

**The roles of intra-seasonal Kelvin waves and
tropical instability waves in SST variability along
equatorial Pacific in an isopycnal ocean model**

ChuanLi Jiang,* LuAnne Thompson

School of Oceanography, University of Washington, Seattle, WA

Kathryn A. Kelly

Applied Physics Laboratory, University of Washington, Seattle, WA

Meghan F. Cronin

NOAA/Pacific Marine Environmental Laboratory, Seattle, WA

December 21, 2008

*Corresponding author address: ChuanLi Jiang School of Oceanography, Box 357940, University of Washington, Seattle, WA 98195; e-mail: chuanlij@ocean.washington.edu

Abstract

1
2 The roles of intra-seasonal Kelvin waves and tropical instability waves (TIWs) in
3 the intra-seasonal and low-frequency mixed-layer temperature budget were examined
4 in an isopycnal ocean model forced by QuikSCAT winds from 2000 to 2004. Cor-
5 relations between temperature tendency and other terms of the intra-seasonal budget
6 compare well with previous results using TAO observations: the net heat flux has
7 the largest correlation in the western Pacific; and zonal advection has the largest cor-
8 relation in the central Pacific. In the central Pacific, the intra-seasonal variations in
9 zonal advection were due to both the zonal background velocity acting on the Kelvin
10 wave temperature anomaly and the Kelvin wave's anomalous velocity acting on the
11 background temperature. In the eastern Pacific, three of the four temperature budget
12 terms have comparable correlations. In particular, the vertical processes acting on
13 the shallow thermocline cause large SST anomalies in phase with the intra-seasonal
14 thermocline anomalies.

15 On intra-seasonal time scales, the influence of composite upwelling and down-
16 welling Kelvin waves cancel each other. However, because the intra-seasonal SST
17 anomalies increase to the east, a zonal gradient of SST is generated that is in phase
18 with intra-seasonal zonal velocity. Consequently, heat advection by the Kelvin waves
19 rectifies into lower frequencies in the eastern Pacific. Rectification due to TIWs was
20 also seen. The prevalence of intra-seasonal Kelvin waves and the zonal structure of
21 intra-seasonal SST from 2002 to early 2004 suggested that they might be important
22 in setting the eastern Pacific SST on interannual time scales.

23 1. Introduction

24 Previous research suggests possible connections between intra-seasonal downwelling Kelvin
25 waves driven by westerly wind bursts in the western Pacific and the SST warming in the eastern
26 Pacific on both intra-seasonal and low frequency time scales (Harrison and Schopf 1984; Harri-
27 son and Giese 1988; Giese and Harrison 1991; Kessler et al. 1995; McPhaden 1999; Kessler and
28 Kleeman 2000; Vecchi and Harrison 2000; Zhang and Gottschalck 2002; McPhaden 2002; Kut-
29 suwada and McPhaden 2002; Seo and Xue 2005). On intra-seasonal time scales, the downwelling
30 Kelvin waves can remotely affect the eastern Pacific SST by changing the zonal current structure
31 in the central and eastern equatorial Pacific (Harrison and Giese 1988; Giese and Harrison 1991;
32 Kessler et al. 1995; Vecchi and Harrison 2000), by changing the thermocline slope (Zhang 2001),
33 and by influencing the meridional advection by the tropical instability waves (TIWs) (Giese and
34 Harrison 1991). See Kessler (2005) for a review. Intra-seasonal signal can also rectify into lower
35 frequencies through nonlinearities. In the western Pacific, Kessler and Kleeman (2000) found
36 rectification in SST by the feedback between the warm pool SST and Madden-Julian Oscillation
37 (MJO). Likewise, if the intra-seasonal wave causes temperature gradient anomalies that are in
38 phase with the velocity anomalies, then advective processes can cause the anomalies to rectify
39 into lower frequencies. For instance, Jochum and Murtugudde (2004) found rectification in SST
40 from TIWs in the eastern Pacific.

41 McPhaden (2002) examined the physical processes that control the intra-seasonal SST vari-
42 ability in the equatorial Pacific at four TAO (Tropical Atmospheric-Ocean) moorings sites ($165^{\circ}E$,
43 $170^{\circ}W$, $140^{\circ}W$, and $110^{\circ}W$). McPhaden found that zonal advection dominates in the central
44 Pacific and vertical advection and entrainment dominate in the eastern Pacific. His findings pro-
45 vided an explanation for the warming and cooling events that occurred simultaneously over a

46 wide longitude range, as noted by Kessler and McPhaden (1995) during the 1991/1992 El Niño.
47 McPhaden argued that the increased importance of vertical advection and entrainment in the east-
48 ern Pacific, which leads the thermocline depth by a quarter of cycle, can cause the SST to vary
49 in phase along the equator or even to appear to propagate westward. We note that if SST varied
50 in phase perfectly with the same magnitude at all longitudes, then there would be no zonal SST
51 gradient anomalies associated with Kelvin waves and the temperature advection would not rectify
52 into lower frequencies. Likewise, if the SST anomaly was perfectly in phase with the velocity
53 anomaly, then the zonal SST gradient due to the wave would be zero exactly when the velocity
54 anomaly was maximum and, again, there would be no rectification into lower frequencies. Given
55 the complexity of the dynamics in the equatorial Pacific and the approximation and assumptions
56 invoked by the empirical analysis, it is not clear that these two cases are uniformly valid. In this
57 study we will use a numerical model to investigate the intra-seasonal variations due to Kelvin
58 waves and whether and how advection rectifies intra-seasonal variations into the lower frequency
59 temperature balance. We also will examine potential rectification by tropical instability waves.

60 Legeckis (1977) first characterized TIWs from satellite sea surface temperature (SST), with
61 a period of about 25 days and a wavelength of about 1000 km. The contribution of TIWs to
62 the low frequency SST anomalies in the eastern Pacific, particularly to seasonal SST anomalies,
63 has been studied in the past (Hansen and Paul 1984; Swenson and Hansen 1999; Wang and
64 McPhaden 1999; Kessler et al. 1998; Polito et al. 2001; Menkes et al. 2006; Jochum and Mur-
65 tugudde 2004). Many of these studies emphasize the role of TIWs in warming the cold tongue
66 in its seasonal evolution through horizontal eddy heat transport. Determining how TIWs modu-
67 late both intra-seasonal and low frequency SST anomalies of the cold tongue in an OGCM with
68 improved forcing of high-resolution QuikSCAT winds is the secondary goal of this study.

69 The overall goal of this study is to explore the influence of horizontal advection by Kelvin
70 waves and TIWs on both the intra-seasonal and low frequency SST variability in the equatorial
71 Pacific. The improved high-resolution satellite forcing enables us to investigate this influence
72 with more realism than was possible before. The QuikSCAT winds have been shown to provide
73 high accuracy and high resolution winds that produce more realistic mean SST, $20^{\circ}C$ isotherm
74 depth, and latent heat flux than NCEP reanalysis-2 winds (Jiang et al. 2008). They also provide
75 high quality hybrid turbulent heat fluxes in the tropical Pacific (Jiang et al. 2005; Zhang 2006).
76 Thus QuikSCAT winds would be expected to allow an ocean model to accurately simulate intra-
77 seasonal Kelvin waves and TIW variability, along with their SST response.

78 The model and data used in this study are described in Section 2. Section 3 gives a detailed
79 comparison between the model and the observations. The mixed-layer temperature budget anal-
80 ysis on both the intra-seasonal and low-frequency time scales are described in Section 4 and
81 Section 5, respectively. The roles of the intra-seasonal Kelvin waves and the tropical instability
82 waves in the horizontal advection and influence on the temperature budgets are also examined.
83 Finally, we give a discussion and summary in Section 6.

84 **2. Model and data**

85 The GFDL Hallberg Isopycnal Model (HIM, Hallberg (1997); Ladd and Thompson (2002)) was
86 used in this study. HIM is a three-dimensional, isopycnal coordinate, C-grid general ocean circu-
87 lation model. A Kraus-Turner-like bulk mixed layer which is similar to the Kraus-Turner model
88 except that the contribution to the entrainment velocity by wind mixing decays with mixed-layer
89 depth, and Richardson number dependant mixing are implemented in the model (Oberhuber

90 1993). Note that the mixed layer is one single model layer. The model domain extended from
91 $100^{\circ}E - 70^{\circ}W$, $30^{\circ}S - 30^{\circ}N$ in the tropical Pacific, with 1° in longitude and 0.5° in latitude, and
92 16 layers in the vertical including an active mixed layer. The biharmonic along-isopycnal vis-
93 cosity ($9 \times 10^{11} m^4/s$) is used. A biharmonic form of Smagorinsky's nonlinear eddy viscosity
94 is also used, with the nondimensional biharmonic Smagorinsky's constant 0.032. The kinematic
95 viscosity below the mixed layer is $1 \times 10^{-4} m^2/s$. For the diffusivity, the along-isopycnal tracer
96 diffusivity is $1 \times 10^3 m^2/s$, and the diapycnal diffusivity of density below the mixed layer is $3 \times$
97 $10^{-5} m^2/s$. We spun up the model for 10 years using ECMWF (European Centre for Medium-
98 Range Weather Forecasts) 40-yr Reanalysis (ERA40) forcing from January 1995 to December
99 1999 repeated once, and then we ran the model for five years from January 2000 to Decem-
100 ber 2004 using QuikSCAT winds, ISCCP (International Satellite Cloud Climatology Project)
101 shortwave and longwave radiation, and NCEP reanalysis-2 (NCEP2) for other atmospheric state
102 variables.

103 It has been shown that QuikSCAT winds have smaller errors than NWP (Numerical Weather
104 Prediction) reanalysis winds when compared to TAO buoy winds (Kelly et al. 1999; Chelton
105 et al. 2001; Jiang et al. 2005). The model was forced by the $1^{\circ} \times 1^{\circ}$ gridded daily QuikSCAT
106 winds field (Kelly et al. 1999). For the shortwave and longwave radiation, we chose $1^{\circ} \times 1^{\circ}$
107 daily ISCCP data. The turbulent heat fluxes (latent and sensible heat fluxes) were calculated in
108 the model using the University of Arizona bulk algorithm (Zeng et al. 1998) from QuikSCAT
109 wind speed, NCEP2 reanalysis atmospheric variables, and model SST. Single variables (e.g., T ,
110 u , v , etc) and mixed-layer temperature budget terms from January 2000 to December 2004 were
111 saved as five-day averaged fields for analysis. See Jiang et al. (2008) for details on the dynamical
112 forcing fields used in this study.

113 To gain confidence in the analysis, the model SST and $20^{\circ}C$ isotherm depth (Z20) averaged
114 between $2^{\circ}S$ and $2^{\circ}N$ are compared with TAO array buoy measurements within $2^{\circ}S - 2^{\circ}N$. We
115 also compare the model SST along $2^{\circ}N$ with the fusion SST product from Remote Sensing Sys-
116 tems (RSS), which is an optimally interpolated SST map using TMI Tropical Rainfall Measuring
117 Mission (TRMM) Microwave Imager) sensor.

118 To obtain the intra-seasonal signal, which is primarily Kelvin waves but also includes some
119 energy from Rossby waves propagating from the far eastern Pacific, we used a bandpass scheme
120 similar to that used in McPhaden (2002). The five-year mean and seasonal cycle were first
121 subtracted from the initial time series to derive an anomalous time series. The anomalous time
122 series were then low-pass filtered with a filter whose half-power frequency was 30 days and
123 another filter whose half-power frequency was 90 days. The bandpassed intra-seasonal signal was
124 the difference between the above two low-pass filtered results. The time series associated with
125 tropical instability waves (hereafter called high-frequency) was obtained by high-pass filtering
126 the anomalous time series with a filter whose half-power frequency was 30 days. The above
127 bandpass scheme with intra-seasonal Kelvin waves and TIWs is justified by the distinct peak
128 gaps between $20^{\circ}C$ isotherm depth at $0^{\circ}140^{\circ}W$ and SST at $2^{\circ}N125^{\circ}W$ for both the observations
129 and the model (Fig. 1). A peak of 50–75 days (Kelvin waves) is shown in TAO Z20 at $0^{\circ}140^{\circ}W$,
130 and a peak of 20–35 days (TIWs) is shown in TMI SST at $2^{\circ}N125^{\circ}W$. The respective values
131 for the model match well with the observations. Note that the peaks in both the observations and
132 the model are statistically significant.

133 [Figure 1 about here.]

