Discrete Mathematics
and its Applications

Ngày 18 tháng 9 năm 2011

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How many subsets can a family $\mathbb{F} \subset P(A))$ *have if any two subsets have exactly one element in common?*

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Remark

Note that if all memebers of $\mathbb{F}$ have the same size then no subset contains another subset. Does this give us a clue to the answer?