

Electrodynamics III: Assignment 6

Due May 15 at 11:00 am.

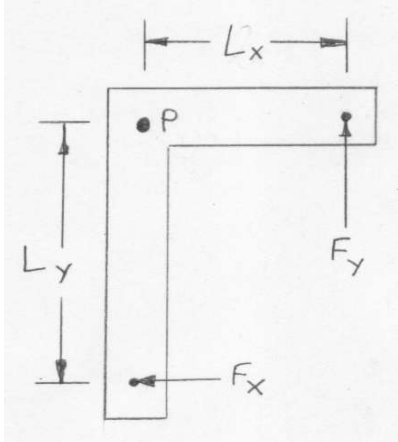
- 1. Scan your solutions as a single PDF file**
- 2. Name your file HW6-*lastname*.pdf**
- 3. Attach your file to an email...**
- 4. ... with subject line HW6-*lastname* ...**
- 5. ... and send the email to ljrosenberg@phys.washington.edu**

1. Show by direct calculation that the Lorentz transformation applied to the field tensor $F_{\mu\nu}$ gives the transformed fields of Jackson equation 11.147.

2. Show that if a divergenceless 4-vector A^μ has non-zero components in a bounded spatial region, then the Euclidian-volume integral over 3D space $\iiint A^4 dv$ is a Lorentz invariant. Hint: you may want to apply the 4D analog of Gauss's law we introduced in class. For that surface integration: since da_μ is a component of the 3D "surface" normal to the vector A^μ in 4-space, $da_4 = dv$.

3. Consider the static "Minkowski lever" from lecture, below. Suppose this system is viewed by an observer moving in the direction of one of the arms at speed v .

- What's the torque according to the moving observer?
- Explain the principle that forbids the system from undergoing rotation in one inertial frame and not undergoing rotation in another inertial frame.
- Explain how you can reconcile the result of part a and part b.



4. Show from tensor algebra that the field tensor $F_{\mu\nu}$, and therefore the fields, is invariant under the covariant form of the gauge transformation.