3. Comparison of the model with observations

The model compares well with mean TAO measurements along the equator (Fig. 2) in most aspects (Jiang et al. 2008). The five-year-mean temperature from the model (Fig. 2c) matches well with the TAO observations (Fig. 2a) for isotherms above $15^{\circ}C$, but is much colder below. Additionally, the mean model temperature in the eastern Pacific (around $110^{\circ}W$) is slightly warmer than the observations above 200m. The mean zonal velocity from the model (Fig. 2d) captured the main features of the observed velocity (Fig. 2b), with the maximum magnitude of the equatorial undercurrent (EUC) in the model only slightly weaker and the position of the EUC core only slightly deeper than observed. The weak EUC in the model might be partly responsible for the slightly warm temperature in the eastern Pacific. The westward ocean currents in the western Pacific shown in the observations was not simulated well in the model, probably owing to either the poor data availability of TAO observations or the coarse coastline and topography used in the model there.

The time-longitude plots of Z20 and SST in the model agree well with TAO measurements (not shown). The model Z20 is slightly shallower in the western Pacific and deeper in the east. Consistent with errors in Z20, the model SST is slightly colder in the western equatorial Pacific, and warmer in the eastern equatorial Pacific than observed. The time series of model Z20 correlates well with the observations in the central and eastern Pacific ($c \geq 0.60$), while the correlation is relatively small in the western Pacific around $160^{\circ}E$. For SST, the model and the observations correlate well in the central and eastern Pacific ($c > 0.75$), but not as well in the western Pacific. The poor data availability of TAO observations and the coarse coastline and topography used in the model are two possible factors that contribute to the small correlations in the western Pacific.

[Figure 2 about here.]

156

157 **3a. *Intra-seasonal***

158 The intra-seasonal signal in the model, as represented by Z20, compares well with the observa-
159 tions, especially in phase speed (Fig. 3a, c). The eastward propagation of Z20 can be seen in
160 both the observations and the model and is associated with the propagation of downwelling and
161 upwelling Kelvin waves, generated in response to both westerly wind bursts and easterly wind
162 anomalies in the western Pacific. The magnitude of the intra-seasonal thermocline fluctuation
163 (up to 20m) in the model is generally larger than in the observation, which suggests that the
164 intra-seasonal Kelvin waves in the model are somewhat too vigorous. The time-longitude plots
165 of the intra-seasonal sea surface temperature also compare well with the TMI observations (Fig.
166 3b, d). Contrary to the eastward propagation of the Z20, the warming and cooling events on
167 intra-seasonal timescales occurred near simultaneously over a wide range of longitudes or even
168 appeared to propagate westward, especially in the eastern Pacific. This phenomena has also been
169 noticed in the 1990s and early 2000s (Kessler and McPhaden 1995; Zhang 2001; McPhaden
170 2002). Note that the magnitude of the SST variations tended to increase from west to east. As a
171 result, the zonal gradient of the intra-seasonal temperature showed large magnitude in the eastern
172 Pacific, which can be seen in both the observations and the model (Fig. 4a, b). The intra-seasonal
173 zonal velocity anomalies propagate eastward in phase with Z20 anomalies (Fig. 4c). However, an
174 interesting pulsing pattern can also be seen in the zonal velocity that we interpret as interference
175 between eastward propagating Kelvin and westward propagating Rossby waves. It is notewor-
176 thy that the magnitude of the zonal velocity by the Kelvin wave is much larger than that of the
177 Rossby wave. The effect of this interference pattern is westward propagating zonal convergence

178 anomalies that appear to be responsible for the westward propagation of the intra-seasonal zonal
179 temperature gradient anomalies shown in Fig. 4 a and b.

180 [Figure 3 about here.]

181 [Figure 4 about here.]

182 The intra-seasonal Z20 time series in the model correlates well with TAO in the central Pacific
183 ($c \geq 0.60$). The correlations are relatively low, however, in the far western and eastern Pacific,
184 which might be due to the too vigorous Kelvin waves there in the model. For the intra-seasonal
185 SST, the model agrees well with the observations in the western and central Pacific, but has a
186 relatively small correlation in the eastern Pacific (not shown).

187 **3b. High frequency**

188 The 30-day high-pass filtered SST in the model (Fig. 5a) agrees well with TMI SST (Fig. 5b)
189 along $2^\circ N$. The westward propagation of the TIWs can be easily seen, especially during autumn
190 and winter. The model did not capture very well TIW activity in the central Pacific in the second
191 half of 2000 and 2001. However, the model simulated well the strong TIW activity in early 2003,
192 whose importance will be addressed in detail later.

193 [Figure 5 about here.]

194 The strength of TIWs in the model, which can be illustrated by the meridional velocity (time
195 averaged from January 2000 to December 2004) in the mixed layer at $0^\circ 140^\circ W$, is consistent
196 with the meridional velocity observations of TAO array at 35m depth, which is in the middle of
197 the mixed layer in the model (Fig. 2). In addition, the meridional velocity in the mixed layer at

198 $0^{\circ}140^{\circ}W$ has a period of approximately 20 days, which is consistent with the peak in the velocity
199 at 35m depth from $0^{\circ}140^{\circ}W$ TAO mooring (not shown). The five-year TAO time series at $140^{\circ}W$
200 and $110^{\circ}W$ along the equator show a surface (35m) maximum of EKE (eddy kinetic energy) of
201 $436 \text{ cm}^2/\text{s}^2$ and $649 \text{ cm}^2/\text{s}^2$ with periods less than 30 days, the respective values for the model
202 are $403 \text{ cm}^2/\text{s}^2$ and $562 \text{ cm}^2/\text{s}^2$.

203 **4. Intra-seasonal mixed-layer temperature budget**

204 Given the adequate performance of the model in reproducing the variability and the mean along
205 the equator mentioned in Section 3, we proceed with the budget analysis to investigate the roles
206 of Kelvin waves and TIWs in SST variability.

207 The mixed-layer temperature (MLT) in the model evolves in a sequential manner with the
208 following five steps: (1) horizontal advection, (2) horizontal diffusion, (3) net surface heat flux,
209 (4) vertical diffusion, and (5) entrainment. We calculate the mixed-layer temperature budget
210 terms associated with each of these processes by evaluating the temperature values before and
211 after the relevant model routines are recorded (Dawe and Thompson 2007). The MLT budget
212 closes and is consistent with the representation of the temperature budget in the model. The
213 vertical diffusion is not separated from the vertical entrainment term in this study. The horizontal
214 diffusivity term is much smaller (averaged $\sim 0.1^{\circ}C \text{ yr}^{-1}$) than other terms ($\sim 1 - 10^{\circ}C \text{ yr}^{-1}$)
215 so that it is excluded in the analysis. At the same time as the temperature is evolved in the model,
216 the mixed-layer depth and other layer thickness also evolve, such that the mixed-layer depth at
217 each step and the model temperature evolution are consistent.

218 Thus the four primary mixed-layer temperature budget terms that influence its tendency ($\frac{\partial T}{\partial t}$)

219 are the zonal advection, meridional advection, vertical diffusion and entrainment, and the net
220 surface heat flux absorbed in the mixed layer (absorbed shortwave radiation in the mixed layer,
221 net outgoing longwave radiation, sensible heat flux, and latent heat flux) respectively. For a
222 shorthand, we write those four terms as $-u\frac{\partial T}{\partial x}$, $-v\frac{\partial T}{\partial y}$, $-w_e\frac{\Delta T}{h}$, and $\frac{Q_{net}}{\rho_0 C_p h}$, with u , v , and w_e
223 being the mixed-layer zonal velocity, meridional velocity, and vertical entrainment at the base
224 of the mixed layer, ρ_0 the seawater density, C_p the heat capacity, h the mixed-layer depth, and
225 ΔT the temperature difference between the mixed layer and the temperature of the layer being
226 entrained into the mixed layer. Q_{net} in this study represents the net surface heat flux absorbed in
227 the mixed layer, and is equivalent to the adjusted net surface heat flux Q_{adj} used in McPhaden
228 (2002). We emphasize, however, that as discussed earlier, our method of estimating these terms
229 differs from that typically used in empirical analyses such as McPhaden (2002). In particular,
230 each term, including vertical diffusion and entrainment, is calculated implicitly at each model
231 time step.

232 **4a.** *Along the equator*

233 The correlations between the intra-seasonal MLT tendency and each of the other four temperature
234 budget terms along the equator are shown in the left panel of Fig. 6. The correlations on the same
235 four TAO moorings as in McPhaden (2002) are presented in the right panel of Fig. 6 to facilitate
236 the comparison with his results. The time series of the model at a certain mooring location are ob-
237 tained by taking the mean of the nearby model points within 5° longitude. The model suggested
238 an important role for zonal advection (top panel) at all longitudes on the equator, with the largest
239 correlations in the central Pacific. The net surface heat flux term (bottom panel) has the largest
240 correlation in the western Pacific. In the eastern Pacific, zonal advection, vertical diffusion and

241 entrainment, and the meridional advection all have comparable magnitudes of correlations with
242 the temperature tendency. The net heat flux has the smallest correlation in the eastern Pacific,
243 especially east of $120^{\circ}W$. In general, the model results at the four TAO sites (right panel of Fig.
244 6) compare well with those of McPhaden (2002) (his figures 6, 8, 10, and 12) that were based on
245 TAO buoy data at those four sites: the correlation between the zonal advection and the tempera-
246 ture tendency is largest in the central Pacific, and the correlation between the net surface heat flux
247 and temperature tendency is the largest in the western Pacific. However, in the eastern Pacific
248 the model differs from his result: three of those four terms (zonal advection, vertical diffusion
249 and entrainment, and meridional advection) have comparable magnitudes, whereas McPhaden
250 found that the vertical flux and entrainment dominated. It is noteworthy that the vertical term in
251 McPhaden (2002) is the residual of other budget terms. The model result suggested that, when
252 following a single Kelvin wave, one would expect to see the effect of zonal advection from the
253 wave on the intra-seasonal temperature tendency in the central Pacific, but not necessarily in the
254 eastern Pacific since other two other processes contribute as well.

255 [Figure 6 about here.]

256 To determine which physical processes associated with Kelvin waves and TIWs contribute
257 most to the temperature tendency along the equator, we decomposed the zonal and meridional
258 advection terms by frequency. We independently bandpass filtered the temperature and velocities,
259 and then calculated the contribution to the tendency from each crossterm. We decomposed each
260 single variable (e.g., T , u , v) into three parts: high frequency, which represents the TIWs (hf , $<$
261 30 days), intra-seasonal signal, which represents primarily the Kelvin waves, but also includes
262 other variability such as from Rossby waves generated in the far eastern Pacific (is , 30 days – 90
263 days), and the residual signal, which we hereafter refer to as the low-frequency signal (lf , $>$ 90

264 days). The residual low-frequency signal includes the seasonal cycle, the interannual signal and
 265 the five-year mean.

266 Single variables can be expressed as a sum of three frequency band components:

$$\begin{aligned}
 T &= T_{hf} + T_{is} + T_{lf}; \\
 u &= u_{hf} + u_{is} + u_{lf}; \\
 v &= v_{hf} + v_{is} + v_{lf};
 \end{aligned} \tag{1}$$

267 Their contribution to the advection gives 9 crossterms for zonal advection:

$$\begin{aligned}
 u \frac{\partial T}{\partial x} &= (u_{hf} + u_{is} + u_{lf}) \times \frac{\partial}{\partial x} (T_{hf} + T_{is} + T_{lf}) \\
 &= u_{hf} \frac{\partial T_{hf}}{\partial x} + u_{hf} \frac{\partial T_{is}}{\partial x} + u_{hf} \frac{\partial T_{lf}}{\partial x} \\
 &+ u_{is} \frac{\partial T_{hf}}{\partial x} + u_{is} \frac{\partial T_{is}}{\partial x} + u_{is} \frac{\partial T_{lf}}{\partial x} \\
 &+ u_{lf} \frac{\partial T_{hf}}{\partial x} + u_{lf} \frac{\partial T_{is}}{\partial x} + u_{lf} \frac{\partial T_{lf}}{\partial x},
 \end{aligned} \tag{2}$$

268 and meridional advection:

$$\begin{aligned}
 v \frac{\partial T}{\partial y} &= (v_{hf} + v_{is} + v_{lf}) \times \frac{\partial}{\partial y} (T_{hf} + T_{is} + T_{lf}) \\
 &= v_{hf} \frac{\partial T_{hf}}{\partial y} + v_{hf} \frac{\partial T_{is}}{\partial y} + v_{hf} \frac{\partial T_{lf}}{\partial y} \\
 &+ v_{is} \frac{\partial T_{hf}}{\partial y} + v_{is} \frac{\partial T_{is}}{\partial y} + v_{is} \frac{\partial T_{lf}}{\partial y} \\
 &+ v_{lf} \frac{\partial T_{hf}}{\partial y} + v_{lf} \frac{\partial T_{is}}{\partial y} + v_{lf} \frac{\partial T_{lf}}{\partial y}
 \end{aligned} \tag{3}$$

269 We calculated each term separately from filtered five-day averaged variables and then filtered
270 the crossterms to determine how much each contributed to the temperature tendency in the corre-
271 sponding frequency band (hf , is , and lf). The physical interpretation of some crossterms in (2)
272 and (3) are listed in Table 1.

