High-Performance Scientific Computing

Instructor: Randy LeVeque TA: Grady Lemoine

Applied Mathematics 483/583, Spring 2011 http://www.amath.washington.edu/~rjl/am583



Roadrunner (Los Alamos) 122,400 cores

"World's fastest computers" http://top500.org



Jaguar (Oak Ridge) 224,162 cores

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Outline of today's lecture

- · Goals of this course, strategy for getting there
- Mechanics of homeworks
- Computer/software requirements
- Brief overview of computational science and challenges

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Overview

High Performance Computing (HPC) generally means heavy-duty computing on clusters or supercomputers with 100s to million(s) of cores.

Our focus is more modest, but we will cover much background material that is:

- Essential to know if you eventually want to do HPC
- Extremely useful for any scientific computing project, even on a laptop.

Focus on scientific computing as opposed to other computationally demanding domains, for which somewhat different tools might be best.

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Focus and Topics

Efficiently using single processor and multi-core computers

- Basic computer architecture, e.g. floating point arithmetic, cache hierarchies, pipelining
- Using Unix (or Linux, Mac OS X)
- Language issues, e.g. compiled vs. interpreted, object oriented, etc.
- Specific languages: Python, Fortran 90/95
- Parallel computing with OpenMP, MPI, IPython

Efficient programming as well as minimizing run time

- Version control: Mercurial (hg),
- · Makefiles, Python scripting,
- Debuggers

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Strategy

So much material, so little time....

- Concentrate on basics, simple motivating examples.
- Get enough hands-on experience to be comfortable experimenting further and learning much more on your
- Learn what's out there to help select what's best for your
- · Teach many things "by example" as we go along.

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Lecture notes

- html and pdf versions at (green = link in pdf file) http://www.amath.washington.edu/~rjl/am583
- · Written using Sphinx: Python-based system for writing documentation. Learn by example!!
- · Source for each file can be seen by clicking on "Show Source" on right-hand menu.
- Source files are in class hg repository. You can clone the repository and run Sphinx yourself to make a local version.
 - \$ hg clone http://bitbucket.org/.../uwamath583s11 \$ cd uwamath583s11/sphinx \$ make html \$ firefox _build/html/index.html

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Lecture slides

Slides from lectures will be linked from the Slides section of the class notes.

Generally in 3 forms, including one with space for taking notes.

With luck they will be posted at least 2 hours before class if you want to print and bring along.

Note: Slides will contain things not in the notes, lectures will also include hands-on demos not on the slides.

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Prerequisites

Some programming experience in some language, e.g., Matlab, C, Java.

You should be comfortable:

- · editing a file containing a program and executing it,
- using basic structures like loops, if-then-else, input-output,
- · writing subroutines or functions in some language

You are not expected to know Python or Fortran.

Some basic knowledge of linear algebra, e.g.:

- what vectors and matrices are and how to multiply them
- How to go about solving a linear system of equations

Some comfort level for learning new sofware and willingness to dive in to lots of new things.

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Homeworks

There will be 6 homeworks, plus a take-home final "exam".

Electronic submission: via Mercurial (in order to get experience using Mercurial!)

Homework assignments will be in the notes.

Main goal: introduce many topics and get some hands-on experience with each.

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Homework #1

Homework #1 is in the notes.

Tasks:

- Make sure you have a computer that you can use with
 - Unix (e.g. Linux of Mac OSX),
 - Python 2.5 or higer,
 - Mercurial

See next slide.

- Use Mercurial (hg) to clone the class repository and set up your own repository.
- Copy a Python script from one to the other and run it, putting the output in a second file.
- · Commit these files and push them to your repository for us to see.

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Computer/Software requirements

You will need access to a computer with a number of things on it, see the section of the notes on Downloading and Installing Software.

Note: Unix is often required for scientific computing.

Windows: Many tools we'll use can be used with Windows, but learning Unix is part of this class.

Options:

- Install everything you'll need on your own computer,
- Install VirtualBox and use the Virtual Machine (VM) created for this class.
- Use a Linux machine in the Applied Mathematics department (via ssh).

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TA and Office Hours

TA: Grady Lemoine

See the Class Catalyst Page for contact info, updated hours.

Office hours in Guggenheim 406

Monday, Tuesday, Friday 1:30 - 2:30

There is also a Discussion Board on the Class Catalyst Page, feel free to post (and answer!) questions about getting things to work.

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Survey

Please take the survey found on the Class Catalyst Page to let us know about your background and computing plans.

As soon as possible.

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Computational Science (and Engineering)

Often called the third pillar of science, complementing the traditional pillars of theory and experiment.

