### Inference on Treatment Effect Modification by Marker Response in a Baseline Surrogate Measure Three-Phase Sampling Design

#### Michal Juraska<sup>1</sup>

Joint work with: Peter B. Gilbert<sup>1,2</sup> and Ying Huang<sup>1,2</sup>

<sup>1</sup> Vaccine and Infectious Disease Division, Fred Hutchinson Cancer Research Center <sup>2</sup> Department of Biostatistics, University of Washington

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### Motivation: two Phase 3 Dengvaxia trials

- Two randomized placebo-controlled Phase 3 dengue vaccine trials in 31144 children
- Harmonized trial designs
- Vaccine/placebo administered at months 0, 6, and 12
- Primary clinical endpoint: symptomatic virologically confirmed dengue (VCD) between months 13 and 25
- Asian trial:  $\widehat{VE} = 56.5\%$  (95% CI, 43.8 to 66.4)
- Latin American trial:  $\widehat{VE} = 60.8\%$  (95% CI, 52.0 to 68.0)

#### Does average neutralizing antibody titer, measured in the vaccine group at month 13, modify VE(13–25) against VCD in participants free of VCD through month 13?

### Motivation: two Phase 3 Dengvaxia trials

Three-phase case-cohort sampling design

- Baseline serum samples collected from a random sample (subcohort S) of
  - $\blacktriangleright \approx 10\%$  of all participants in the Asian trial
  - $\blacktriangleright~\approx 20\%$  of all participants in the Latin American trial
- Month 13 serum samples collected from all participants

### ₩

- Phase 1: baseline covariates (e.g., demographics) in all participants
- Phase 2: biomarker S (NAb titer) at month 13 in a subset of subcohort S and in all post-month 13 VCD cases
- Phase 3: biomarker's baseline value S<sub>b</sub> only in a subset of subcohort S

### Motivation: two Phase 3 Dengvaxia trials

- S<sub>b</sub> and S highly correlated, making S<sub>b</sub> ideal as a baseline immunogenicity predictor<sup>1</sup> (baseline surrogate measure<sup>2</sup>)
- All alternative EML and PS methods<sup>3</sup> require that S<sub>b</sub> be measured from all vaccine recipients with S measured
- ⇒ These methods would discard data from 80–90% of VCD endpoint cases in the vaccine group!

<sup>1</sup> Follmann (2006); Gilbert and Hudgens (2008)

<sup>2</sup> Gabriel and Gilbert (2014)

<sup>3</sup> Gilbert and Hudgens (2008); Huang and Gilbert (2011); Huang, Gilbert, and Wolfson (2013); Gabriel and Gilbert (2014); Huang (2017)

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### Notation

- Z treatment indicator
- $\boldsymbol{X} = (X_1, \dots, X_k)$  baseline covariate vector
- S discrete or continuous univariate biomarker at fixed time τ after randomization
- S<sub>b</sub> baseline value of the biomarker
- $\epsilon$  and  $\delta$  indicators of measured S and  $S_b$
- Y indicator of clinical endpoint after  $\tau$
- Y<sup>τ</sup> indicator of clinical endpoint at or before τ
- Y<sup>τ</sup>(Z), ε(Z), S(Z), Y(Z) potential outcomes of Y<sup>τ</sup>, ε, S, Y under Z

To evaluate S(1) as a modifier of treatment effect on Y, S needs to be measured prior to Y.

 $\Rightarrow$  Analysis restricted to participants with  $Y^{\tau} = 0$ .