273 [Table 1 about here.]

274 We first examine the zonal advection contribution to the intra-seasonal temperature tendency.
275 In the central Pacific, where the correlation with temperature tendency is largest, intra-seasonal
276 zonal advection is owing both to advection of intra-seasonal temperature gradient by the low-
277 frequency zonal velocity ($-u_{lf} \frac{\partial T_{is}}{\partial x}$, Table 1 (a)) and advection of the low-frequency temperature
278 gradient by the intra-seasonal zonal velocity ($-u_{is} \frac{\partial T_{lf}}{\partial x}$, Table 1 (b)). This implies that the intra-
279 seasonal waves can affect the temperature in the central Pacific by both modifying the zonal
280 current structure (u_{is}) and the zonal temperature gradient ($\frac{\partial T_{is}}{\partial x}$). In the eastern Pacific, $-u_{lf} \frac{\partial T_{is}}{\partial x}$
281 increases and dominates, owing to the larger anomalous zonal temperature gradient there (Fig.
282 4b). As discussed earlier, the increased magnitude of the intra-seasonal SST anomaly in the
283 eastern Pacific results in an anomalous zonal SST gradient.

284 The contribution to the intra-seasonal temperature tendency from meridional advection crossterms
285 (Fig. 7b) is relatively small when compared to zonal advection (Fig. 7a). However, among the
286 9 crossterms in (3), there are two terms that stand out in the eastern Pacific: meridional advec-
287 tion of the mean temperature gradient by the intra-seasonal meridional velocity $-v_{is} \frac{\partial T_{lf}}{\partial y}$, which
288 might be owing to cross-equatorial wind stress anomalies, and the high-frequency nonlinear term
289 $-v_{hf} \frac{\partial T_{hf}}{\partial y}$ (Table 1 (e)) produced by the TIWs that rectify into the intra-seasonal band.

290 [Figure 7 about here.]

291 One might argue that if the largest crossterms in either zonal or meridional advection could
292 cancel, then their sum would not matter to the intra-seasonal temperature tendency. However, the
293 largest crossterms, averaged from $150^{\circ}W$ to $90^{\circ}W$, are not significantly anticorrelated, and thus
294 they appear to play a role in the intra-seasonal temperature tendency.

295 **4b.** *Along the composite Kelvin waves*

296 The intra-seasonal signal in this study includes primarily the Kelvin waves, but also includes
297 some energy from intra-seasonal Rossby waves in the far eastern Pacific. Therefore, to examine
298 the effect of intra-seasonal Kelvin waves on SST variability, it is important to quantify how
299 much a composite downwelling or upwelling Kelvin wave contributes to the intra-seasonal SST
300 anomaly at a certain location. From the contours of the intra-seasonal time-longitude plots of the
301 $20^{\circ}C$ isotherm depth along the equator ($2^{\circ}S - 2^{\circ}N$), we tracked 14 downwelling (dark dotted
302 lines in Fig. 3c) and 12 upwelling (white dotted lines in Fig. 3c) Kelvin waves during the five-
303 year period. For each downwelling Kelvin wave, for instance, we determined its temporal and
304 spatial extent from the positive maximum anomaly of the intra-seasonal $20^{\circ}C$ isotherm depth.
305 Note that Z20 is positive throughout this paper. The temporal and spatial locations of all 14
306 downwelling and 12 upwelling Kelvin waves for single variables (e.g., T , u , v , etc) and mixed-
307 layer temperature budget terms were then obtained. Finally, at each longitude grid point, we
308 averaged the single variables and budget terms over periods of anomalous positive and negative
309 Z20 to obtain the average values for respectively downwelling and upwelling Kelvin waves.

310 As evident in Fig. 8, there was a warming anomaly almost all the way from west to east
311 along the trajectory of a composite downwelling Kelvin wave. In the central Pacific, from 180°
312 to $125^{\circ}W$, zonal advection along the composite downwelling Kelvin wave accounted for most

313 of the positive anomaly in the temperature tendency (Fig. 8a). In the eastern Pacific, east of
314 $130^{\circ}W$, however, the vertical diffusion and entrainment started to play an important role (Fig.
315 8b). The region separation of those two processes appeared to be much less than $2,500Km$, a
316 quarter of the Kelvin wavelength. Thus, the time for a composite Kelvin wave to travel from the
317 region where the zonal advection dominates to the region where the vertical processes contribute
318 is short relative to the time for SST to respond to zonal advection. Therefore, warming by a single
319 downwelling Kelvin wave could occur earlier in the eastern than in the central Pacific, given the
320 fact that the vertical diffusion and entrainment leads the zonal advection by a quarter of cycle. It
321 is noteworthy that the magnitude of the meridional advection along Kelvin waves (not shown) is
322 smaller than the zonal advection, and vertical diffusion and entrainment.

323 We also found apparent cancellations of the temperature tendency, zonal advection, vertical
324 diffusion and entrainment along the equator between the composite downwelling and upwelling
325 Kelvin waves. Zonal advection and vertical processes tend to oppose the cooling anomalies by
326 an upwelling Kelvin wave, although this cancellation is not exact. As shown in the histograms of
327 the intra-seasonal Z20 along 14 downwelling (Fig. 8c) and 12 upwelling (Fig. 8d) Kelvin waves,
328 the mean magnitude of Z20 along the two selected types of waves are the same (about $12m$).

329 [Figure 8 about here.]

330 **5. Low-frequency mixed-layer temperature budget**

331 For the low-frequency temperature budget (>90 days), the correlation results are similar to those
332 of the intra-seasonal time scale: zonal advection has a significant correlation with temperature
333 tendency along the equator, especially in the central Pacific (Fig. 9 top panel). In addition, the

334 net surface heat flux (Fig. 9 bottom panel) has the largest correlation with temperature tendency
335 in the western Pacific. Meridional advection and vertical diffusion and entrainment have slightly
336 smaller correlations along the equator than zonal advection and net surface heat flux, but might
337 still be important.

338 [Figure 9 about here.]

339 Of the three crossterms in (2) that contribute significantly to the low-frequency zonal ad-
340 vection, advection of the low-frequency temperature gradient by the low-frequency velocity
341 ($-u_{lf} \frac{\partial T_{lf}}{\partial x}$, Table 1 (c)) has the largest magnitude (Fig. 10a). This term is associated with the
342 interaction between the low-frequency horizontal velocity with temperature gradient fluctuations.
343 The rectification from the intra-seasonal Kelvin waves ($-u_{is} \frac{\partial T_{is}}{\partial x}$, Table 1 (d)) is associated with
344 the interaction between the intra-seasonal zonal current with zonal SST gradient by the intra-
345 seasonal waves to the temperature tendency and contributes significantly in the eastern Pacific.
346 In addition, there is a small rectification from tropical instability waves ($-u_{hf} \frac{\partial T_{hf}}{\partial x}$). There are
347 no significant anticorrelations between the largest crossterms, suggesting that they are all crucial
348 terms in zonal advection (Fig. 11a, b). Whether or not those crossterms contribute greatly to
349 the low-frequency temperature tendency requires a complete decomposition analysis of all the
350 budget terms, including the vertical diffusion and entrainment and net heat flux, which can not be
351 easily done using the same bandpass method as in the horizontal advection, because the mixed
352 layer depth evolves in concert with other variables in this isopycnal model. The time series of
353 the largest crossterms in zonal advection (Fig. 11a), averaged from $150^{\circ}W$ to $90^{\circ}W$, suggest that
354 the rectification from intra-seasonal waves ($-u_{is} \frac{\partial T_{is}}{\partial x}$) is a positive (warming) contribution to the
355 low-frequency temperature tendency from late 2002 to early 2004.

[Figure 10 about here.]

356
357 For meridional advection, rectification from tropical instability waves ($-v_{hf} \frac{\partial T_{hf}}{\partial y}$, Table 1
358 (e)) has the largest magnitude from $140^\circ W$ to $110^\circ W$ among all the crossterms (Fig. 10b). As
359 in the zonal advection, there are no significant cancellations between the largest crossterms in
360 the meridional advection (Fig. 11b). The term associated with the interaction between the low-
361 frequency meridional velocity and temperature gradient fluctuations ($-v_{lf} \frac{\partial T_{lf}}{\partial y}$) showed seasonal
362 cycles, with cooling in March and warming in September. Meanwhile, the cooling by this term in
363 early 2003 seems to be mostly compensated by the anomalous warming by the rectification from
364 TIWs ($-v_{hf} \frac{\partial T_{hf}}{\partial y}$), indicating a possibly important role of TIWs in the seasonal evolution of the
365 cold tongue.

[Figure 11 about here.]

366
367 It can be shown that the approaches used by Kessler and Kleeman (2000) and Shinoda and
368 Hendon (2002) to calculate the rectification are comparable to the bandpassed method used in
369 this study. Briefly, the rectification from an anomalous signal (V') to the mean (V_{mean}) in their
370 approaches is the running mean of the difference between a product of the anomalous signals
371 plus their means and a product of the means. In analogy to their approach, the rectification in the
372 zonal advection is defined as the running mean of the difference between the following two terms:
373 $(u_{mean} + u_{is}) \frac{\partial(T_{mean} + T_{is})}{\partial x}$ and $u_{mean} \frac{\partial(T_{mean})}{\partial x}$. The signal longer than 90 days was referred to as the
374 “mean” in Shinoda and Hendon (2002), and is the same as the low-frequency signal in this study.
375 Therefore, the rectification using their approaches before the 90-day running mean is identical to
376 three crossterms in this study ($u_{is} \frac{\partial T_{is}}{\partial x}$, $u_{is} \frac{\partial T_{lf}}{\partial x}$, and $u_{lf} \frac{\partial T_{is}}{\partial x}$). We found that rectification calculated
377 from their approaches is primarily from one single bandpass filtered term ($u_{is} \frac{\partial T_{is}}{\partial x}$) in this study.

378 The low-frequency temperature tendency has both seasonal and interannual cycles (Fig.12a),
379 while the rectification of the intra-seasonal waves occurred during the second year of 2002, the
380 whole year of 2003, and the first half of 2004 (Fig. 12b). The large magnitude of the rectification
381 was mainly centered in the eastern Pacific, especially east of $140^{\circ}W$, where large magnitude of
382 the zonal gradient of the intra-seasonal SST was found (Fig. 4). As mentioned in Section 4, the
383 increased magnitude of the intra-seasonal temperature tendency in the east by the Kelvin waves
384 (Fig. 8) might be responsible for the large SST gradient, and therefore the rectification. Five
385 years of analysis is not long enough to identify which timescale of temperature tendency the
386 intra-seasonal Kelvin waves rectified to. Meanwhile, there is distinct rectification of the tropical
387 instability waves in the meridional advection term in early 2003, which might be associated with
388 the strong TIW activity during that period, as shown in Fig. 5. This strong TIW activity caused
389 a large positive latitudinal SST gradient (over $1^{\circ}C/$ between $2^{\circ}N$ and equator); the resulting
390 warming of the cold tongue may have contributed to the demise of the 2003 La Niña (McPhaden
391 2004). It is yet unclear whether this strong TIW activity is related to the prevalence of intra-
392 seasonal Kelvin waves from 2002 to 2004.

393 [Figure 12 about here.]

394 **6. Discussion and conclusion**

395 In this study, we examined the contribution of Kelvin waves and TIWs to the intra-seasonal and
396 low-frequency mixed-layer temperature tendency from 2000 to 2004. An isopycnal ocean model
397 was forced with QuikSCAT winds, ISCCP shortwave and longwave radiation, and other NCEP2
398 meteorological variables.

399 The model captured well the mean and variability along the equator compared to observa-
400 tions. The intra-seasonal variability of Z20, the SST and its zonal gradient compared well with
401 TAO observations. The zonal SST gradient has large magnitude in the eastern Pacific and ap-
402 peared to propagate westward in the far east. The intra-seasonal anomalies in the zonal SST
403 gradient are ultimately caused by the large SST variations to the east caused by vertical processes
404 acting on the shallow thermocline there. These large SST variations tend to be in phase with
405 weaker SST variations in the central Pacific and thus result in a SST zonal gradient. Once this
406 gradient is generated, the westward propagating zonal convergence associated with the Kelvin
407 and Rossby wave interference pattern causes the zonal temperature gradient to also propagate
408 westward. Additionally, the TIW signals along $2^{\circ}N$ in the model agreed well with the TMI SST
409 observations, especially in early 2003. The strength of TIWs in the model is consistent with the
410 TAO observations.

411 The intra-seasonal mixed-layer temperature budget is consistent with the results of McPhaden
412 (2002) based on four TAO moorings: the temperature tendency has the largest correlation with
413 the net surface heat flux in the western Pacific, where the thermocline is deep; and with zonal
414 advection in the central Pacific. In the eastern Pacific, the model differs from McPhaden's re-
415 sults, in that three of the four temperature budget terms (zonal advection, vertical diffusion and
416 entrainment, and meridional advection) have comparable correlations with temperature tendency.
417 In particular, the vertical processes acting on the shallow thermocline cause large SST anomalies
418 in phase with the intra-seasonal thermocline anomalies.

