single logarithm.

$$2\ln 2x - 3(\ln x^2 + \ln x)$$

$$2\ln 3x - 3(\ln x^{2} \cdot x)$$

 $2\ln 3x - 3(\ln x^{2} \cdot x)$
 $2\ln (3x)^{2} - \ln (x^{3})^{3}$
 $2\ln (4x^{2}) - \ln x^{9}$
 $2\ln (4x^{2})$
 $2\ln (4x^{2})$

$$3 - \log_6(36y)$$

$$\log(x-16) = 2 - \log(x-1) + \log(x-1) + \log(x-1)$$

61

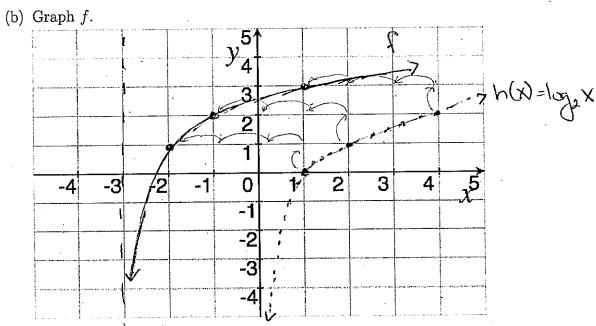
9. Let
$$h(x) = \log_2 x$$
 and $f(x) = \log_2(x+3) + 1$.

$$(3^{2})^{x} - 3 \cdot 3^{x} = 10$$
 $10^{4} + 3 \cdot 3^{x} = 10$
 $3^{2x} - 3$

 $4^x - 3 * 2^x = 10$

Let
$$h(x) = \log_2 x$$
 and $f(x) = \log_2(x+3) + 1$.

(a) List the transformations needed to transform the graph of h to the graph of f .



(c) Find the inverse function to
$$f$$
.

- 10. A sound with intensity x has $10 \log \frac{x}{I_0}$ decibels, where $I_0 = 10^{-12}$ watts per square meter (W/m²).
 - (a) France passed a law limiting iPods and other MP3 players to a maximum possible volume of 100 decibels. Find the maximum intensity (in W/m^2) an iPod is legally

allowed to output in France. Max de cross = $100 = 10\log X$ $= 100 = 10\log X$ $= 100\log X$ we want to solve for x .-

(b) Normal conversation has a sound level of about 65 decibels. How many times intense than normal conversation is the sound an iPod operating at the French maximum of 100 decibels?

Let It be the intrody of a convergation and Ip the intrody of an iPad at max we want bolived? so that I to find I we use $|S_0| = |D|^2$ $|S_0| = |S_0| = |S$

11. Find a cubic polynomial whose graph passes through the points (-2,0), (-1,5), and (1,0) and has a root at 6.

Note -2 is a rost => (x-2) is factor 1 is a rook => (x-1) is lacker 6 is a root of (x-6) is sucher

=> a = 5/4 (55 4 = 5/4 (x+2)(x-1)(x

12. Let $m(x) = x^3 + x^2 - \frac{39}{4}x + 9$ and n(x) = x + 4. Use long division to find D(x) and R(x) so that $\frac{m(x)}{n(x)} = D(x) + \frac{R(x)}{n(x)}$

X+4/X3+X-394 X+94 700