### Three-phase case-cohort sampling design

Phase 1: Z, X,  $Y^{\tau}$ , Y measured in all randomized participants Phase 2 (classic case-cohort design [Prentice, 1986]):

- Bernoulli sample S at baseline
- S measured at \(\tau\) in
  - a subset of S with  $Y^{\tau} = 0$ , and
  - all (or almost all) cases (Y = 1) with  $Y^{\tau} = 0$

Phase 3:

•  $S_b$  measured at baseline in a subset of S with  $Y^{\tau} = 0$ 

Consequence:  $S_b$  measured only in those cases with  $Y^{\tau} = 0$ that were sampled into S

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### Identifiability assumptions

- 1.  $(Z_i, X_i, \delta_i, \delta_i S_{b,i}, Y_i^{\tau}(0), Y_i^{\tau}(1), \epsilon_i(0), \epsilon_i(0)S_i(0), \epsilon_i(1), \epsilon_i(1)S_i(1), Y_i(0), Y_i(1)), i = 1, ..., n, i.i.d.$  with no drop-out
- 2. Standard identifiability assumptions<sup>†</sup>
  - a. Stable unit treatment value assumption (SUTVA) and consistency:

 $(Y_i^{\tau}(0), Y_i^{\tau}(1), \epsilon_i(0), \epsilon_i(0)S_i(0), \epsilon_i(1), \epsilon_i(1)S_i(1), Y_i(0), Y_i(1)) \\ \perp Z_j, j \neq i, \text{ and } (V_i(Z_i), \epsilon_i(Z_i)S_i(Z_i), Y_i(Z_i)) = (V_i, \epsilon_iS_i, Y_i)$ 

b. Ignorable treatment assignment:

 $Z_i \perp \\ (\delta_i, \delta_i S_{b,i}, Y_i^{\tau}(0), Y_i^{\tau}(1), \epsilon_i(0), \epsilon_i(0) S_i(0), \epsilon_i(1), \epsilon_i(1) S_i(1), \\ Y_i(0), Y_i(1)) \mid \mathbf{X}_i$ 

c. Equal early clinical risk:

 $P\{Y_i^{\tau}(0) = Y_i^{\tau}(1)\} = 1^*$ 

\* Henceforth all unconditional and conditional probabilities of Y(z) = 1 implicitly condition on  $Y^{\tau}(1) = Y^{\tau}(0) = 0$ .

<sup>†</sup> Gilbert and Hudgens (2008); Huang and Gilbert (2011); Huang, Gilbert, and Wolfson (2013); Gabriel and Gilbert (2014); Huang (2017)

### Modeling assumptions

3.  $P{Y(z) = 1 | X, S(z)}$  follows a GLM for z = 0, 1

- For z = 0, it replaces "placebo structural risk" assumption of all EML and PS methods<sup>†</sup> that P{Y(0) = 1 | X, S(1)} follows a GLM
- 4. Conditional independence:  $P\{Y(0) = 1 | X, S(0), S(1)\} = P\{Y(0) = 1 | X, S(0)\}$
- 5. Time constancy:

$$f(s_1|X = X, S(0) = s_0) = \tilde{f}(s_1|X = X, S_b = s_0)$$
 for all  $(s_1, X, s_0)$ 

<sup>†</sup> Gilbert and Hudgens (2008); Huang and Gilbert (2011); Huang, Gilbert, and Wolfson (2013); Gabriel and Gilbert (2014); Huang (2017)

### Estimand of interest: $mCEP(s_1)$

- ► Overall causal treatment effect on Y CE = h(P{Y(1) = 1}, P{Y(0) = 1})
- h(x, y) a known contrast function
- ► Marginal causal effect predictiveness curve<sup>\*,†</sup> mCEP(s<sub>1</sub>) = h(P{Y(1) = 1|S(1) = s<sub>1</sub>}, P{Y(0) = 1|S(1) = s<sub>1</sub>})

- ► Principal stratification estimand<sup>‡</sup> ⇒ measures causal treatment effect on Y for a subgroup with S(1) = s<sub>1</sub>
- Examples:

h(x, y) = 1 - x/y multiplicative risk reduction h(x, y) = y - x attributable risk

- \* Gilbert and Hudgens (2008)
- <sup>†</sup> If *S* is continuous, this definition abuses notation for simplicity of exposition.
- <sup>‡</sup> Frangakis and Rubin (2002)