419 The intra-seasonal temperature budget analysis along the composite Kelvin wave confirmed
420 the above results along the equator. The region where the zonal advection dominates was found
421 to be adjacent and to the east of the region where the vertical processes contribute, with the tran-

422 sition occurring roughly at $130^{\circ}W$. This finding can not be achieved from TAO observations
423 because of their sparse resolution (McPhaden 2002; Zhang 2001). Meanwhile, this finding con-
424 firms the statement of McPhaden (2002) that the growing importance of the vertical diffusion
425 and entrainment in the eastern Pacific is responsible for the in-phase or even westward propa-
426 gating SST variations shown in Fig. 3. Furthermore, there were apparent cancellations in the
427 intra-seasonal temperature tendency, zonal advection, and vertical diffusion and entrainment be-
428 tween the composite downwelling and upwelling Kelvin waves. These cancellations suggested
429 that the importance of Kelvin waves to SST variability depends on the ratio of the numbers of
430 downwelling to upwelling Kelvin waves weighted by their strength and only the linear effect is
431 considered.

432 We decomposed the horizontal advection terms into three spectral bands (high-frequency:
433 <30 days; intra-seasonal: 30 days–90 days; low-frequency: >90 days). For the intra-seasonal
434 temperature tendency, a comparison of the contributions suggested that zonal advection of the
435 intra-seasonal temperature gradient by the low-frequency zonal velocity $-u_{lf} \frac{\partial T_{is}}{\partial x}$ and zonal ad-
436 vection of the low-frequency temperature gradient by intra-seasonal zonal velocity $-u_{is} \frac{\partial T_{lf}}{\partial x}$ are
437 comparable in the central Pacific, but that $-u_{lf} \frac{\partial T_{is}}{\partial x}$ dominates in the eastern Pacific where the
438 thermocline is shallow. A small contribution from the meridional advection of the high-frequency
439 meridional temperature gradient by high-frequency meridional velocity, $-v_{hf} \frac{\partial T_{hf}}{\partial y}$, indicated a
440 rectification of meridional advection from the TIWs to the intra-seasonal temperature tendency.

441 The low-frequency mixed-layer temperature tendency has the largest correlation with zonal
442 advection in the central Pacific, and with the net surface heat flux in the western Pacific, but all
443 budget terms might contribute to low-frequency temperature tendency in the eastern Pacific.

444 We found rectification in horizontal advection from the intra-seasonal waves and TIWs to be

445 secondary contributors, with the largest contribution from the advection of the low-frequency
446 temperature gradients by low-frequency velocities. The rectification from the intra-seasonal
447 waves ($-u_{is} \frac{\partial T_{is}}{\partial x}$) had large magnitude in the eastern Pacific, especially east of $140^\circ W$, where
448 large magnitude of the zonal gradient of the intra-seasonal SST can also be found. In addi-
449 tion, the cancellations we found in the intra-seasonal temperature tendency between a composite
450 downwelling and upwelling Kelvin wave does not indicate there would be no net contribution.
451 There would be no net contribution from a downwelling Kelvin wave and a subsequent upwelling
452 Kelvin wave only in a linear context, in which no interaction among intra-seasonal oscillations
453 (for instance $-u_{is} \frac{\partial T_{is}}{\partial x}$) occurred. It is the nonlinearity between the intra-seasonal zonal velocity
454 and the zonal gradient of the intra-seasonal SST by the Kelvin waves that resulted in the recti-
455 fication to low-frequency SST. The rectification in SST by the feedback between the warm pool
456 SST and MJO in the western Pacific has been found in Kessler and Kleeman (2000). This study,
457 however, provided the physical mechanism for the rectification in SST from intra-seasonal waves
458 in the eastern Pacific.

459 The rectification in SST from TIWs in the eastern Pacific has been found in the coupled model
460 of Jochum et al. (2007b) and Jochum and Murtugudde (2004). This study suggested that the
461 strong TIW activity associated with strong SST fronts along $2^\circ N$ and cold SST on the equator in
462 early 2003 may be responsible for the rectification of the TIWs to the low-frequency temperature
463 tendency. Averaged from $150^\circ W - 90^\circ W$, the magnitude of the rectification of TIWs in early
464 2003 to the low-frequency SST variability is comparable with the cooling contribution from low-
465 frequency interaction. This implies that anomalously strong TIWs in early 2003 warm the cold
466 tongue, which may contribute to the abrupt cessation of the La Niña in early 2003 (McPhaden
467 2004).

468 Since we only decomposed the horizontal advection terms in this study, the rectification from
469 the intra-seasonal Kelvin waves and TIWs to the low-frequency temperature tendency through
470 zonal advection might be smaller than other MLT budget terms and therefore have less of a
471 contribution to the low-frequency temperature tendency. Further and more complete studies are
472 required to determine the roles of these two types of waves to the low-frequency SST variabil-
473 ity. Meanwhile, the low-frequency analysis in this study includes both the seasonal cycle and
474 the interannual variability, our results did not indicate the exact time scales on which the Kelvin
475 waves and TIWs rectified. With only five years of QuikSCAT wind forcing, we could not exam-
476 ine the longer time scale in detail. It would be interesting to explore further this scale interaction
477 when a longer period of QuikSCAT winds is available. In addition, our analysis focused on the
478 equatorial temperature budget, not on the meridional temperature structure. Using a numerical
479 model, Jochum and Murtugudde (2006) showed that the off-equatorial zonal heat flux conver-
480 gences by the TIWs were comparable in size to the meridional eddy heat flux convergence on the
481 equator. This was verified by Jochum et al. (2007a) using on and off-equatorial current meter
482 measurements. According to Jochum and Murtugudde (2006), TIWs act as a vertical heat pump
483 and increase the net air-sea surface heat flux on the annual-mean time scale. Further temperature
484 budget studies with longer model runs are needed to determine whether or not the rectification
485 from intra-seasonal Kelvin waves and TIWs are critical to ENSO and to climate variability.

Acknowledgement The authors would like to thank Suzanne Dickinson for preparing the QuikSCAT gridded winds and NCEP2 fields. We would also like to thank Jordan T. Dawe and David Darr for their help in HIM model. NCEP2 reanalysis data are obtained from <ftp://ftp.cdc.noaa.gov/Datasets/ncep.reanalysis2.dailyavgs/>. ECMWF ERA40 data have been obtained from <http://data.ecmw->

f.int/data/d/era40_daily/. The TAO buoy data are from NOAA's Pacific Marine Environmental Laboratory (PMEL) http://www.pmel.noaa.gov/tao/data_deliv/. We also acknowledge the TAO Project Office, Dr. Michael J. McPhaden, Director. This work was supported by grant GC99-370 from the NOAA Office of Global Programs Pan American Climate Studies, and NASA's Ocean Vector Winds Science Team through contract 1285662 with the Jet Propulsion Laboratory.

References

- Chelton, D., S. Esbensen, M. Schlax, N. Thum, and M. Freilich, 2001: Observations of coupling between surface wind stress and sea surface temperature in the eastern tropical Pacific. *J. Climate*, **14**, 1479–1498.
- Dawe, J. and L. Thompson, 2007: PDO-related heat and temperature budget changes in a model of the north Pacific. *J. Climate*, **20**, 2092–2108.
- Giese, B. and D. Harrison, 1991: Eastern equatorial Pacific response to three composite westerly wind types. *J. Geophys. Res.*, **96**, 3239–3248.
- Hallberg, R., 1997: Localized coupling between surface and bottom intensified flow over topography. *J. Phys. Oceanogr.*, **27**, 27 911–27 988.
- Hansen, D. V. and C. A. Paul, 1984: Genesis and effects of long waves in the equatorial Pacific. *J. Geophys. Res.*, **89**, 10,430–10,440.
- Harrison, D. and B. Giese, 1988: Remote westerly wind forcing of the eastern equatorial Pacific: some model results. *Geophys. Res. Lett.*, **15**, 804–807.
- Harrison, D. and P. Schopf, 1984: Kelvin-wave-induced anomalous advection and the onset of surface warming in El Niño events. *Mon. Wea. Rev.*, **112**, 923–933.
- Jiang, C., M. F. Cronin, K. Kelly, and L. Thompson, 2005: Evaluation of a hybrid satellite- and NWP-based turbulent heat flux product using Tropical Atmosphere-Ocean (TAO) buoys. *J. Geophys. Res.*, **110**, C09007.
- Jiang, C., L. Thompson, and K. Kelly, 2008: Equatorial influence of QuikSCAT

- winds in an isopycnal ocean model compared to NCEP2 winds. *Ocean Modeling*, 10.1016/j.ocemod.2008.05.003.
- Jochum, M., M. F. Cronin, W. S. Kessler, and D. Shea, 2007a: Observed horizontal temperature advection by Tropical Instability Waves. *Geophys. Res. Lett.*, **34**, doi:10.1029/2007GL029416.
- Jochum, M., C. Deser, and A. Phillips, 2007b: Tropical atmospheric variability forced by oceanic internal variability. *J. Climate.*, **20**, 765–771.
- Jochum, M. and R. Murtugudde, 2004: Internal variability in the tropical Pacific ocean. *Geophys. Res. Lett.*, **31**, doi:10.1029/2004GL020488.
- 2006: Temperature advection by tropical instability waves. *J. Phys. Oceanogr.*, **36**, 592–605.
- Kelly, K., S. Dickinson, and Z.-J. Yu, 1999: NSCAT tropical wind stress maps: Implications for improving ocean modeling. *J. Geophys. Res.*, **105**, 11 291–11 310.
- Kessler, W. and R. Kleeman, 2000: Rectification of the Madden Julian Oscillation into the ENSO cycle. *J. Climate*, **13**, 3560–3575.
- Kessler, W. and M. McPhaden, 1995: 1991-93 El Niño in the central Pacific. *Deep-Sea Res.*, **42B**, 295–334.
- Kessler, W., M. McPhaden, and K. Weickman, 1995: Forcing of intraseasonal Kelvin waves in the equatorial Pacific. *J. Geophys. Res.*, **100**, 10 613–10 631.
- Kessler, W., L. Rothstein, and D. Chen, 1998: The annual cycle of SST in the eastern tropical Pacific, diagnosed in an ocean GCM*. *J. Climate*, **11**, 777–799.

- Kessler, W. S., 2005: Intraseasonal variability in the oceans. *Intraseasonal variability of the Atmosphere-Ocean system.*, W.K.M Lau and D.E. Waliser, Eds. Praxis Publishing.
- Kutsuwada, K. and M. McPhaden, 2002: Intraseasonal variations in the upper equatorial Pacific Ocean prior to and during the 1997-98 El Niño. *J. Phys. Oceanogr.*, **32**, 1133–1149.
- Ladd, C. and L. Thompson, 2002: Decadal variability of north Pacific central mode water. *J. Phys. Oceanogr.*, **32**, 2870–2881.
- Legeckis, R., 1977: Long waves in the eastern equatorial Pacific ocean - A view from a geostationary satellite. *Science*, **197**, 1179–1181.
- McPhaden, M., 1999: Genesis and evolution of the 1997-98 El Niño. *Science*, **283**, 950–954.
- 2002: Mixed layer temperature balance on intraseasonal time scales in the equatorial Pacific Ocean. *J. Climate*, **15**, 2632–2647.
- 2004: Evolution of the 2002-03 El Niño. *Bull. Amer. Meteor. Soc.*, **85**, 677–695.
- Menkes, C., V. JG., K. SC., J. Boulanger, and M. GV., 2006: A modeling study of the impact of tropical instability waves on the heat budget of the eastern equatorial Pacific. *J. Phy. Oceanogr.*, **36**, 847–865.
- Oberhuber, J., 1993: Simulation of the Atlantic circulation with a coupled sea ice-mixed layer-isopycnal general circulation model. Part I: Model description. *J. Phys. Oceanogr.*, **23**, 808–829.
- Polito, P., J. Ryan, W. Liu, and P. Chavez, 2001: Oceanic and atmospheric anomalies of tropical instability waves. *Geophys. Res. Lett.*, **28**, 2233–2236.

