

Physics 322, Winter Quarter 2016

Electrodynamics: Homework Assignment 6

(a) Turn in all problems and clearly note all constants and assumptions you use.

(1-point penalty each otherwise)

(b) Use 8½ x 11 paper & staple

(1-point penalty each otherwise)

(c) Due February 18 either 9:00 am in class or 8:45 am in the instructor's mailbox; late homework gets 0.

1. Conduction versus displacement currents. Consider copper threaded by an alternating electric field $E_0 \cos \omega t$, with frequency $\omega/2\pi = 1$ Hz. You can assume the permittivity of copper is close to ϵ_0 .

a. Find the ratio of the magnitude of the displacement current to the magnitude of the conduction current. Which dominates at typical radio frequencies?

b. Is the conduction current in-phase or out-of-phase with the electric field? If out-of-phase, by how much does the conduction current lead or lag (specify which)?

c. Is the displacement current in-phase or out-of-phase with the electric field? If out-of-phase, by how much does the current lead or lag (specify which)?

2. Magnetic pressure. Consider a long solenoid carrying current I , of radius R , length L , with n turns/length. Notice the $\mathbf{B}$ field at the windings applies a force to the windings. The current is held constant while the magnetic pressure expands the radius of the solenoid by dR . according to the principal of virtual work.

a. Find the resulting increase in the magnetic energy.

b. A source supplies the current. Find the extra energy the source needs to supply for the expansion to take place. Hint: Why might the source need to increase its voltage?

- c. Explain why your answers in a and b are different.
- d. Hence, find the magnetic pressure. That is: suppose you had a difference in parallel $\mathbf{B}$ across a surface, find the pressure on the surface.

3. A cylinder of length L and radius R carries a uniform current density $\mathbf{J}$ in the axial direction. Consider a charged particle beam entering the end of the solenoid in the axial direction. Each beam particle carries charge q and has momentum P .

- a. Relative to the direction of the current, what's the direction of the particle beam so the beam is focused (and not de-focused)?
- b. Find the focal length of the cylinder. You can assume the focal length is much longer than the length of the cylinder (the thin lens approximation).

4. A very simple plasma is a material containing charge carriers and having conductivity σ . Suppose the plasma is threaded by a magnetic field $\mathbf{B}(\mathbf{r},t)$, where $\mathbf{r}$ is some position in the plasma. For simplicity, assume the permittivity and permeability are ϵ_0 and μ_0 . Find $\nabla^2 \mathbf{B}$. This is one of many “plasma equations”.