### Estimation of mCEP(s<sub>1</sub>)

- $p_z(s_1) := P\{Y(z) = 1 | S(1) = s_1\}$  for z = 0, 1
- mCEP $(s_1) = h\{p_1(s_1), p_0(s_1)\}$
- Estimate p<sub>1</sub>(s<sub>1</sub>) via the specified GLM, accounting for case-cohort sampling of S
  - ▶ E.g., using the tps function in the R osDesign package

### Estimation of mCEP(s<sub>1</sub>)

$$p_0(s_1) = \int P\{Y(0) = 1 | \mathbf{X} = \mathbf{x}, S(0) = s_0\} \times \\ \times \frac{f(s_1|s_0, \mathbf{x})g(s_0|\mathbf{x})r(\mathbf{x})}{m(s_1)} d^{k+1}(s_0, \mathbf{x}),$$

 $m(s_1) = \int f(s_1|s_0, \mathbf{x}) g(s_0|\mathbf{x}) r(\mathbf{x}) d^{k+1}(s_0, \mathbf{x})$ 

- ► Estimate  $P{Y(0) = 1 | \textbf{X} = \textbf{x}, S(0) = s_0}$  via the specified GLM, accounting for case-cohort sampling of *S*
- ► Estimate f(s<sub>1</sub>|S<sub>0</sub> = s<sub>0</sub>, X = x) by estimating f̃(s<sub>1</sub>|S<sub>b</sub> = s<sub>0</sub>, X = x) via nonparametric kernel smoothing, accounting for the three-phase sampling design
  - E.g., using the npcdensbw, npcdens, npudensbw, npudens functions in the R np package

• Estimate  $g(s_0|\mathbf{x})$  and  $r(\mathbf{x})$  analogously

Bootstrap procedures designed to construct

- 1. pointwise Wald-type CI for  $mCEP(s_1)$  for a given  $s_1$
- 2. simultaneous Wald-type CI for  $\{mCEP(s_1), s_1 \in S\}$ , for an arbitrary subset S of the support of S(1)
  - Cases and controls sampled separately in each bootstrap sample

### Simultaneous Wald-type CI for $\{mCEP(s_1), s_1 \in \mathbb{S}\}$

►  $\eta(s_1) := \eta\{\text{mCEP}(s_1)\}$  a "symmetrizing" transformation ►  $h(x, y) = 1 - x/y \Rightarrow n\{h(x, y)\} = \log\{1 - h(x, y)\}$ 

• 
$$h(x,y) = 1 - x/y \Rightarrow \eta\{h(x,y)\} = \log\{1 - h(x,y)\}$$

$$\widehat{\eta}(\boldsymbol{s}_1) = \eta\{\mathrm{mCEP}(\boldsymbol{s}_1)\}$$

- $c^*_{\alpha}$  empirical quantile of  $U^{(b)}$ , b = 1, ..., B, at probability  $1 \alpha$
- $(1 \alpha) \times 100\%$  CI as  $\eta^{-1}(\cdot)$  transformation of

$$(I^{\eta}_{\alpha}(\boldsymbol{s}_{1}),\boldsymbol{u}^{\eta}_{\alpha}(\boldsymbol{s}_{1})) = \widehat{\eta}(\boldsymbol{s}_{1}) \mp \boldsymbol{c}^{*}_{\alpha} \boldsymbol{S}\boldsymbol{E}^{*}\{\widehat{\eta}(\boldsymbol{s}_{1})\}.$$

Hypothesis tests via simultaneous estimation method of Roy and Bose (1953) for

- 1.  $H_0^1$  : mCEP( $s_1$ )  $\equiv CE$  for all  $s_1 \in \mathbb{S}$
- 2.  $H_0^2$  : mCEP( $s_1$ )  $\equiv c$  for all  $s_1 \in S_1 \subseteq S$  and a known constant  $c \in \mathbb{R}$
- 3.  $H_0^3$  : mCEP<sub>1</sub>( $s_1$ ) = mCEP<sub>2</sub>( $s_1$ ) for all  $s_1 \in \mathbb{S}_1 \subseteq \mathbb{S}$ , where mCEP<sub>1</sub> and mCEP<sub>2</sub> are each associated with either a different biomarker (measured in the same units) or a different endpoint or both
- H<sub>0</sub><sup>4</sup> : mCEP(s<sub>1</sub>|X = 1) = mCEP(s<sub>1</sub>|X = 0) for all s<sub>1</sub> ∈ S<sub>1</sub> ⊆ S, where X is a baseline dichotomous phase 1 covariate of interest included in X