- Seo, K.-H. and Y. Xue, 2005: MJO-related oceanic Kelvin waves and the ENSO cycle: A study with the NCEP Global Ocean Data Assimilation System. *Geophys. Res. Lett.*, **32**, L07712.
- Shinoda, T. and H. H. Hendon, 2002: Rectified wind forcing and latent heat flux produced by the Madden-Julian Oscillation. *J. Climate*, **15**, 3500–3508.
- Swenson, M. and D. Hansen, 1999: Tropical Pacific ocean mixed layer heat budget: the Pacific cold tongue. *J. Phys. Oceanogr.*, **29**, 69–81.
- Vecchi, G. and D. Harrison, 2000: Tropical Pacific sea surface temperature anomalies, El Niño, and Equatorial westerly wind events. *J. Climate*, **13**, 1814–1830.
- Wang, W. and M. J. McPhaden, 1999: The surface-layer heat balance in the equatorial Pacific Ocean. Part I: mean seasonal cycle. *J. Phys. Oceanogr.*, **29**, 1812–1831.
- Zeng, X., M. Zhao, and R. E. Dickinson, 1998: Intercomparison of bulk aerodynamic algorithms for the computation of sea surface fluxes using TOGA COARE and TAO data. *J. Climate*, **11**, 2628–2644.
- Zhang, C., 2001: Intraseasonal perturbations in Sea Surface Temperature of the Equatorial eastern Pacific and their association with the Madden-Julian Oscillation. *J. Climate*, **14**, 1309–1322.
- 2006: The impact of satellite winds and latent heat fluxes in a numerical simulation of the Tropical Pacific Ocean. *J. Climate*, **19**, 5889–5902.
- Zhang, C. and J. Gottschalck, 2002: SST anomalies of ENSO and the Madden-Julian Oscillation in the equatorial Pacific. *J. Climate*, **15**, 2429–2445.

List of Figures

- 1 Power spectral density of Z20 (m) at $0^{\circ}N140^{\circ}W$ where the distinct signal of Kelvin waves were shown for (a) TAO, and (b) HIM; and power spectral density of SST ($^{\circ}C$) at $2^{\circ}N125^{\circ}W$ where the distinct signals of TIWs were shown for (c) TAO, and (d) HIM. The smooth solid curve is the spectrum of red noise which has the same total variance as the signal. The dashed curve is the 95% confidence level (CL) needed to reject a null hypothesis of red noise on a priori basis. 31
- 2 Five-year-mean temperature ($^{\circ}C$) (left panel) and zonal velocity (cm/s) (right panel) from TAO (upper panel) and from the model (lower panel) along the equator (averaged over $2^{\circ}S - 2^{\circ}N$). The dark black line in (a) shows the mean Levitus mixed layer depth, and the dark black line in (c) shows the mean mixed layer depth in the model. 32
- 3 Time-longitude plots of the intra-seasonal (a) TAO $20^{\circ}C$ isotherm depth, (b) TMI SST, (c) HIM $20^{\circ}C$ isotherm depth, and (d) HIM SST. The 14 dotted black lines in (c) show the selected downwelling Kelvin wave ray paths, and the 12 dotted white lines show the upwelling Kelvin wave ray paths. The zonal grid resolutions in (b) and (d) are 1 degree. 33
- 4 Time-longitude plots of the equatorial (a) TMI $\partial T_{is}/\partial x$, (b) HIM $\partial T_{is}/\partial x$, (c) HIM zonal velocity u_{is} , and (d) HIM $\partial u_{is}/\partial x$ 34
- 5 Time-longitude plots of the 30-day highpassed SST ($^{\circ}C$) along $2^{\circ}N$ for (a) TMI, and (b) the model. 35

6	Correlations of the intra-seasonal temperature tendency with temperature budget terms: zonal advection, meridional advection, vertical diffusion and entrainment, and net surface heat flux (from top to bottom, left panel) along the equator. Corresponding values at four TAO buoys are shown in the right panel. Ninety-five percent confidence limits for the correlations (dash-dot lines in left panel, asterisks in right panel) are also shown.	36
7	Root mean square (RMS) of the intra-seasonal temperature tendency and the decompositions of (a) the zonal advection, and (b) the meridional advection along the equator.	37
8	(a) The intra-seasonal temperature tendency versus zonal advection along composite Kelvin waves, (b) temperature tendency versus vertical diffusion and entrainment along composite Kelvin waves, (c) histogram of the intra-seasonal Z20 for all 14 downwelling Kelvin waves, and (d) histogram of the intra-seasonal Z20 for all 12 upwelling Kelvin waves.	38
9	Same as Fig. 6 left panel, but for low-frequency signal.	39
10	Same as Fig. 7, but for low-frequency signal and three largest terms.	40
11	Time series of the largest three terms averaged from $150^{\circ}W - 90^{\circ}W$ in (a) zonal advection, and (b) the meridional advection from Jan 2000 to Dec 2004.	41
12	Time-longitude plots of the (a) low-frequency temperature tendency, (b) intra-seasonal zonal advection of the intra-seasonal zonal temperature gradient, and (c) high-frequency meridional advection of the high-frequency meridional temperature gradient. Units are $10^{-7} \text{ }^{\circ}C s^{-1}$	42

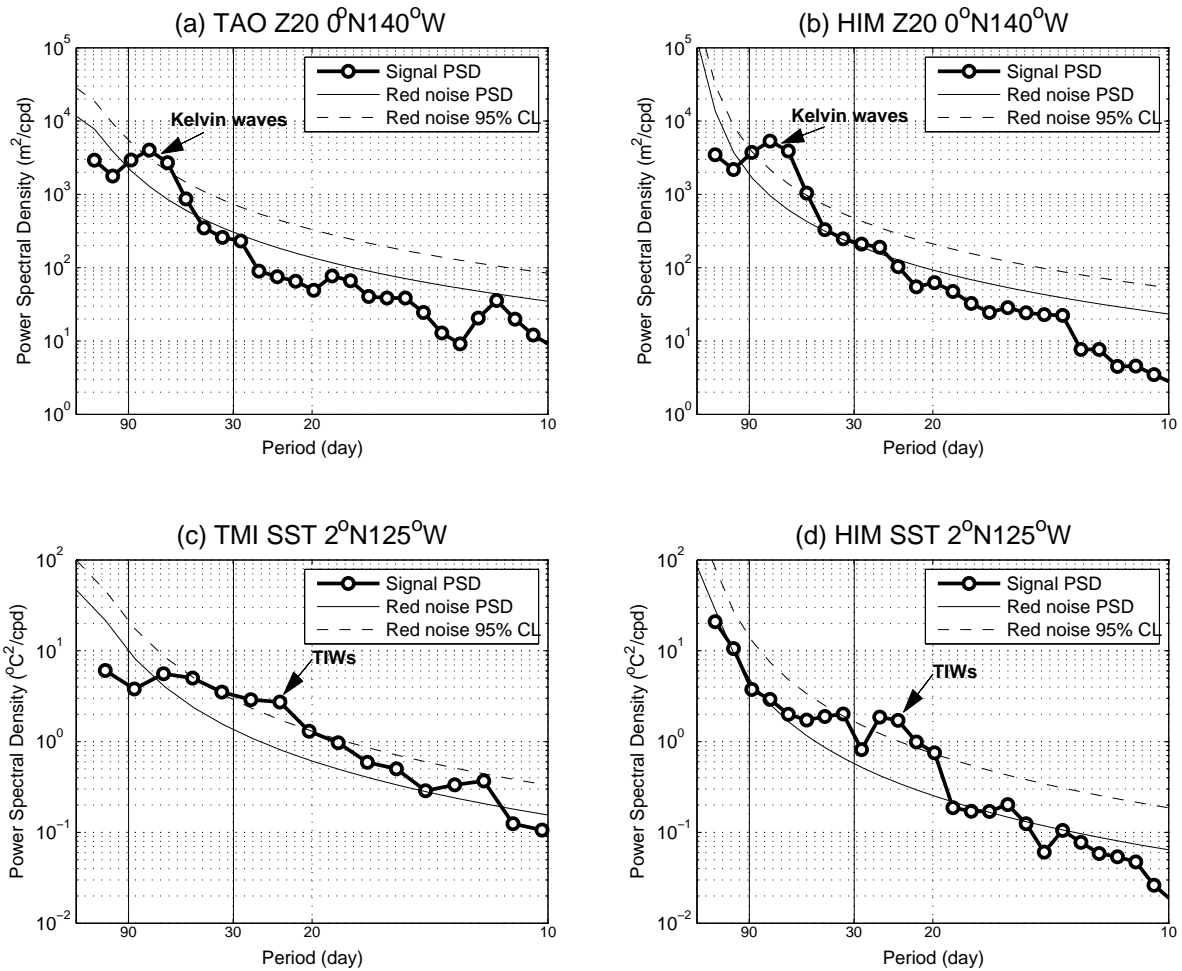


Figure 1: Power spectral density of Z20 (m) at $0^{\circ}N140^{\circ}W$ where the distinct signal of Kelvin waves were shown for (a) TAO, and (b) HIM; and power spectral density of SST ($^{\circ}C$) at $2^{\circ}N125^{\circ}W$ where the distinct signals of TIWs were shown for (c) TAO, and (d) HIM. The smooth solid curve is the spectrum of red noise which has the same total variance as the signal. The dashed curve is the 95% confidence level (CL) needed to reject a null hypothesis of red noise on a priori basis.

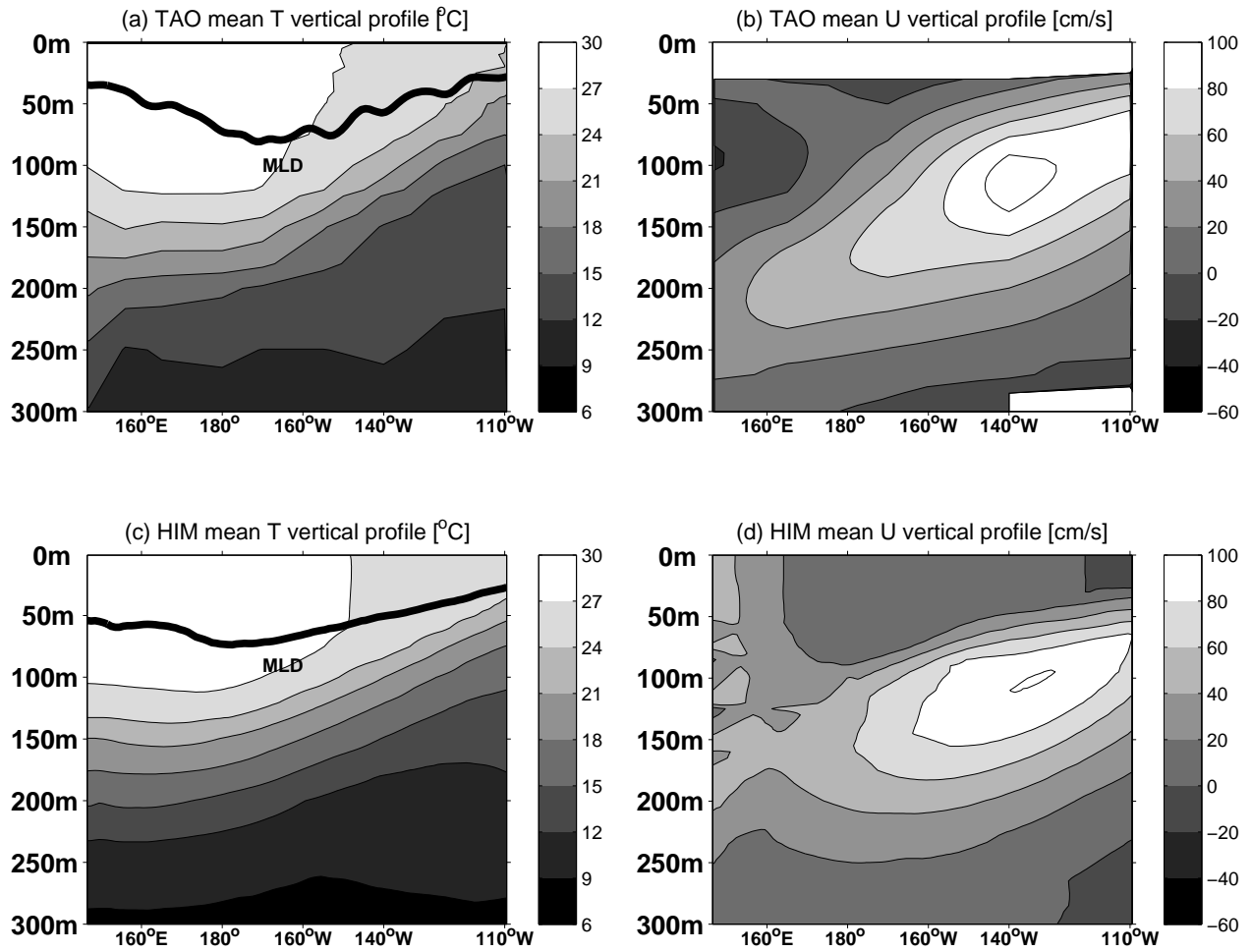


Figure 2: Five-year-mean temperature ($^{\circ}C$) (left panel) and zonal velocity (cm/s) (right panel) from TAO (upper panel) and from the model (lower panel) along the equator (averaged over $2^{\circ}S - 2^{\circ}N$). The dark black line in (a) shows the mean Levitus mixed layer depth, and the dark black line in (c) shows the mean mixed layer depth in the model.

