Discrete Mathematics Notes Number theory

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1 Factoring Challenge

The following Key was intercepted during an exchange session on the internet:

 $\label{eq:Key} {\rm Key} = 514965520148166628839323406279147259515409971362330783421853637487810361\\ 0851426544234449973390985027568730853699423276912721013674109248474046130789$

I happen to posses an **oracle** that can extract square roots mod this key.

If you send me an integer, if it is a quadratic residue mod Key, I will send you its' square root mod Key.

Note that it is very easy to verify that Key is a composite number.

Your mission is to factor this integer.