### Tests of $H_0^1$ and $H_0^2$

 $\begin{array}{l} H_0^1 : \operatorname{mCEP}(s_1) \equiv \textit{CE} \text{ for all } s_1 \in \mathbb{S} \\ H_0^2 : \operatorname{mCEP}(s_1) \equiv \textit{c} \text{ for all } s_1 \in \mathbb{S}_1 \subseteq \mathbb{S} \text{ and a known constant } \textit{c} \in \mathbb{R} \end{array}$ 

▶ Regions of rejection of  $H_0^1$  and  $H_0^2$  at significance level  $\alpha$ :

$$\begin{split} U_1 &:= \sup_{s_1 \in \mathbb{S}} \left| \widehat{\eta}(s_1) - \eta(\widehat{CE}) \right| / SE^* \{ \widehat{\eta}(s_1) \} > c_{1\alpha}^* \\ U_2 &:= \sup_{s_1 \in \mathbb{S}_1} \left| \widehat{\eta}(s_1) - \eta(c) \right| / SE^* \{ \widehat{\eta}(s_1) \} > c_{2\alpha}^* \end{split}$$

- $c_{1\alpha}^*$  and  $c_{2\alpha}^*$  empirical quantiles of  $U_{\eta}^{(b)}(\mathbb{S}, \widehat{CE})$  and  $U_{\eta}^{(b)}(\mathbb{S}_1, c), b = 1, \dots, B$ , at probability  $1 \alpha$
- Two-sided p-values as empirical probabilities that *U*<sup>(b)</sup><sub>η</sub>(S, *CE*) > *U*<sub>1</sub> and *U*<sup>(b)</sup><sub>η</sub>(S<sub>1</sub>, *c*) > *U*<sub>2</sub>

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## Test of $H_0^3$

 $H_0^3$ : mCEP<sub>1</sub>( $s_1$ ) = mCEP<sub>2</sub>( $s_1$ ) for all  $s_1 \in S_1 \subseteq S$ , where mCEP<sub>1</sub> and mCEP<sub>2</sub> are each associated with either a different biomarker or a different endpoint or both

$$\bullet \ \theta(\boldsymbol{s}_1) := \eta\{\mathrm{mCEP}_1(\boldsymbol{s}_1)\} - \eta\{\mathrm{mCEP}_2(\boldsymbol{s}_1)\}$$

• Region of rejection of  $H_0^3$  at significance level  $\alpha$ :

$$U_3 := \sup_{s_1 \in \mathbb{S}_1} \left| \widehat{ heta}(s_1) \right| / SE^* \{ \widehat{ heta}(s_1) \} > c^*_{3lpha}$$

- $c_{3\alpha}^*$  empirical quantile of  $U_{\theta}^{(b)}$ , b = 1, ..., B, at probability  $1 \alpha$
- Two-sided p-value as empirical probability that  $U_{\theta}^{(b)} > U_3$

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 $H_0^4$ : mCEP( $s_1|X = 1$ ) = mCEP( $s_1|X = 0$ ) for all  $s_1 \in S_1 \subseteq S$ , where X is a baseline dichotomous phase 1 covariate of interest

- Estimates of mCEP(s<sub>1</sub>) in subgroups X = 1 and X = 0 are independent
- Test of H<sup>4</sup><sub>0</sub> identical to that of H<sup>3</sup><sub>0</sub> except

$$SE^*\{\widehat{\theta}(s_1)\} = \left\{SE^{*2}\left[\eta\{\widehat{\mathrm{mCEP}}(s_1|X=1)\}\right] + SE^{*2}\left[\eta\{\widehat{\mathrm{mCEP}}(s_1|X=0)\}\right]\right\}^{1/2}$$