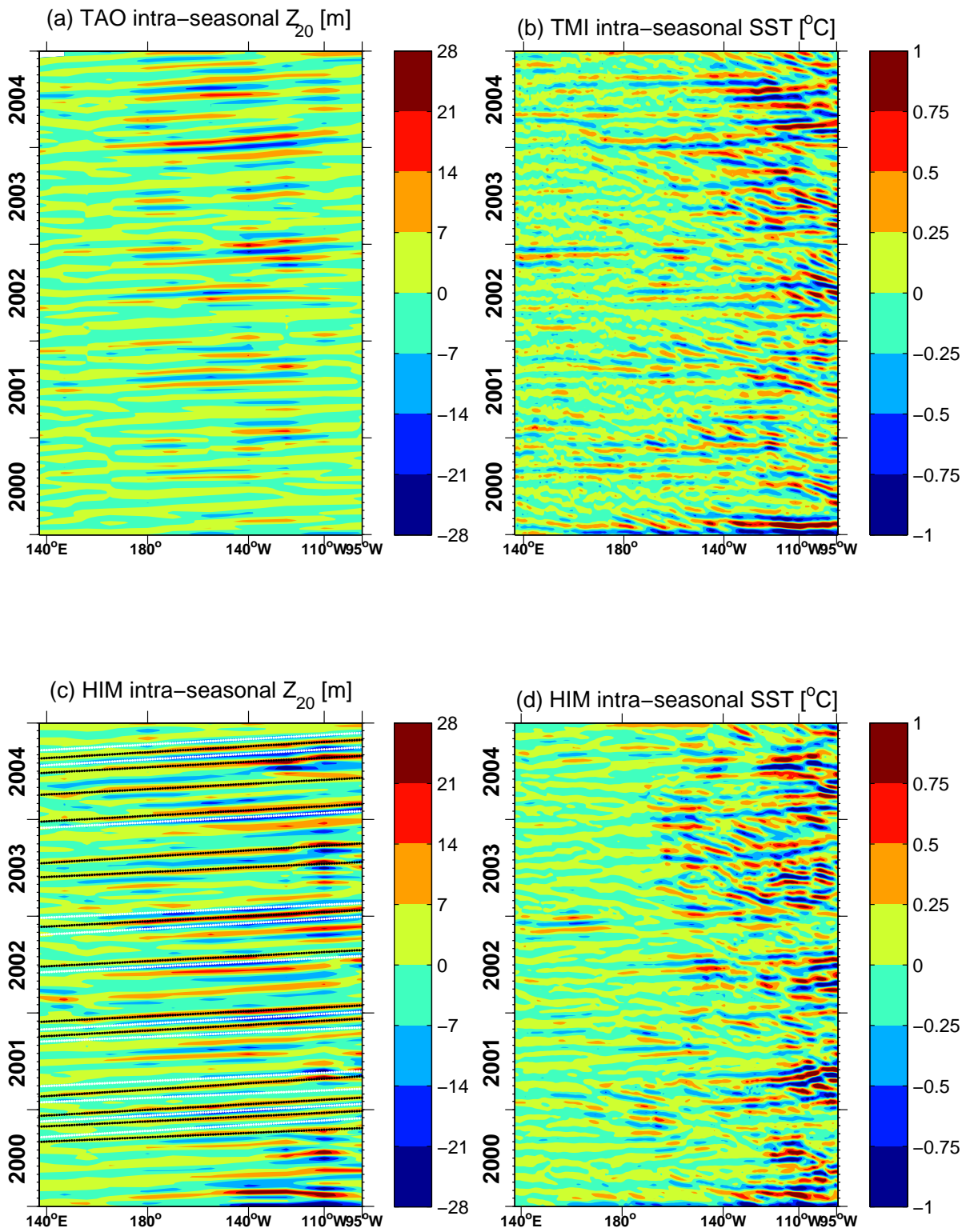


Figure 3: Time-longitude plots of the intra-seasonal (a) TAO 20°C isotherm depth, (b) TMI SST, (c) HIM 20°C isotherm depth, and (d) HIM SST. The 14 dotted black lines in (c) show the selected downwelling Kelvin wave ray paths, and the 12 dotted white lines show the upwelling Kelvin wave ray paths. The zonal grid resolutions in (b) and (d) are 1 degree.

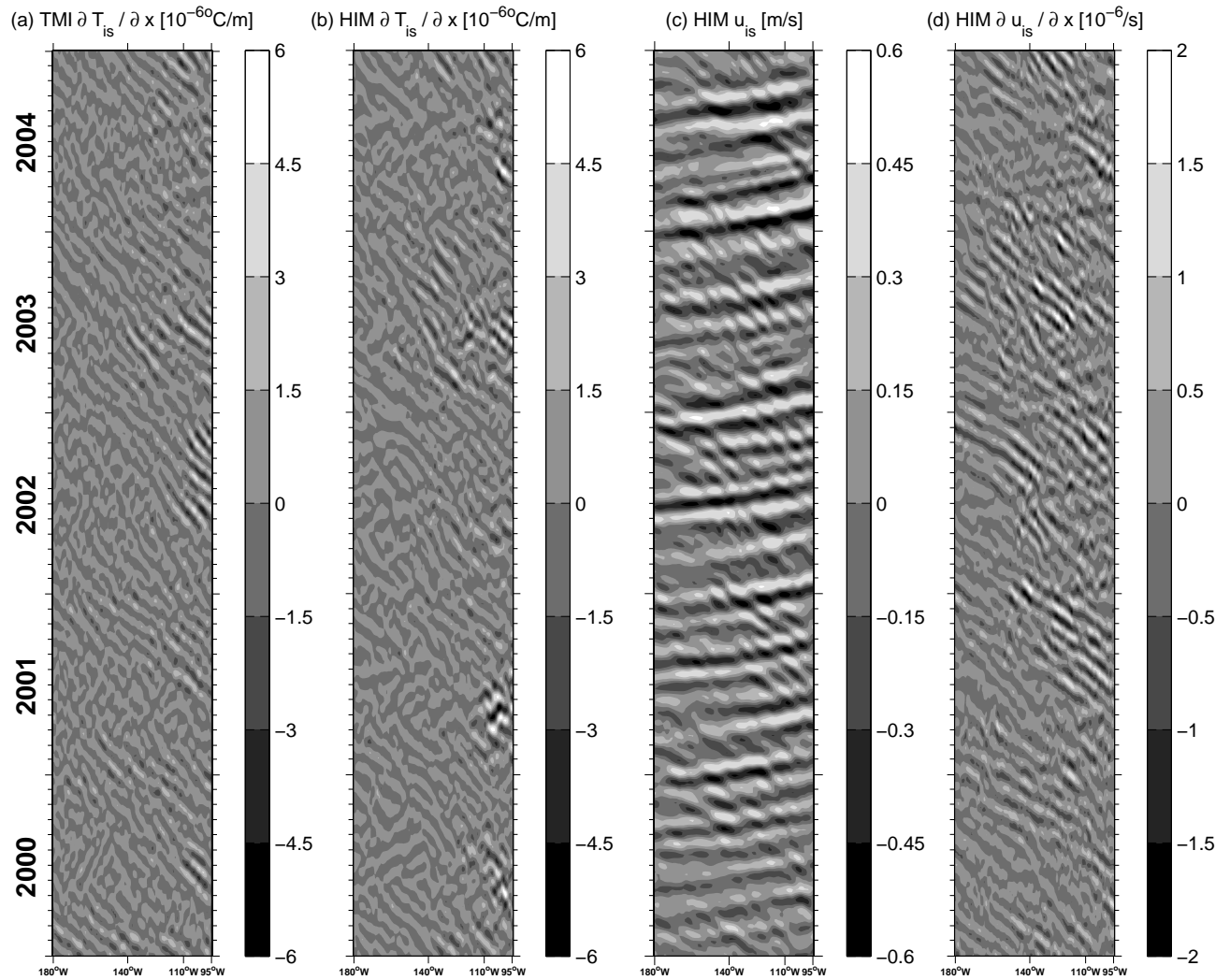


Figure 4: Time-longitude plots of the equatorial (a) TMI $\partial T_{is} / \partial x$, (b) HIM $\partial T_{is} / \partial x$, (c) HIM zonal velocity u_{is} , and (d) HIM $\partial u_{is} / \partial x$.

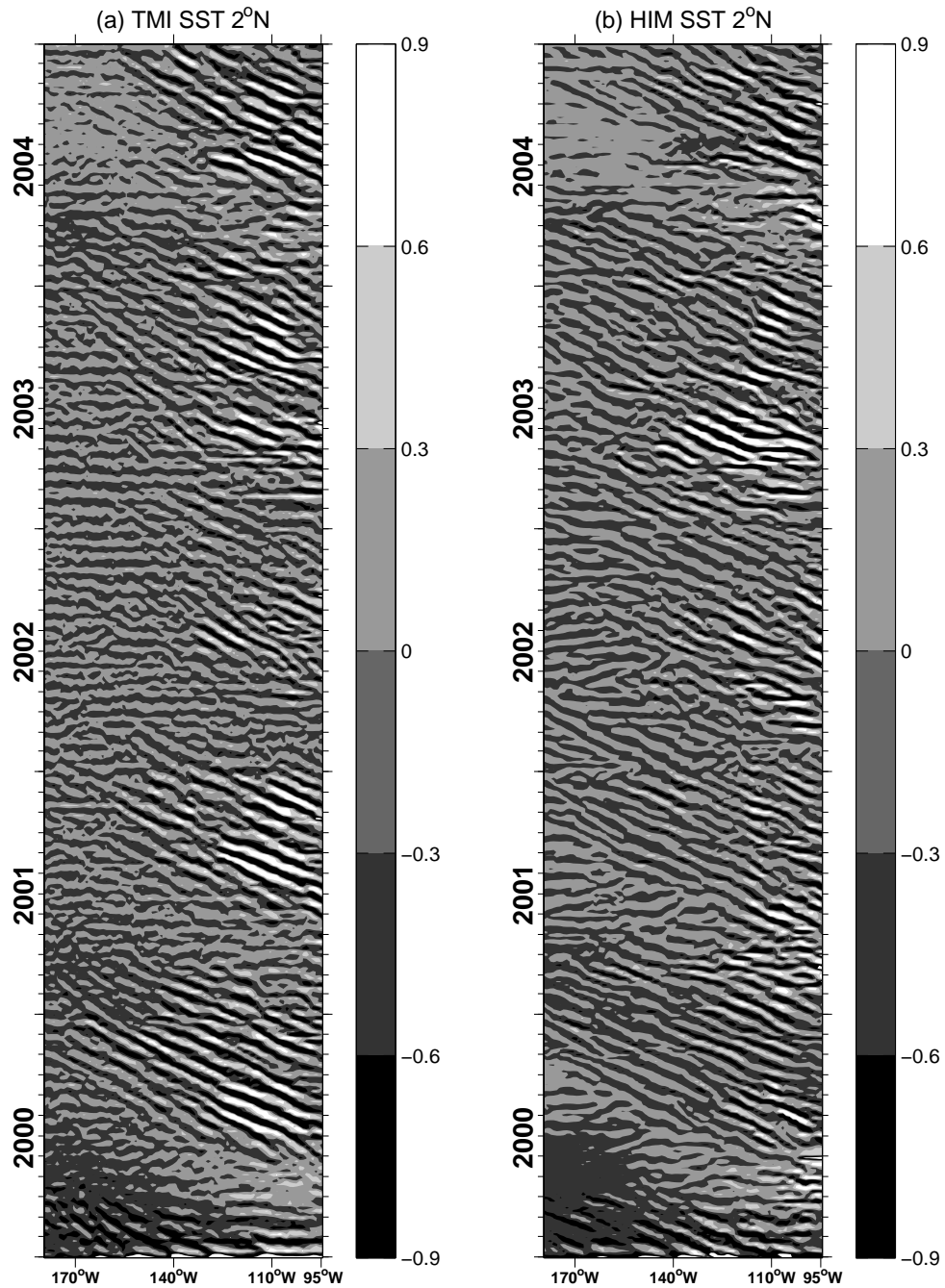


Figure 5: Time-longitude plots of the 30-day highpassed SST ($^{\circ}C$) along $2^{\circ}N$ for (a) TMI, and (b) the model.

