

**Test 1- ME 374**  
Winter 1931  
(Open book and notes).

1) (50%)

a) Consider the system in Figure 1 when  $k_1=100$ ,  $M=1$ ,  $f(t)=\sin(9.9t)$ .

Using the transfer function that relates  $x$  to  $f$  determine the steady state amplitude of  $x(t)$

b) If a second mass and spring are added to the system as shown in Figure 2 the equation of motions become

$$M\ddot{x} + k_1x + k_2(x - y) = f(t)$$

$$m\ddot{y} + k_2(y - x) = 0$$

Show the pole(s) and zeros(s) of the transfer function  $H(s)=X/F$  in the complex plane. Since there is no damping the poles are all purely imaginary. What should  $m/k$  be in order for the steady state solution  $x_p(t) = 0$ .

Figure 1

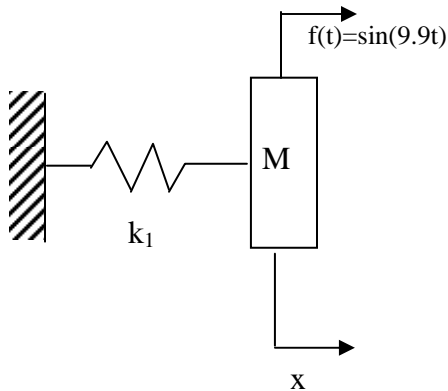
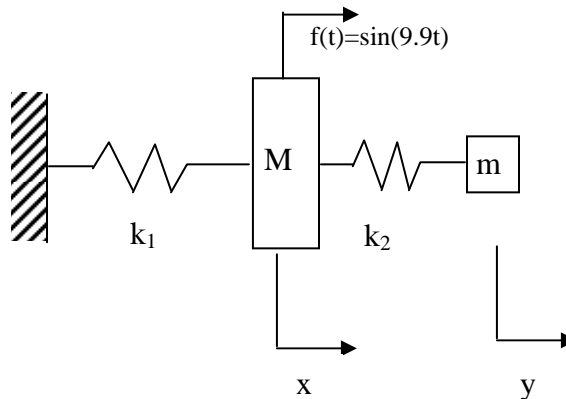


Figure 2



2) (50%) Consider the following state equation

$$\frac{d}{dt} \begin{pmatrix} v \\ f \end{pmatrix} = \begin{bmatrix} 4 & 2 \\ 3 & 5 \end{bmatrix} \begin{pmatrix} v \\ f \end{pmatrix}$$

with

$$\begin{pmatrix} v \\ f \end{pmatrix} = \begin{pmatrix} 2 \\ 1 \end{pmatrix} \text{ at } t = 0$$

Using the state transition matrix obtain  $f$  as a function of time.