### Simulation setup

Three-phase case-cohort sampling design Phase 1:

N = 5000 randomized at 1:1 ratio to Z = 1 or 0 and followed for a binary Y (assumed to occur after τ at which S(Z) is measured)

Phase 2:

- Bernoulli sample S at baseline with sampling probability  $\pi = 0.1, 0.25, and 0.5$
- S(Z) measured at  $\tau$  in S and in all cases (Y = 1)

Phase 3:

► S<sub>b</sub> measured at baseline in S only, i.e., S<sub>b</sub> missing in cases not included in S

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### Simulation setup

• 
$$\begin{pmatrix} S_b \\ S(0) \\ S(1) \end{pmatrix} \sim N \begin{pmatrix} 2 \\ 2 \\ 3 \end{pmatrix}, \begin{pmatrix} 1 & 0.9 & 0.7 \\ 0.9 & 1 & 0.7 \\ 0.7 & 0.7 & 1 \end{pmatrix} \end{pmatrix},$$
  
left-censored at 1.5  
•  $P\{Y(z) = 1 | S(0) = s_0, S(1) = s_1\} =$   
 $= \Phi\{\beta_0 + \beta_1 z + \beta_2(1 - z)s_0 + \beta_3 z s_1\}, \quad z = 0, 1$   
•  $TE(s_1) := mCEP(s_1)$  defined by  $h(x, y) = 1 - x/y$ 



Three estimators for  $TE(s_1)$ :

 NP-TE: nonparametric generalized-product kernel density estimation of Hall, Racine, and Li (2004); bandwidths optimized by likelihood cross-validation

#### 2. MLE-TE: Gaussian maximum likelihood density estimation

3. PSN: pseudo-score estimation of Huang (2017) assuming  $P\{Y(z) = 1 | S(1) = s_1\} = \Phi\{\gamma_0 + \gamma_1 z + \gamma_2 s_1 + \gamma_3 s_1 z\}, z = 0, 1$ 

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## Relative bias of $\widehat{TE}(s_1)$



Results based on 10<sup>3</sup> replicated data sets

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## Mean squared error of $\widehat{TE}(s_1)$



Results based on 10<sup>3</sup> replicated data sets

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### Coverage probabilities of pointwise 95% CIs for $TE(s_1)$



Results based on 10<sup>3</sup> replicated data sets with 500 bootstrap samples drawn in each data set

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# Coverage probabilities of simultaneous 95% CI for ${TE(s_1), s_1 \in \mathbb{S}}$

$\pi$	NP-TE	MLE-TE
0.1	0.959	0.943
0.25	0.956	0.944
0.5	0.959	0.954

Results based on 10<sup>3</sup> replicated data sets with 500 bootstrap samples drawn in each data set

### Size/power of hypothesis tests

	Test of $H_0^{1a}$		Test	Test of $H_0^{2b}$		Test of H <sub>0</sub> <sup>4c</sup>	
$\pi$	Size	Power	Size	Power	Size	Power	
	NP-TE						
0.1	0.01	0.73	0.04	0.83	0.04	0.12	
0.25	0.01	0.84	0.05	0.89	0.04	0.15	
0.5	0.01	0.89	0.05	0.93	0.04	0.18	
	MLE-TE						
0.1	0.01	0.87	0.06	0.92	0.05	0.17	
0.25	0.01	0.91	0.05	0.95	0.05	0.20	
0.5	0.01	0.92	0.06	0.96	0.05	0.20	
$^{a}$ $\mu^{1}$ , TE(a) - TE for all a $\subset \mathbb{S}$							

 ${}^{a}H^{1}_{0}:\operatorname{TE}(\boldsymbol{s}_{1})\equiv \mathit{TE} ext{ for all }\boldsymbol{s}_{1}\in\mathbb{S}$ 

<sup>*b*</sup> 
$$H_0^2$$
 : TE( $s_1$ )  $\equiv 0.5$  for all  $s_1 \in \mathbb{S}$ 

