

Discrete Mathematics

Assignment RR

Moshe Rosenfeld

Hanoi 2012

moishe@u.washington.edu

Due: Tuesday (Dec 11)

1 Recurrence Relations

1.1 Telescoping

Use the telescoping technique to find the recurrence relation for the following sequences:

- 1, 3, 6, 10, 15, 21, ...
- 1, 2, 3, 5, 16, 231, ...
- Solve $a_n = \sqrt{a_{n-1} \cdot a_{n-2}}$, $a_0 = 2, a_1 = 1$. What is $\lim_{n \rightarrow \infty} a_n$.

1.2 Linear recurrence Relations

- Solve: $a_n = 2a_{n-1} - a_{n-3}$, $a_0 = 1, a_2 = 0, a_3 = 2$.
- Find the general solution to: $a_n = 4a_{n-1} - 4a_{n-2} + 3n$

1.3 Misc recurrence relations

- A domino is a 2×1 tile. In how many different ways can you arrange n dominoes to form a $2 \times n$ strip?*
- How many binary sequences $b_1 b_2 \dots b_8$ such that $\sum_{n=1}^8 b_n = 4$ and for each $1 \leq j \leq 8$ $\sum_{i=1}^j b_i \geq \frac{j}{2}$ are there?

5. * Obtain a recurrence relation for b_n , the number of binary sequences of length $2n$ containing exactly n 1's such that $\sum_{i=1}^j b_j \geq \frac{j}{2}$.
6. * Prove that for every positive integer n there is an integer m such that $(\sqrt{2} - 1)^n = \sqrt{m+1} - \sqrt{m}$
7. * Prove that $(\sqrt{170} + 13)^n$ has at least n zeros after the decimal point.*