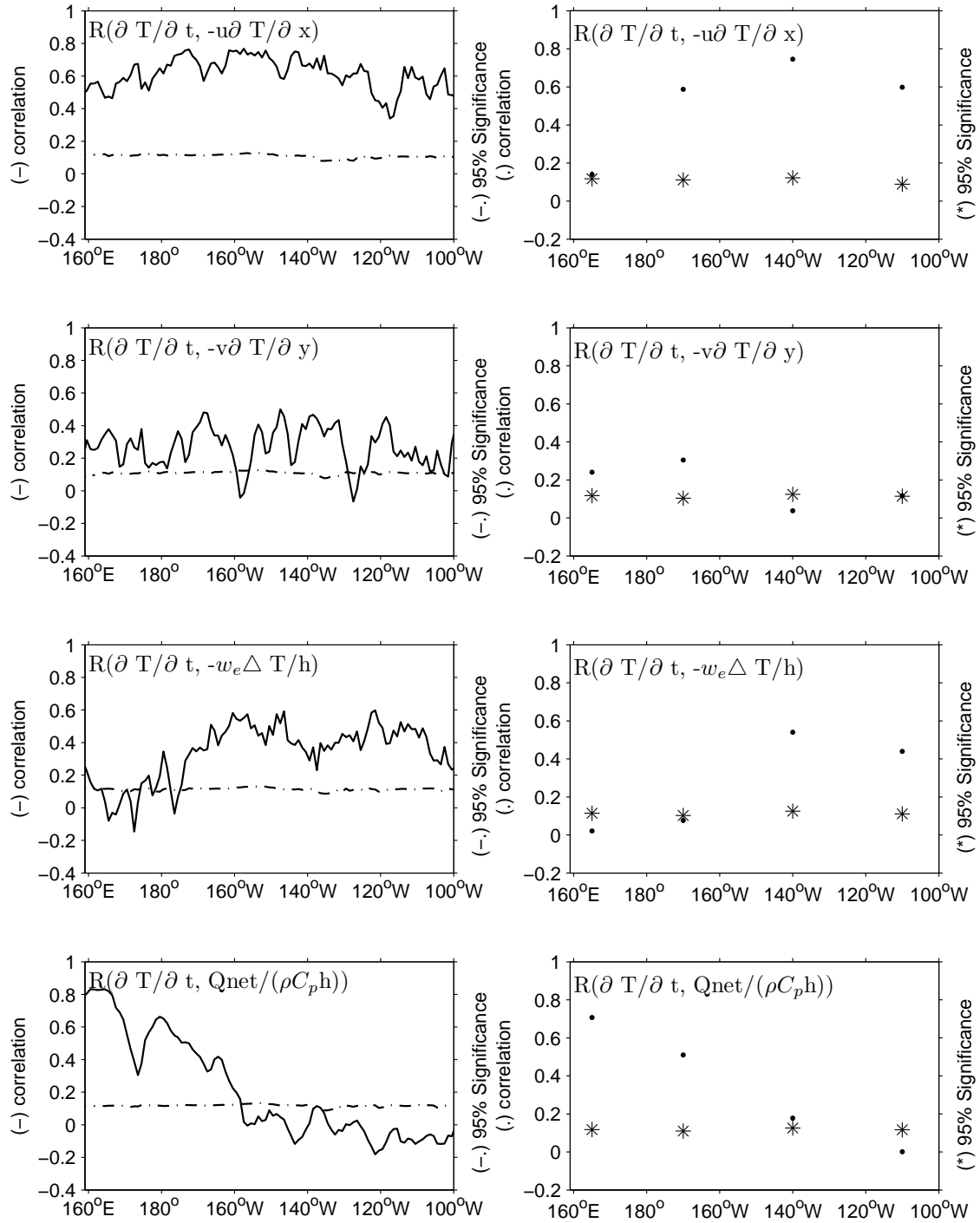


Figure 6: Correlations of the intra-seasonal temperature tendency with temperature budget terms: zonal advection, meridional advection, vertical diffusion and entrainment, and net surface heat flux (from top to bottom, left panel) along the equator. Corresponding values at four TAO buoys are shown in the right panel. Ninety-five percent confidence limits for the correlations (dash-dot lines in left panel, asterisks in right panel) are also shown.

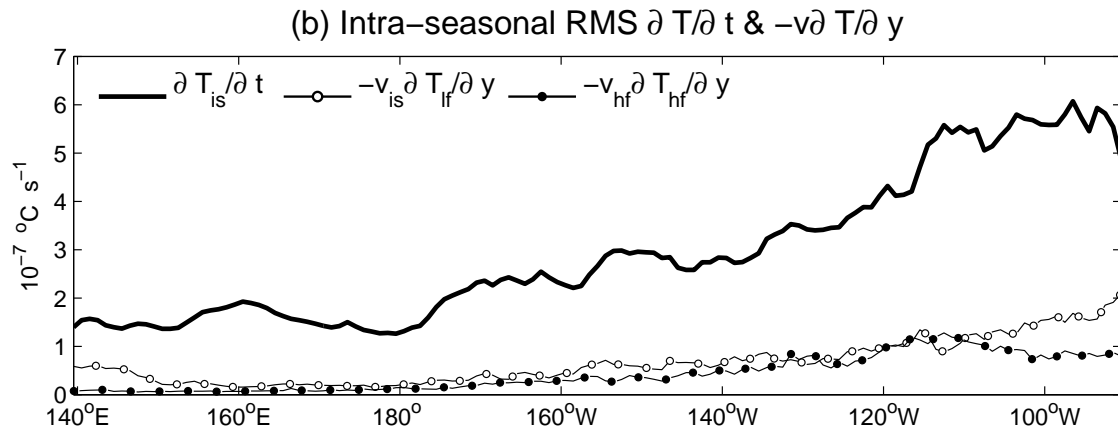
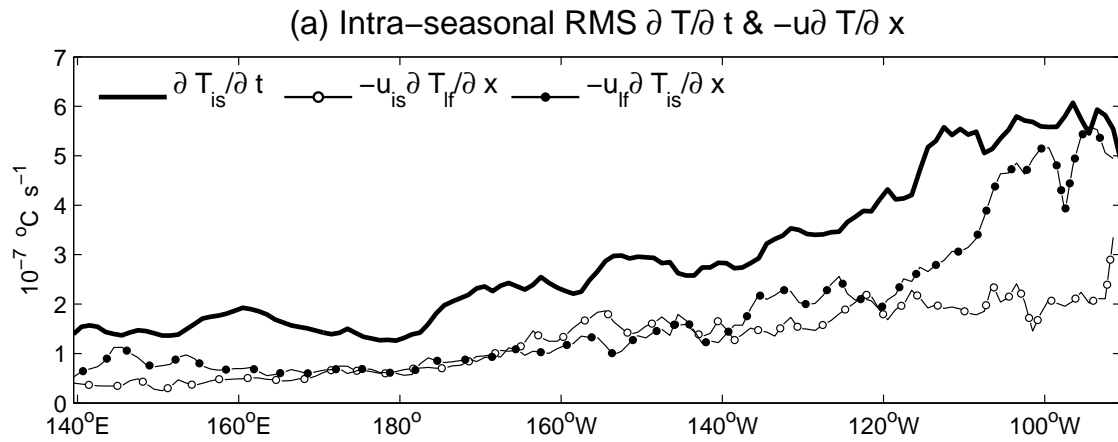


Figure 7: Root mean square (RMS) of the intra-seasonal temperature tendency and the decompositions of (a) the zonal advection, and (b) the meridional advection along the equator.

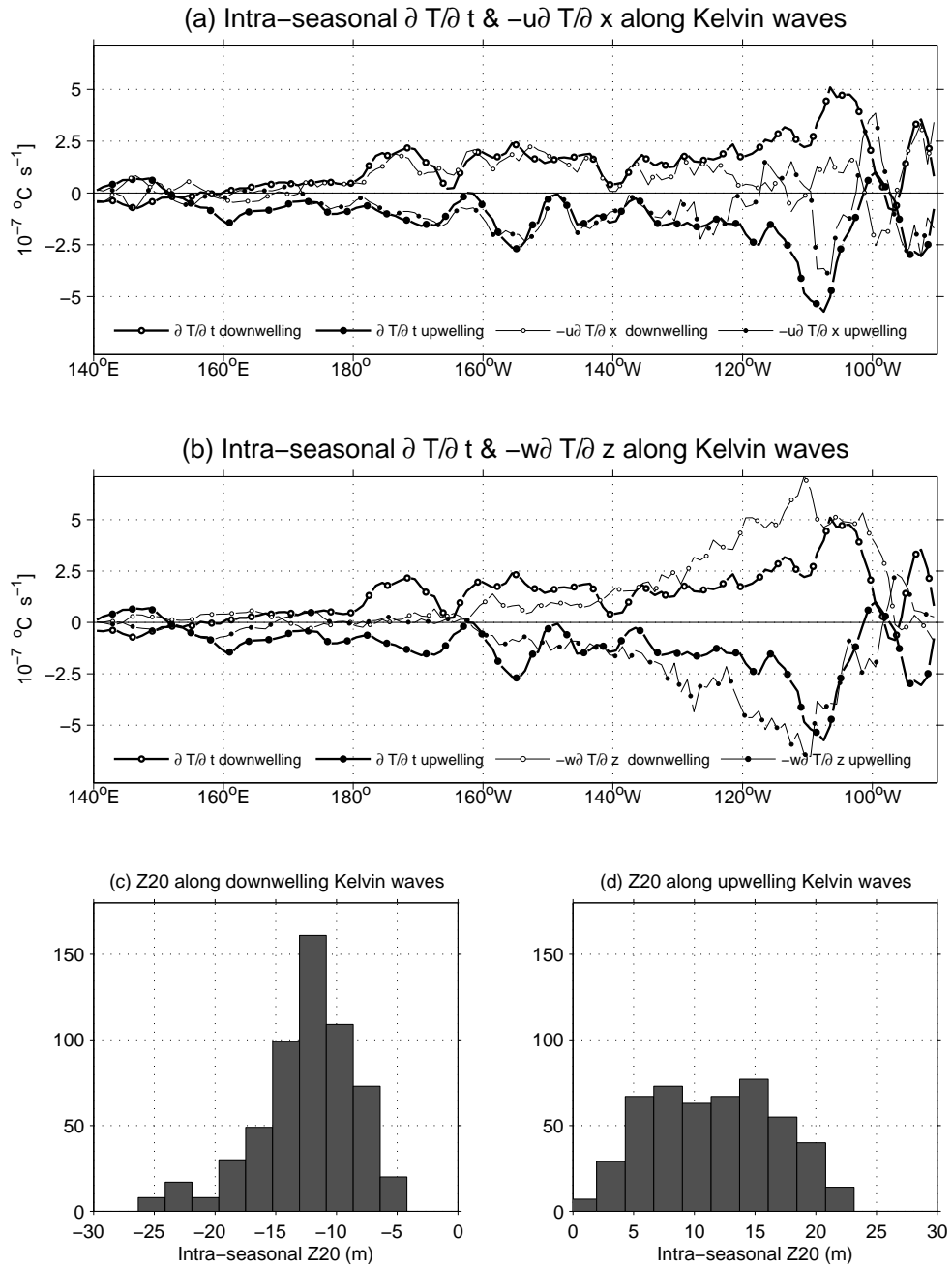


Figure 8: (a) The intra-seasonal temperature tendency versus zonal advection along composite Kelvin waves, (b) temperature tendency versus vertical diffusion and entrainment along composite Kelvin waves, (c) histogram of the intra-seasonal Z20 for all 14 downwelling Kelvin waves, and (d) histogram of the intra-seasonal Z20 for all 12 upwelling Kelvin waves.

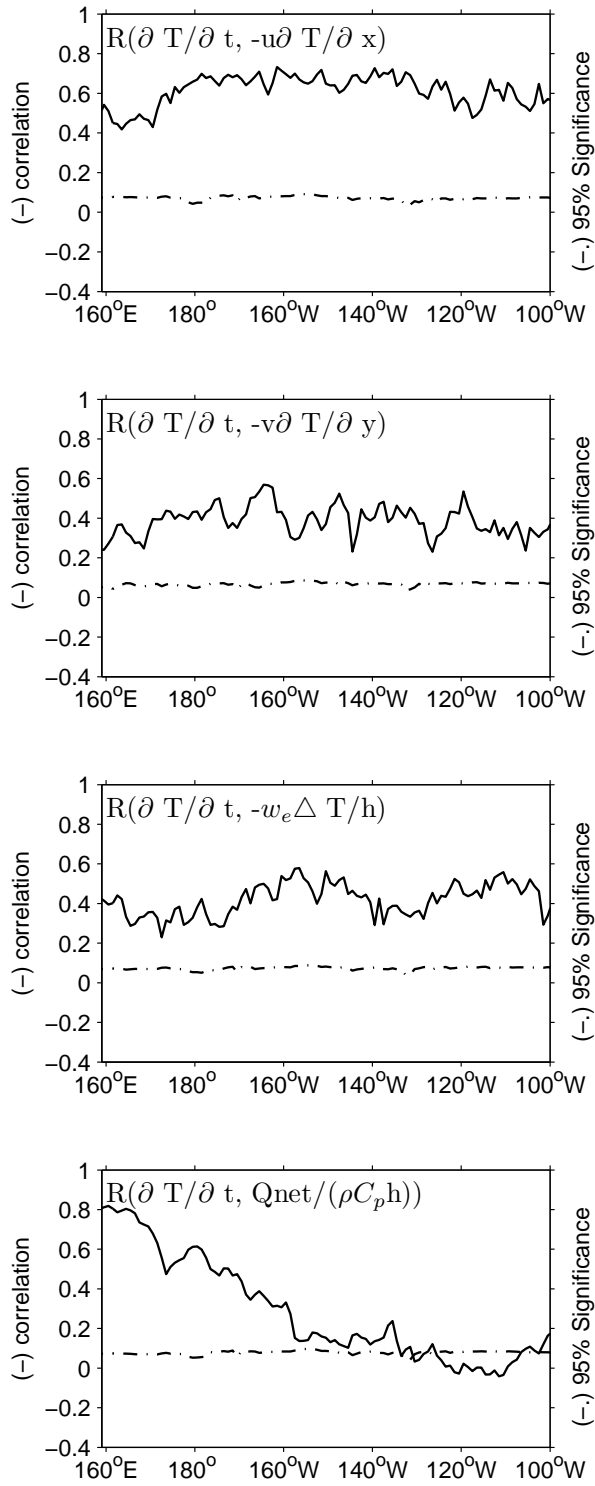


Figure 9: Same as Fig. 6 left panel, but for low-frequency signal.