<sup>c</sup>  $H_0^4$  : TE( $s_1|X = 1$ ) = TE( $s_1|X = 0$ ) for all  $s_1 \in \mathbb{S}$ 

Results based on 10<sup>3</sup> replicated data sets with 500 bootstrap samples drawn in each data set 25

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### Analysis of CYD14/CYD15 Dengvaxia trials

- Current age indication ≥ 9 years
- Trial-pooled analysis in 24,768 children aged ≥ 9 years at risk for VCD at month 13
- S = average of log<sub>10</sub> neutralizing antibody titers to 4 dengue vaccine strains at month 13

	Controls ( $Y = 0$ )	Cases $(Y = 1)$
S	2766	502
$S_b$	2759	55

 Goal: to assess modification of Dengvaxia's effect on VCD risk through month 25 by S(1)

### Analysis of CYD14/CYD15 Dengvaxia trials

▶ Two mCEP(*s*<sub>1</sub>) estimands:

- 1.  $h_1(x, y) = \log(x/y)$
- 2.  $h_2(x, y) = y x$
- 1. NP: estimate  $P\{Y(z) = 1 | X, S(z)\}, z = 0, 1$ , via IPW logistic regression models
  - X = age category ( $\leq 11 \text{ vs.} > 11 \text{ years}$ ) and country
  - Hinge model (Fong et al., 2017) for modeling the effect of S(z) using the chagptm function in the R chagpt package
- 2. PSN (Huang, 2017): estimate  $P\{Y(z) = 1 | X, S(1)\}$ , z = 0, 1, via IPW probit models with the same X and hinge model

### Analysis of CYD14/CYD15 Dengvaxia trials



### R package pssmooth on CRAN



### Summary

The proposed methods:

- Provide an alternative to PS estimation methods<sup>1</sup>, which do **not** assume:
  - $P{Y(0) = 1 | \boldsymbol{X}, S(0)}$  follows a GLM
    - PS methods instead assume P{Y(0) = 1 | X, S(1)} follows a GLM

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- $Y(0) \perp S(1) \mid \boldsymbol{X}, S(0)$
- $\triangleright S(1) \mid \boldsymbol{X}, S(0) \stackrel{d}{=} S(1) \mid \boldsymbol{X}, S_b$
- Allow flexible nonparametric kernel smoothing
- Provide formal tests of
  - $H_0^2$ : mCEP $(s_1) \equiv c$
  - $H_0^3$  : mCEP<sub>1</sub>( $s_1$ ) = mCEP<sub>2</sub>( $s_1$ )
  - $H_0^4$  : mCEP $(s_1|X = 1) = mCEP(s_1|X = 0)$

<sup>1</sup> Huang, Gilbert, and Wolfson (2013); Huang (2017)

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### **Extra Slides**



### Distributions of S(0) and S(1)

CYD14

CYD15



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#### MAJOR ARTICLE



### Neutralizing Antibody Correlates Analysis of Tetravalent Dengue Vaccine Efficacy Trials in Asia and Latin America

Zoe Moodie,<sup>1</sup> Michal Juraska,<sup>1</sup> Ying Huang,<sup>12</sup> Yingying Zhuang,<sup>2</sup> Youyi Fong,<sup>12</sup> Lindsay N. Carpp,<sup>1</sup> Steven G. Self,<sup>12</sup> Laurent Chambonneau,<sup>3</sup> Robert Small,<sup>4</sup> Nicholas Jackson,<sup>5</sup> Fernando Noriega,<sup>4</sup> and Peter B. Gilbert<sup>12</sup>

<sup>1</sup>Vaccine and Infectious Disease Division, Fred Hutchinson Cancer Research Center, Seattle, Washington, <sup>2</sup>Department of Biostatistics, University of Washington, Seattle; <sup>3</sup>Sanofi Pasteur, Marcy-L'Etoile, France; <sup>4</sup>Sanofi Pasteur, Swiftwater, Pennsylvania; <sup>4</sup>Sanofi Pasteur, Lyon, France