## Physics 321, Autumn Quarter 2015 Electrodynamics: Homework Assignment 6 (a) Turn in all problems and clearly note all constants and assumptions you use. (1-point penalty each otherwise) (b) Use 8½ x 11 paper & staple (1-point penalty each otherwise) Due 9:30 am Thursday November 12

1. Challenge problem. Consider the capacitor shown below. Each plate has length *L* and width *W*. The capacitor plates are not quite parallel. The gap is *d* on one side and  $d+\delta d$  on the other. Ignoring fringing fields, find the electrostatic potential between the plates. Hint: this problem has multiple symmetries: how can these symmetries be applied to Laplace's equation?



2. Consider two semi-infinite grounded planes joining at an angle  $\pi/3$  as shown below. A charge +Q is not necessarily along the mid-plane. Make a careful sketch showing the size and positions of charges for the corresponding image-charge problem.

3. Consider a lightning cloud drifting overhead. At the earth's surface you measure a vertical electric field of magnitude 100 Volts/meter. Suppose the bottom of the cloud is 300 m above the earth surface and the top of the cloud is 600 m above the earth surface. The simplified charge distribution of the cloud is such that its total charge is zero, but it has charge -Q at the very bottom, and charge +Q at the very top. (a) Estimate the magnitude of the charge Q. (b) Estimate the force on the cloud. Hint: the earth surface is a reasonably good ground plane.

4. Consider the linear arrangement of charges as shown below. Assume the separation *d* of the charges is small relative to their distance *r* to the field point located at  $(r, \theta, \phi)$  in spherical coordinates. Find to lowest non-trivial order (in r) the electrostatic potential at the field point.