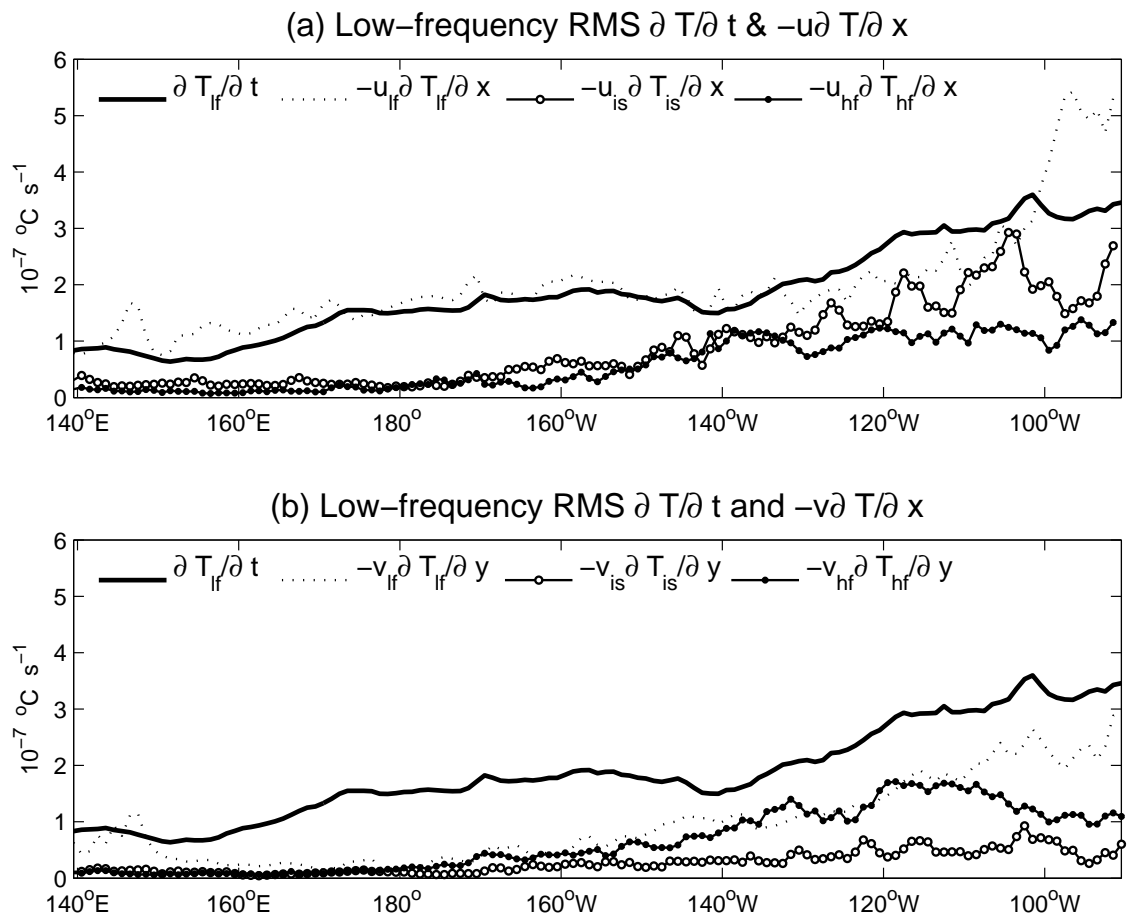


Figure 10: Same as Fig. 7, but for low-frequency signal and three largest terms.

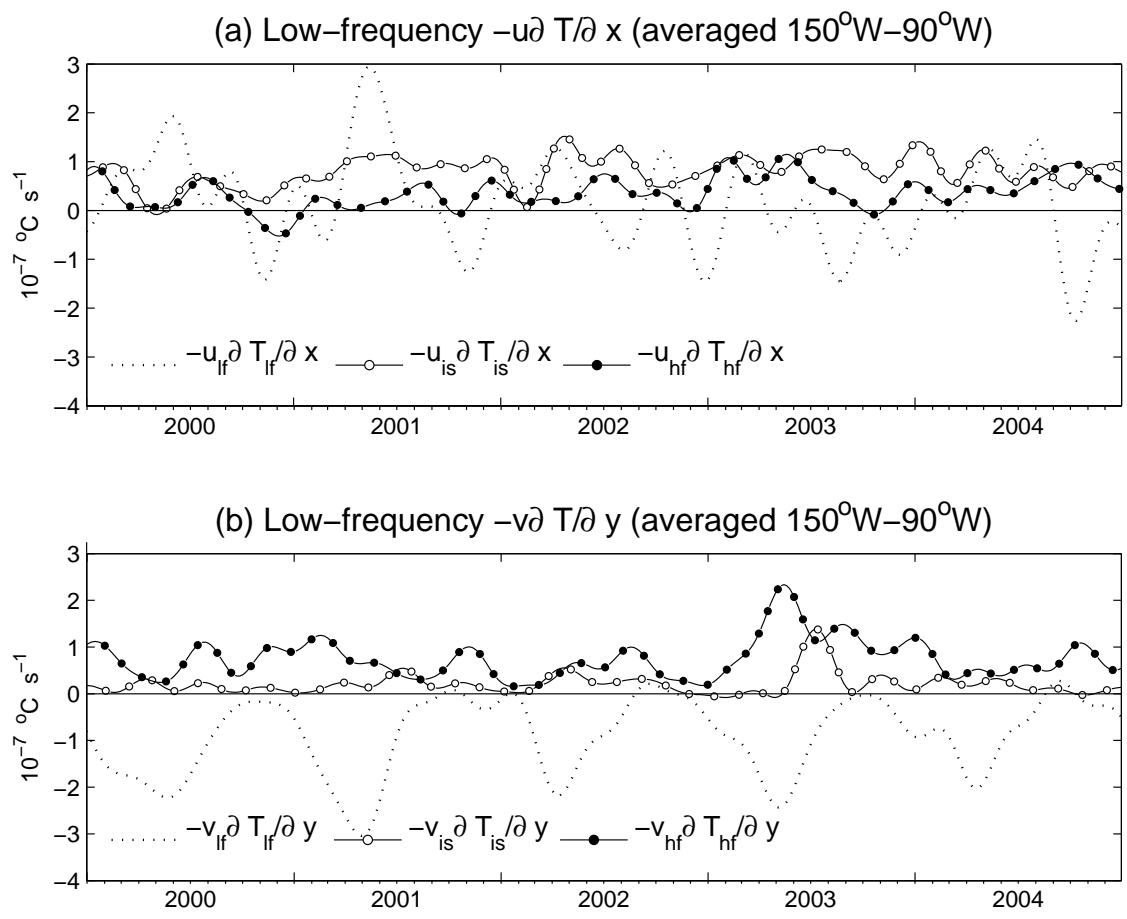


Figure 11: Time series of the largest three terms averaged from $150^\circ W - 90^\circ W$ in (a) zonal advection, and (b) the meridional advection from Jan 2000 to Dec 2004.

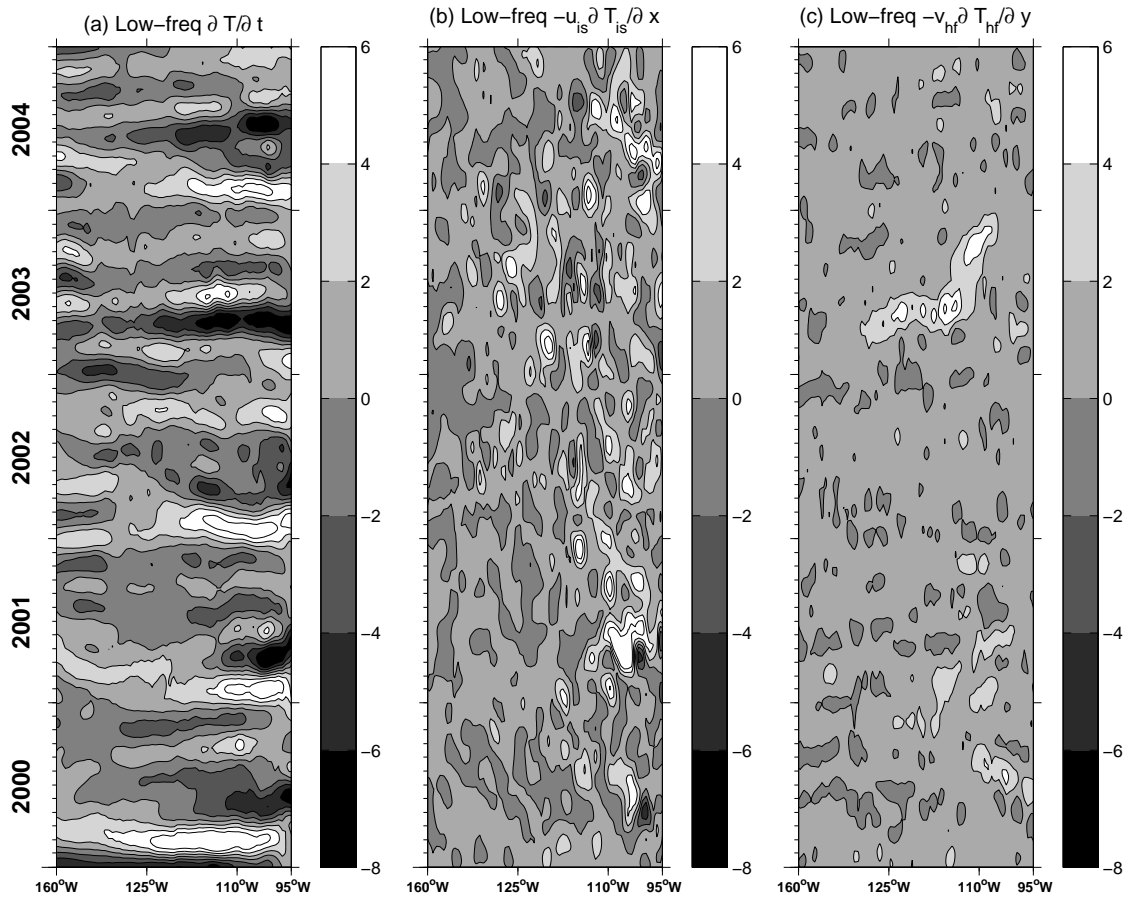


Figure 12: Time-longitude plots of the (a) low-frequency temperature tendency, (b) intra-seasonal zonal advection of the intra-seasonal zonal temperature gradient, and (c) high-frequency meridional advection of the high-frequency meridional temperature gradient. Units are $10^{-7} \text{ } ^\circ\text{C s}^{-1}$.

List of Tables

1	Physical interpretation of some crossterms in (2) and (3).	44
---	--	----

Table 1: Physical interpretation of some crossterms in (2) and (3).

Crossterms	Physical interpretation of advection terms
(a) $-u_{lf} \frac{\partial T_{is}}{\partial x}$	zonal advection of T anomalies from Kelvin waves by low-frequency velocity
(b) $-u_{is} \frac{\partial T_{lf}}{\partial x}$	zonal advection by velocity anomalies from Kelvin waves
(c) $-u_{lf} \frac{\partial T_{lf}}{\partial x}$	low-frequency zonal advection
(d) $-u_{is} \frac{\partial T_{is}}{\partial x}$	zonal rectification from Kelvin waves
(e) $-v_{hf} \frac{\partial T_{hf}}{\partial y}$	meridional rectification from TIWs