

**Physics 514, Winter Quarter 2018**  
**Electrodynamics: Homework Assignment 9**  
**Due March 9, either 11:00am in class or**  
**10:45am in the instructor's mailbox.**  
**This is an exam-review homework.**  
**Note only 2 problems will be graded.**

1. (graded problem) Show that in a good conductor the skin depth is  $\lambda/2\pi$  where  $\lambda$  is the wavelength in the conductor. Show that in a poor conductor the skin depth is  $\frac{2}{\sigma} \sqrt{\epsilon/\mu}$ .

2. The conductivity of air containing mobile electrons is given very approximately by  $\sigma = -i(Ne^2/\omega m)$  where  $e$  is the electron charge and  $m$  its mass. Find the resulting propagation velocity and hence the index of refraction  $n$ . This is related to radio waves bouncing off the ionosphere.

3. (graded problem) Consider a plane wave in a poor lossless conductor incident in the normal direction on a plane conducting surface. Show that the transmitted and reflected amplitudes are the same as those in the non-conducting case except the index of refraction in the conductor is now complex. That is, show in the conductor that the amplitudes are  $E_{0r} = \left(\frac{1-z}{1+z}\right) E_{0i}$  and  $E_{0t} = \left(\frac{2}{1+z}\right) E_{0i}$  with  $z=n_0/n_c$  (where  $n_0$  is the index of refraction in the poor conductor,  $n_c$  the complex index of refraction in the conductor, and  $\mu$  in both is  $\mu_0$ ).

4. A waveguide consists of two almost-infinite parallel conducting sheets separated by a gap  $L$ . A plane wave having free-space wavelength  $\lambda_0$  enters the guide at an angle  $\theta_0$  relative to the normal to the sheet. Find the guide phase velocity and wavelength.