Direct numerical simulation of complex physics / biology / chemistry is possible.

Typically requires solving very large systems of mathematical equations.

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Computational Science (and Engineering)

Unknowns represent values of some physical quantities, e.g.,

- (x, y, z) locations and velocities of individual atoms in a molecular dynamics simulation,
- (x, y, z) locations and velocities of individual stars in a cosmology simulation, e.g. galaxy formation.
- Density, pressure, velocities of a fluid at billions of points in a fluid dynamics simulation,
- · Stress, strain, velocity of a solid at billions of points in a solid mechanics simulation.

Note: $1000 \times 1000 \times 1000$ grid has 1 billion grid points.

Need 8 gigabytes to store one variable at all grid points.

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Computational Science and Engineering

A few examples of large scale problems for motivation.

Currently, that often means Tera-scale or Peta-scale.

Next comes Exa-scale.

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How fast are computers?

Kilo = thousand (10^3) Mega = million (10^6) = billion (10^9) Giga = trillion (10^{12}) Tera Peta $=10^{15}$

Exa $=10^{18}$

Processor speeds usually measured in Gigahertz these days.

Hertz means "machine cycles per second".

One operation may take a few cycles.

So a 1 GHz processor can do

> 100,000,000 operations per second.

Exascale is a billion times more than Gigascale. (More speed and/or data.)

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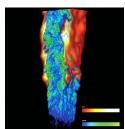
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Combustion

Goal: Developing more fuel efficient and cleaner combustion processes for petroleum and alternative fuels.

Sample computation at Oak Ridge National Laboratory:



Ethylene combustion (simple!)

More than 1 billion grid points, $\Delta x = \Delta y = \Delta z = 15$ microns

4.5 million processor hours on

Jaguar's 31,000 cores

Generated > 120 terabytes of data

http://www.scidacreview.org/0902/html/news1.html

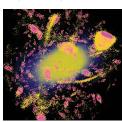
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Milky Way's dark matter halo

Goal: Understand nature of the universe.

Sample computation at Oak Ridge National Laboratory:



1.1 billion particles of dark matter, simulated for 13.7 billion years

> 1 million processor hours on Jaguar (3000 cores)

http://www.scidacreview.org/0901/html/bt.html

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How long does it take to solve a linear system?

Solving an $n \times n$ linear system Ax = b requires $\approx \frac{1}{3}n^3$ flops. (Using Gauss elimination for a dense matrix.)

On a 100 MFlops system:

flops time n10 3.3×10^2 0.0000033 seconds 100 3.3×10^{5} 0.0033 seconds 3.3×10^{8} 1000 3.33 seconds 10000 3.3×10^{11} 333 seconds = 5.5 minutes100000 3.3×10^{14} 333333 seconds = 92.5 hours 1000000 3.3×10^{17} 92500 hours = 105 years

Assuming data transfer is not a problem!

It is a problem: It's often the bottleneck, not compute speed! $10^6 \times 10^6$ matrix has 10^{12} elements \implies 8 terabytes.

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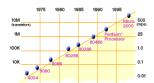
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Moore's Law

Technology Trends: Microprocessor Capacity



2X transistors/Chip Every 1.5 years Called "Moore's Law'

Microprocessors have become smaller, denser, and more powerful.



Gordon Moore (co-founder of Intel) predicted in 1965 that the transistor density of semiconductor chips would double roughly every 18 months.

CS267-Lecture 1

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Increasing speed

Moore's Law: Processor speed doubles every 18 months.

 \implies factor of 1024 in 15 years.

Going forward: Number of cores doubles every 18 months.



Top: Total computing power of top 500 com-

Middle: #1 computer

Bottom: #500 computer

http://www.top500.org

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More Limits: How fast can a serial computer be?

1 Tflop/s, 1 r = 0.3Tbyte sequential machine

- Consider the 1 Tflop/s sequential machine:
 - Data must travel some distance, r, to get from memory to CPU.
 - To get 1 data element per cycle, this means 10^{12} times per second at the speed of light, $c=3x10^8\ m/s.$ Thus $r< c/10^{12}=0.3\ mm.$
- Now put 1 Tbyte of storage in a 0.3 mm x 0.3 mm area:
 - Each bit occupies about 1 square Angstrom, or the size of a small atom.
- No choice but parallelism 01/17/2007 CS267-Lecture 1

Slide Source: Kathy Yellick

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Take away messages

- Massively parallel machines are needed for Petascale or Exascale (millions or billions of cores).
- But also, all machines going to be multicore soon, with lots of cores.
- If you want to continue seeing benefiting from hardware improvements, you need to know something about parallel computing.

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